

Homework # 3

1) Consider the problem of a representative consumer,

$$\text{Max } E_0 \left\{ \sum_{t=0}^{\infty} \beta^t (\ln c_t) \right\}, \quad 0 < \beta < 1$$

Subject to
$$c_t + L_{1t} + L_{2t} \leq d_t + L_{1t-1}R_{1t-1} + L_{2t-2}R_{2,t-2}$$

Where c_t is consumption at time t ,

L_{it} is the amount a perfectly safe loan that lent for i periods at t , and $i = 1, 2$,

R_{it-i} is the rate of returns of this perfectly safe loan for i periods,

d_t is a random dividend from a tree at

- 1) Find the price of a one period perfectly sure claim of 1 unit of consumption at $t+1$, (or R_{1t}^{-1}),
- 2) Find the price of a two period perfectly sure claim of 1 unit of consumption at $t+2$, (or R_{2t}^{-1}),
- 3) Under what situation that one has $R_{1t} \cdot E_t R_{1t} < R_{2t}$ in equilibrium. What is its economic rationality?