

FN201: Lecture Note 5

Investment Criteria and Decision

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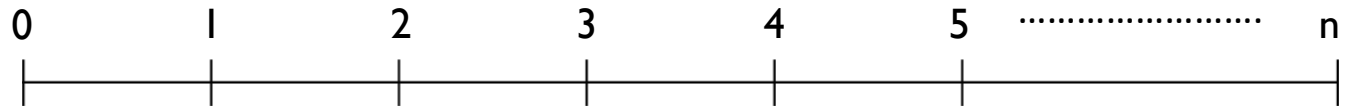
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Project Decision

1. Replacement needed to continue profitable operations
2. Replacement to reduce costs
3. Expansion of existing products or markets
4. Expansion into new products or markets
5. Contraction decisions
6. Safety and/or environmental projects
7. Mergers
8. Others (i.e. catch-all items)

Overview

Investment time line



Decision Tools

1. Net Present Value (NPV)
2. Internal Rate of Return (IRR)
 - Modified Internal Rate of Return (MIRR)
3. Profitability Index (PI)
4. Payback period (PP)
 - Regular PP
 - Discounted PP

1 Net Present Value (NPV)

= PV value of a project's cash inflows minus PV of its costs (cash outflows)

$$\begin{aligned} NPV &= CF_0 + \frac{CF_1}{(1+r)^1} + \frac{CF_2}{(1+r)^2} + \dots + \frac{CF_N}{(1+r)^N} \\ &= \sum_{t=0}^N \frac{CF_t}{(1+r)^t} \end{aligned}$$

1 Net Present Value (NPV)

Example: Find Net Present Value of these projects when cost of capital = 12%

| Year | Expected Net Cash Flows | |
|------|-------------------------|-----------|
| | Project X | Project Y |
| 0 | -10,000 | -10,000 |
| 1 | 6,500 | 3,500 |
| 2 | 3,000 | 3,500 |
| 3 | 3,000 | 3,500 |
| 4 | 1,000 | 3,500 |

1 Net Present Value (NPV)

Decision criteria:

1. Independent projects
2. Mutually exclusive projects

2 Internal Rate of Return (IRR)

= the discount rate that forces the PV of cash inflows to equal the PV of cash outflows

$$\begin{aligned} NPV &= CF_0 + \frac{CF_1}{(1+IRR)^1} + \frac{CF_2}{(1+IRR)^2} + \dots + \frac{CF_N}{(1+IRR)^N} \\ &= \sum_{t=0}^N \frac{CF_t}{(1+IRR)^t} = 0 \end{aligned}$$

2 Internal Rate of Return (IRR)

Example: Find the Internal Rate of Return (IRR) of these projects

| Year | Expected Net Cash Flows | |
|------|-------------------------|-----------|
| | Project X | Project Y |
| 0 | -10,000 | -10,000 |
| 1 | 6,500 | 3,500 |
| 2 | 3,000 | 3,500 |
| 3 | 3,000 | 3,500 |
| 4 | 1,000 | 3,500 |

2 Internal Rate of Return (IRR)

The assumption of reinvestment of project cash flows does not generally hold!

Modified Internal Rate of Return (MIRR)

$$\sum_{t=0}^N \frac{COF_t}{(1+r)^t} = \frac{\sum_{t=0}^N CIF_t (1+r)^{N-t}}{(1+MIRR)^N}$$

$$PV \text{ Costs} = \frac{\text{Terminal Value (TV)}}{(1+MIRR)^N}$$

2 Internal Rate of Return (IRR)

Example: Find the Modified Internal Rate of Return (MIRR) of these projects when reinvestment rate = cost of capital at 12%

| Year | Expected Net Cash Flows | |
|------|-------------------------|-----------|
| | Project X | Project Y |
| 0 | -10,000 | -10,000 |
| 1 | 6,500 | 3,500 |
| 2 | 3,000 | 3,500 |
| 3 | 3,000 | 3,500 |
| 4 | 1,000 | 3,500 |

MIRR **X = 14.61%** **Y = 13.73%**

IRR **X = 18.03%** **Y = 14.96%**

2 Internal Rate of Return (IRR)

Decision criteria:

1. Independent projects

MIRR exceeds cost of capital

2. Mutually exclusive projects

Highest MIRR project

Net Present Value vs. Internal Rate of Return Decision
for mutually exclusive projects

NPV vs. IRR

A) when cost of capital = 12%

NPV

$$X = \$966.01$$

$$Y = \$630.72$$

IRR

$$X = 18.03\%$$

$$Y = 14.96\%$$

MIRR

$$X = 14.61\%$$

$$Y = 13.73\%$$

B) what if cost of capital = 5%

NPV

$$X = \$2,325.78$$

$$Y = \$2,410.83$$

IRR

$$X = 18.03\%$$

$$Y = 14.96\%$$

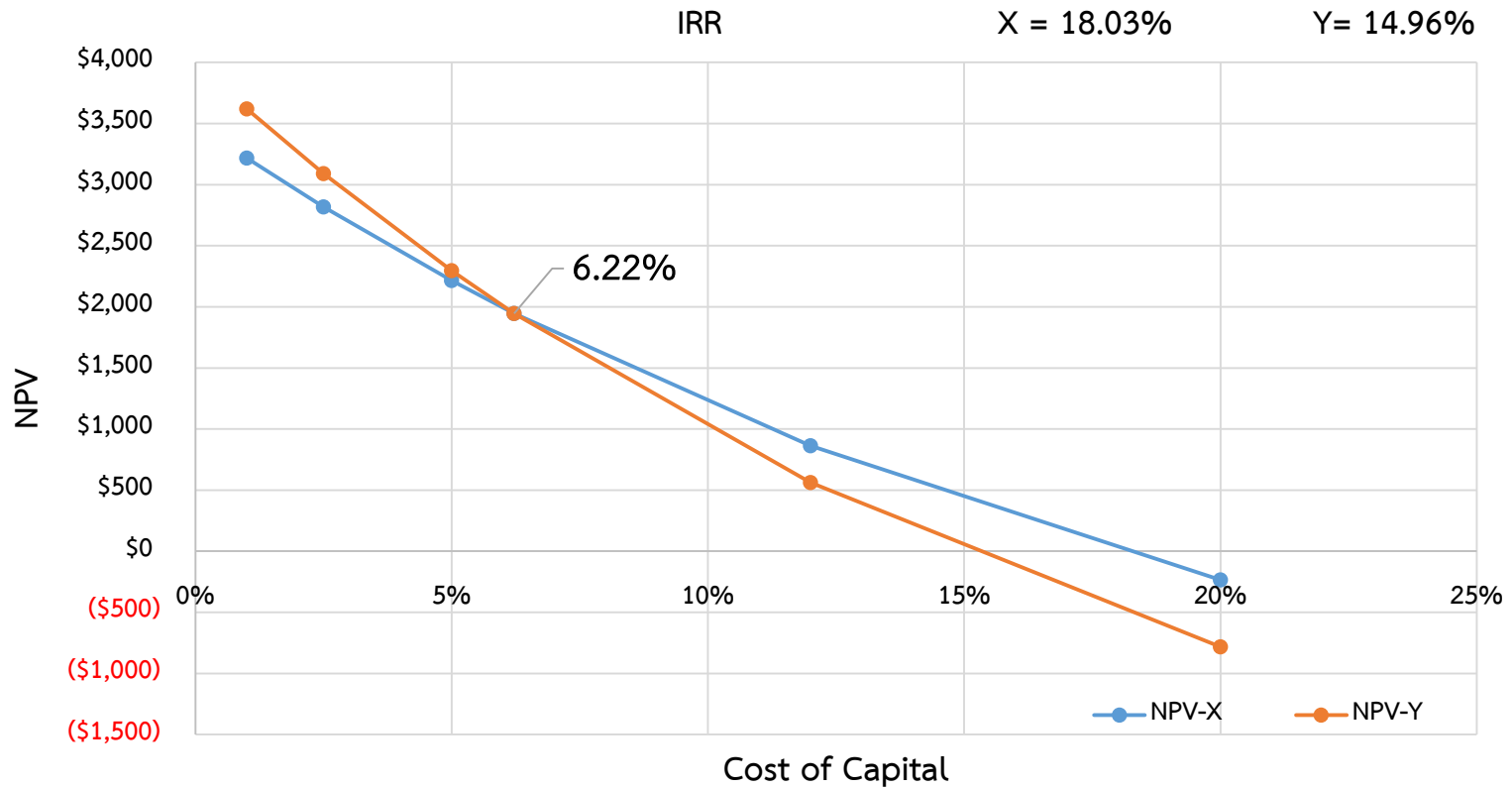
MIRR

$$X = 14.61\%$$

$$Y = 13.73\%$$

NPV vs. IRR

Net Present Value Profiles



NPV vs. IRR

Conflicts arise because:

1. Timing differences of project cash flows
2. Project size (initial investment) differences

Which one is better?

3 Profitability Index (PI)

$$PI = \frac{PV \text{ of future cash flow}}{\text{initial investment}} = \frac{\sum_{t=1}^N \frac{CF_t}{(1+r)^t}}{CF_0}$$

3 Profitability Index (PI)

Example: Find the Profitability Index (PI) of these projects when cost of capital = 12%

| Year | Expected Net Cash Flows | |
|------|-------------------------|-----------|
| | Project X | Project Y |
| 0 | -10,000 | -10,000 |
| 1 | 6,500 | 3,500 |
| 2 | 3,000 | 3,500 |
| 3 | 3,000 | 3,500 |
| 4 | 1,000 | 3,500 |

4 Payback Period

= the number of years required to recover the fund invested in a project from its operating cash flows

$$\text{Payback} = \begin{array}{c} \text{Number of years} \\ \text{prior to full} \\ \text{recover} \end{array} + \frac{\text{Unrecovered cost at} \\ \text{start of year}}{\text{Cash flow during full} \\ \text{recovery year}}$$

4 Payback Period

Example: Find the regular and discounted payback period of these projects given cost of capital = 12%

| Year | Expected Net Cash Flows | |
|------|-------------------------|-----------|
| | Project X | Project Y |
| 0 | -10,000 | -10,000 |
| 1 | 6,500 | 3,500 |
| 2 | 3,000 | 3,500 |
| 3 | 3,000 | 3,500 |
| 4 | 1,000 | 3,500 |

Question?