

→ Quick recap

→ Stages

→ Value fn

→ Riskless loss aversion

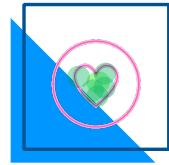
→ Measuring loss aversion

The endowment effect
Mus Exp



PROSPECT THEORY

EPISODE 1



EE 434 Behavioral Finance, SEM1/2021

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From comparing expected value to comparing Prospect theory value

Suppose you have initial wealth w , Consider two lotteries

$$X = (x_1, p; x_2, 1 - p) \text{ vs. } Y = (y_1, q; y_2, 1 - q)$$

You will prefer lottery X over lottery Y IF....

$(x_1, p ; x_2, 1-p)$

$(y_1, q ; y_2, 1-q)$

From comparing expected value to comparing Prospect theory value

We will choose X over Y if:

➤ Expected Value Theory

$$p(w+x_1) + (1-p)(w+x_2)$$

$$(w) + px_1 + (1-p)x_2 > w + qy_1 + (1-q)y_2$$

➤ Expected Utility Theory

$$pU(w+x_1) + (1-p)U(w+x_2) > qU(w+y_1) + (1-q)U(w+y_2)$$

➤ Prospect theory

$$\pi(p)v(x_1) + \pi(1-p)v(x_2) > \pi(q)v(y_1) + \pi(1-q)v(y_2)$$

Prospect Theory: Stages

In order to consider prospects, individuals go through two stages:

- (1.) Editing stage
- (2.) Evaluation stage

Prospect Theory: Editing Stage

This is the stage of organizing & reformulating the problem.

Taking an objective prospect $(\hat{x}_1, \hat{p}_1; \dots; \hat{x}_m, \hat{p}_m)$ and

transforming it into an object for evaluation $(x_1, p_1; \dots; x_n, p_n)$

by:

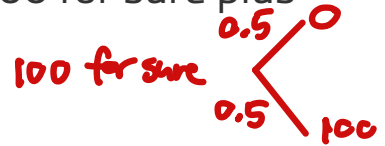
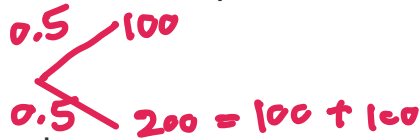
Prospect Theory: Editing Stage

❖ **Coding:** code outcomes as gains & losses relative to reference point.

~~$\pi(0.5)v(100) + \pi(0.5)v(100)$~~

❖ **Combination:** e.g., (100, .5; 100, .5) replaced with (100, 1). $\Rightarrow \pi(1)v(100)$

❖ **Segregation:** e.g., (100, .5; 200, .5) replaced with 100 for sure plus (0, .5; 100, .5).

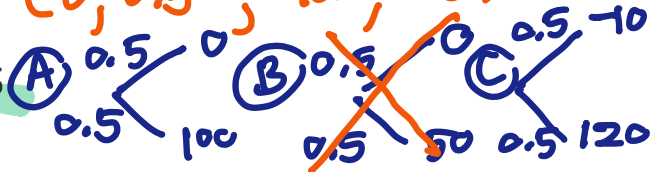


❖ **Cancellation:** discard shared components.

❖ **Simplification:** rounding of probabilities.

~~$(0, 0.488789; 100, 0.510321)$~~
 ~~$(0, 0.5; 100, 0.5)$~~

❖ **Eliminating dominated alternatives**



Prospect theory: Evaluation stage

A prospect can be written as $(x, p; y, q)$ with $p + q \leq 1$.

Note: $p + q < 1$ implies prospect yields 0 with probability $1 - p - q$.

A person evaluates a prospect $(x, p; y, q)$ according to the functional

$$V(x, p; y, q) = \pi(p)v(x) + \pi(q)v(y)$$

note:
Cumulative
Prospect theory
 $(x_1, p_1; \dots; x_n, p_n)$

Note: Nowadays, it might be best to take Prospect theory as a theory for simple prospects with at most two non-zero outcomes.

Prospect Theory's Value Function



Prospect Theory: Value Function

Three key features of the value function $v(\cdot)$:

❖ The carriers of value are changes in wealth (~~$v(\cdot) = 0$~~).

$v(0) = 0$

the value function at the reference point (at 0) is normalized to be 0.

❖ Diminishing sensitivity to the magnitude of changes:

CONCAVE in the gain domain *CONVEX* in the loss domain
 $v''(x) < 0$ for $x > 0$, $v''(x) > 0$ for $x < 0$.

❖ Loss aversion: losses loom larger than gains.

slope of $v(\cdot)$ in loss domain

$\frac{v'(x) \text{ when } x < 0}{v'(x) \text{ when } x > 0} > 1$, or $(y, 0.5; -y, 0.5) > (x, 0.5; -x, 0.5)$ if $0 < y < x$

slope of $v(\cdot)$ in gain domain

$\pi(0.5)v(x) + \pi(0.5)v(-y) > \pi(0.5)v(x) + \pi(0.5)v(-x)$
 $v(-y) - v(-x) > v(x) - v(y)$

Prospect Theory: Value Function

Two common functional forms for the value function:

Tversky & Kahneman (1992)

$$v(x) = \begin{cases} x^\alpha & \text{if } x > 0 \\ -\lambda(-x)^\beta & \text{if } x < 0 \end{cases}, \text{ where } \alpha, \beta \in (0,1] \text{ and } \lambda \geq 1$$

Two-part linear : *no diminishing sensitivity*
highlight the role of loss aversion

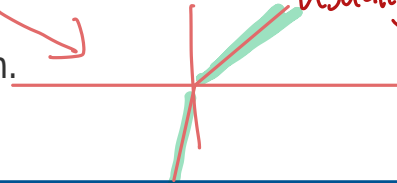
$$v(x) = \begin{cases} x & \text{if } x > 0 \\ \lambda x & \text{if } x < 0 \end{cases}, \text{ where } \lambda \geq 1$$

if $\lambda = 1$: no loss aversion

\Rightarrow higher λ , higher loss aversion

usually consider $\lambda > 1$

λ is the coefficient of loss aversion.



$v(x) = \lambda x$ $v(x)$

$v(x) = x$

Risk seeking

Risk averse

Risk-averse behavior

loss-averse

diminishing sensitivity
in the gain domain

change in wealth x

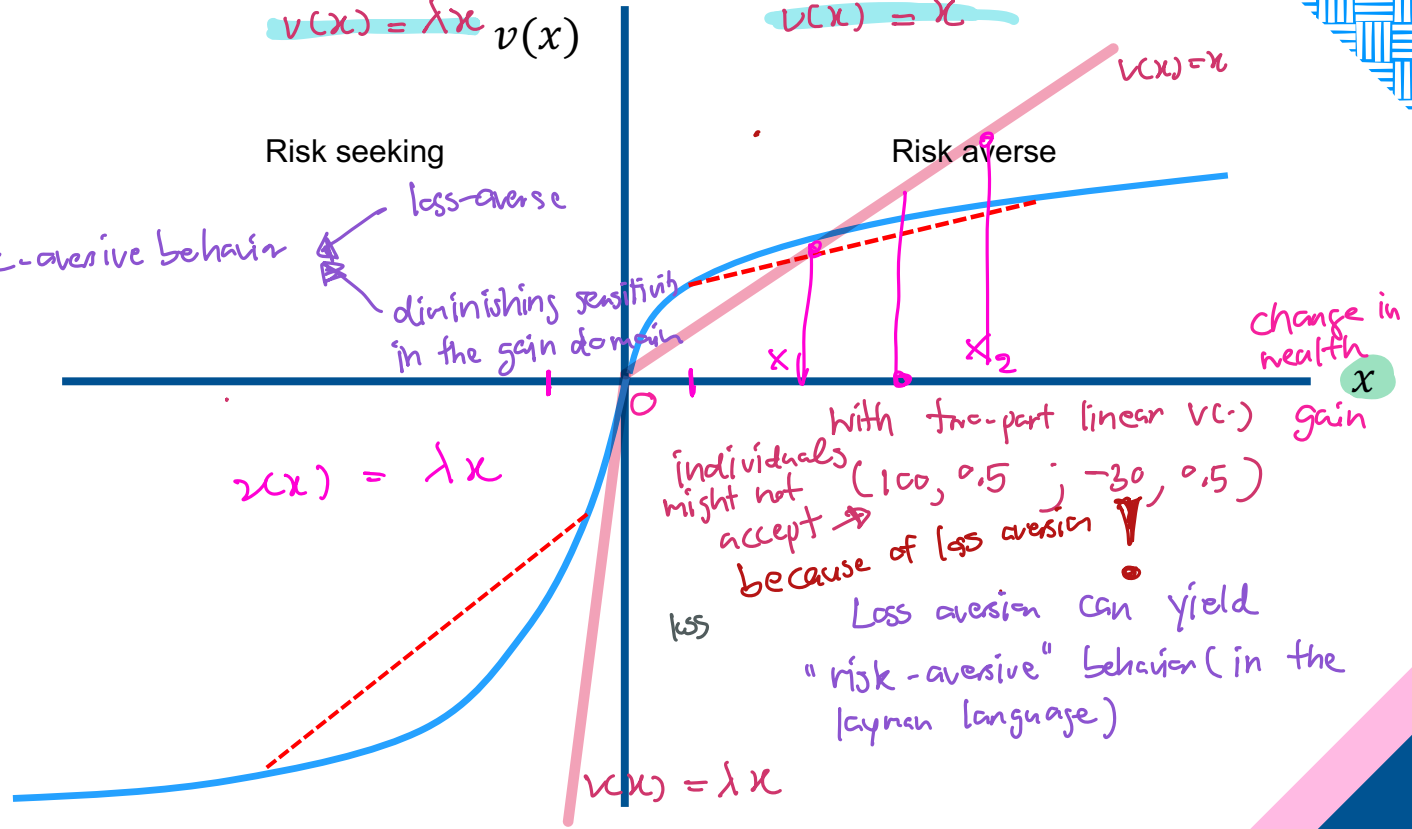
$v(x) = \lambda x$

$v(x) = \lambda x$

with two-part linear $v(\cdot)$ gain
individuals might not accept \rightarrow
 $(100, 0.5 ; -30, 0.5)$
because of loss aversion!

loss

Loss aversion can yield
"risk-averse" behavior (in the
Talmud language)



Risk aversion over gain & Risk seeking over loss

In a situation where a sure loss is compared to a gamble with probable larger loss, diminishing sensitivity cause risk seeking.

In a situation where a sure gain is compared to a gamble with probable larger gain, diminishing sensitivity cause risk aversion.

At the same level of wealth, an individual can both be risk averse and risk seeking.

Riskless Loss Aversion

Loss aversion can also be viewed in a riskless context.

Experiments have examined people's willingness to pay for a good, compared to their willingness to accept money in exchange for the same good.

$$\begin{aligned} \text{WTP} &\rightarrow \text{gain domain} \\ = \\ \text{WTA} &\rightarrow \text{loss domain} \end{aligned}$$

Willingness to Pay(WTP) vs. Willingness to Accept(WTA)

Standard economic theory says that an individual has a single value (i.e. some price p) that she associates with any good

- ✓ If she is given the opportunity to buy the good at (or below) that price, she will pay it. The price is her "willingness to pay(WTP)". \Rightarrow Potential Buyers
*Originally, you don't have it : The money you are willing to sacrifice in order to gain something.
don't have it \rightarrow have it*
- ✓ Similarly, if someone offers to buy the good from her at (or above) that price, she will accept it. The price is her "willingness to accept". (WTA) *of something*
*Originally, you have it : The money you feel that it is enough to compensate for your loss
have it \rightarrow don't have it*
 \Rightarrow Potential sellers
- ✓ Standard economic theory says that ----- $WTP = WTA$

How to support that "loss aversion" is true?

RICHARD
THALER

Around the same time Kahneman and Tversky were working on their model of Prospect Theory, economist Richard Thaler was noticing (and writing about) some of his own "anomalies". Thaler (1980) attributes gap between WTP and WTA to what he coined **the endowment effect**.

$WTP < WTA$: why?

The Endowment Effect

Traditionally,
 $WTP = WTA$
Because you value something the same regardless of whether you own it or not.

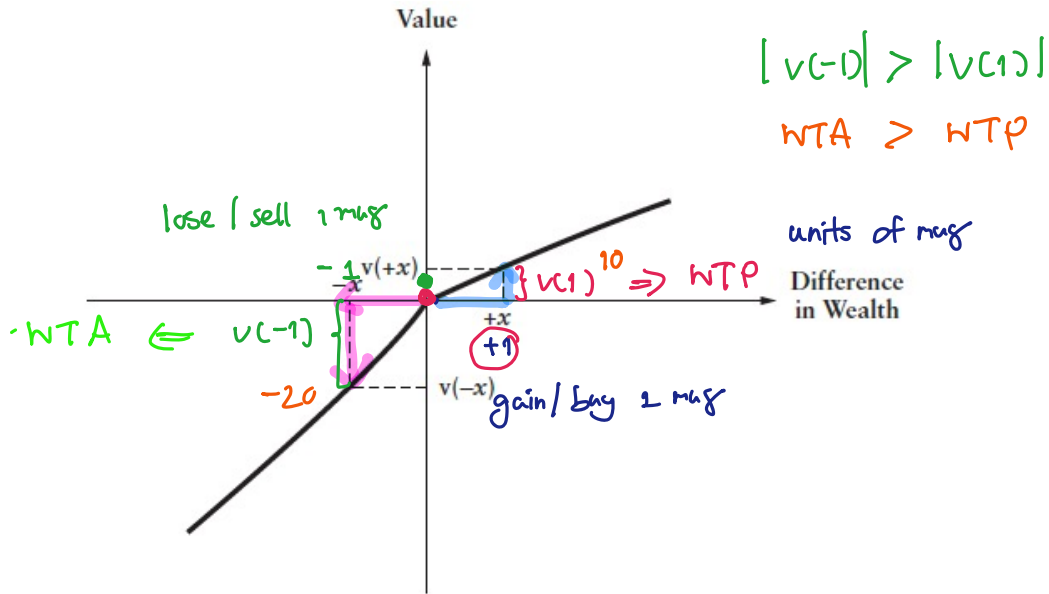


The Endowment effect



- The term endowment effect is used because the value of a good seems to increase once a person owns it.
- This is consistent with prospect theory because losses (i.e., giving up the good) are felt much more strongly than gains (receiving the good).

The Endowment effect



$$|v(-1)| > |v(1)|$$

$$WTA > WTP$$

The absolute value of $v(-x)$ is more than the value of $v(x)$.

Endowment Effect: Mug Experiment



Kahneman, Knetsch, and Thaler (1990) test these ideas in their famous “mug experiments” at Cornell University.

Experiment: Class of 50 - 75 economics students.

After students sit down, half of them are given a coffee mug.

Endowment Effect: Mug Experiment



$WTA > WTP$
endowment effect



Potential "Sellers"

How much willing to accept
for the mug?

Potential Buyers

How much willing to pay
for the mug?

Each seller were given a coffee mug.

Each buyer were shown a coffee mug.

Endowment Effect: Mug Experiment

Students are given cash and asked how much they would be willing to pay for a mug with the university's emblem.

Then another group of students is given mugs and asked how much they would accept in return.

In one session the students were willing to pay only \$1.34 for a mug, yet others would not accept less than \$8.83 for the exact same mug.

Measuring Loss Aversion



"Risk Preferences" "elicitation"

Multiple price list
Would you accept the following bet? A coin toss where:

- (1) If tails, lose \$100, heads win \$150? → Yes → done No
- ⇒ (2) If tails, lose \$100, heads win \$160? → No → go on No
- (3) If tails, lose \$100, heads win \$170? No
- (4) If tails, lose \$100, heads win \$180? :
- (5) If tails, lose \$100, heads win \$190? :
- (6) If tails, lose \$100, heads win \$200? :
- (7) If tails, lose \$100, heads win \$210? :
- If tails, lose \$100, heads win \$220? :
- If tails, lose \$100, heads win \$230? :
- (10) If tails, lose \$100, heads win \$240? Yes

- If tails, lose \$100, heads win \$250? Yes
- (12) If tails, lose \$100, heads win \$260? Yes
- (100) If tails, \$100, \$10,000? Yes

what is the smallest gain that you need in order to at least compensate for the fear of loss from the coin toss?

hypothetical vs. real incentives

How loss averse is the average person?

Measuring Loss Aversion



For coin toss above, typical response is to be indifferent at gain = \$200

The ratio of the amount you'd need to win (to accept the bet) and the amount you could potentially lose is generally found in range 1.5 to 2.5.

People are reluctant to expose themselves to fair gambles because they are loss averse. Typically, for a 50/50 bet, the gain has to be at least twice as great as the loss.



win 20 € with $\frac{4}{8}$ prob

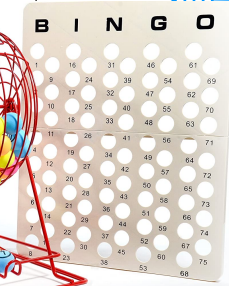
Win € 20 if one of the following balls is extracted:



If one of the following balls is extracted, then:



lose x € with $\frac{4}{8}$ prob.



-20	Lose € 20	O	1	€ 0 for sure
-19	Lose € 19	O	2	€ 0 for sure
	Lose € 18	O	3	€ 0 for sure
	Lose € 17	O	4	€ 0 for sure
	Lose € 16	O	5	€ 0 for sure
	Lose € 15	O	6	€ 0 for sure
	Lose € 14	O	7	€ 0 for sure
	Lose € 13	O	8	€ 0 for sure
	Lose € 12	O	9	€ 0 for sure
	Lose € 11	O	10	€ 0 for sure
	Lose € 10	O	11	€ 0 for sure

* The amount less that I firstly \rightarrow -11
feel indifferent to 50% chance
of winning € 20

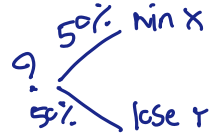
Accept the bet \equiv reject the bet
Reject the bet \equiv reject the bet
Sure amount of 0 Euro \equiv reject the bet



Measuring Loss Aversion



- Earlier, we measured the coefficient of loss aversion from answers to whether you would accept a bet with a 50% chance to win X , and a 50% chance to lose Y , where:



Coefficient of Loss Aversion = $\frac{X}{Y}$ for the smallest X given a fixed Y ,
OR for the largest Y given a fixed X

- We can also measure the coefficient of loss aversion using the endowment effect experiment:

$$\text{Coefficient of Loss Aversion} = \frac{WTA}{WTP}$$



DANKE!

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