

1) (a)  $\text{varr } \beta_i = .7061 - .1512 \text{ pcnv.} - .0070 \text{ avgsent} + .0121 \text{ tottime} - .0393 \text{ ptime } \beta_i - .1031 \text{ qemp } \beta_i$

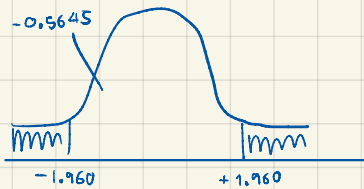
→ test the average sentence served

- Let  $H_0: \beta_3 = 0$ ,  $H_1: \beta_3 \neq 0$

-  $t_{\text{cal}} = \frac{\hat{\beta}_3 - \beta_3}{\text{se}_{\hat{\beta}_3}} = \frac{-0.0070 - 0}{0.0124} = -0.5645$

- critical values when degree of freedom is  $2725 - 6 = 2719$

$t_{\alpha/0.05} = \pm 1.960$



∴ can not reject  $H_0$  which means we can make sure that average sentence served parameter is not zero 95 percent

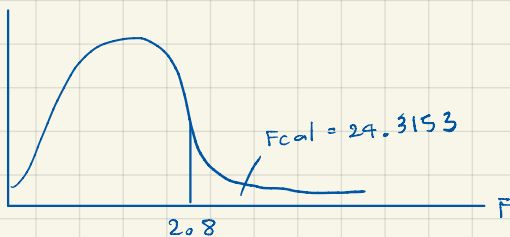
(b) Model (1.1)

→ Use F distribution to calculated

- Let  $H_0: \beta_2 = \beta_3 = \beta_4 = \beta_5 = \beta_6 = 0$ ,  $H_1: \text{otherwise}$

-  $F_{\text{cal}} = \frac{R^2 / (k-1)}{1 - R^2 / (n-k)} = \frac{0.0428 / (6-1)}{(1-0.0428) / (2725-6)} = 24.3153$

-  $F_{\text{upper}, \alpha}(6, 2719)$  when  $\alpha = 0.01 = 2.64$

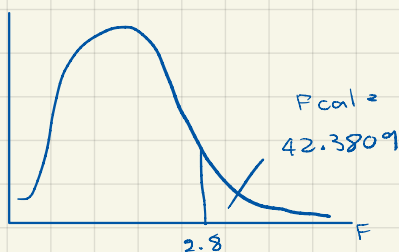


∴  $F_{\text{cal}} > F_{\text{upper}}(6, 2719)$   
we can reject  $H_0$ , in other word, we can make sure that  $\beta_2, \beta_3, \beta_4, \beta_5$  and  $\beta_6$  are not simultaneously equal to zero, 99 times out of 100

Model 2

-  $F_{\text{cal}} = \frac{0.0723 / 5}{(1-0.0723) / 2719} = 42.3809$

-  $F_{\text{upper}, \alpha}(5, 2719) = 2.64$  when  $\alpha = 0.01$



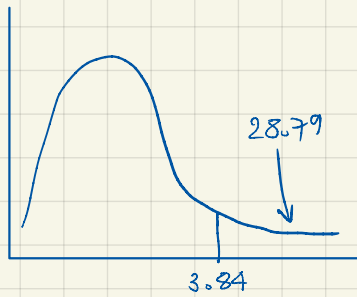
∴  $F_{\text{cal}} > F_{\text{upper}}(5, 2719)$   
we can reject  $H_0$ , in other word, we can make sure that  $\beta_2, \beta_3, \beta_4, \beta_5$  and  $\beta_6$  are not simultaneously equal to zero, 99 times out of 100

① Use F test for marginal contribution of these two variables add in model 2

- Let  $H_0$ : ethnic background and legal income has no marginal contribution to the model  
 $H_1$ : otherwise

$$- F_{cal} = \frac{R^2_{new} - R^2_{old} / m}{1 - R^2_{new} / (n - k_{new})} = \frac{(.0428 - .0723) / 3}{(1 - .0723) / (2725 - 8)} = 28.79$$

$$- F_{upper, \alpha(3, 2716)} = 2.6 \quad \text{when } \alpha = 0.05$$



$$\therefore F_{cal} > F_{upper}$$

We can reject  $H_0$ , in other words, we can make sure two variables added have marginal contribution to the model.

2. (a) - For  $\beta_1$   $H_0: \beta_1 = 0$  ,  $H_1: \beta_1 \neq 0$   
 For  $\beta_2$   $H_0: \beta_2 = 0$  ,  $H_1: \beta_2 \neq 0$   
 For  $\beta_3$   $H_0: \beta_3 = 0$  ,  $H_1: \beta_3 \neq 0$   
 For  $\beta_4$   $H_0: \beta_4 = 0$  ,  $H_1: \beta_4 \neq 0$

$$- t_{cal}(\beta_1) = \frac{9.1748 - 0}{0.0035} = 2,621.3714 \rightarrow \text{Reject } H_0$$

$$t_{cal}(\beta_2) = \frac{0.587 - 0}{0.0072} = 81.5278 \rightarrow \text{Reject } H_0$$

$$t_{cal}(\beta_3) = \frac{-0.0336 - 0}{0.005} = -6.72 \rightarrow \text{Reject } H_0$$

$$t_{cal}(\beta_4) = \frac{0.0444 - 0}{0.0102} = 4.3529 \rightarrow \text{Reject } H_0$$

$$- t_{\frac{\alpha}{2}, 0.025} = \pm 1.960 \quad \text{when } n-k = 97878 - 4 = 97,874$$

$\therefore$  we can reject  $H_0$  for all test. In other word, we can make sure that 95% of all of parameter are significantly different from zero.

(b) If we consider effect of civil servant separately, The coefficient  $\beta_2$  that represent difference between civil servants and other groups. As a result, the civil servants earned more than other group by  $\times(e^{\beta_2} - 1) = 79.86\%$

(c) The pandemic affect the overall wage to drops by  $100 \times (e^{\beta_3} - 1) = 3.3$  percent for all groups

(d) The relationship between civil servant variable and year is positive and different from zero. Therefore, if we consider only year 2020 the result is

$$\ln \widehat{\text{wage}} = 9.1748 + 0.587(1) - 0.0336(1) + 0.0444(1) \cdot (1) \quad \text{while other groups are}$$

$$\ln \widehat{\text{wage}} = 9.1748 + 0.587(0) - 0.0336(1) + 0$$

$\therefore$  In 2019 civil servant wage will decrease by 0.0336, while in 2020 their wage will increase +0.0444

$\therefore$  In summary, The control group is still better-off during pandemic by  $100 \times (e^{\beta_3 + \beta_4} - 1) = 1.09\%$  increase, while other group will worse off by  $100 \times (e^{\beta_3} - 1) = 3.3\%$  decrease

$\rightarrow$  This result is make sense in economic reason because the control group' wage didn't drop while the rest may earn less during pandemic.

3. (a) There is no evidence of multicollinearity in the data because in the multicollinearity their should have correlation between each variable with coefficient exceeding 0.8. Moreover, according to the VIF and TOL, the multicollinearity model should have VIF not exceed 10 and TOL not closer to 1.

$$|r| < 0.8, \text{ VIF} < 10, \text{ TOL closer to 1}$$

→ Set up  $H_0: \beta_k = 0$   
 $H_1: \beta_k \neq 0$  when  $k = 1, 2, 3, 4$

$$t_{cal}(\beta_1) = \frac{\hat{\beta}_1 - \beta_1}{\text{se}(\hat{\beta}_1)} = \frac{-34.1349 - 0}{15.6763} = -2.18 \rightarrow \text{Reject } H_0$$

$$t_{cal}(\beta_2) = \frac{\hat{\beta}_2 - \beta_2}{\text{se}(\hat{\beta}_2)} = \frac{1.5386 - 0}{3.0005} = 0.51 \rightarrow \text{Reject } H_0$$

$$t_{cal}(\beta_3) = \frac{\hat{\beta}_3 - \beta_3}{\text{se}(\hat{\beta}_3)} = \frac{3.9152 - 0}{1.1597} = 3.4 \rightarrow \text{Reject } H_0$$

$$t_{cal}(\beta_4) = \frac{\hat{\beta}_4 - \beta_4}{\text{se}(\hat{\beta}_4)} = \frac{18.8025 - 0}{8.3425} = 2.25 \rightarrow \text{Reject } H_0$$

→ critical value =  $\pm 2.056$  when  $\alpha = 0.05$ ,  $(n-k) = 26$

∴ We can sure that  $R^2$  is 0.6552 and almost all parameters are significantly different from 0. So we can conclude that the conflicting test is not found here and multicollinearity also not present here

(b) Property of BLUE are linear, unbiased, and have the least variance among the class of all linear and unbiased estimators

And the OLS estimator is retain the property of BLUE, because BLUE is not affected by multicollinearity.

4. (a) - Intercept of this coefficient is 1.0108 which mean when the unemployment rate is 0 the inflation rate will be 1.0108 percent.
- Slope of this coefficient is .5055 which mean when unemployment rate increase by 1 percent the inflation rate will increase .5055 percent.

(b) - White's test

- Let  $H_0$ : Homoscedasticity
- $H_1$ : otherwise

- $LM_{cal} = n \cdot R^2_{\hat{u}_i} \sim \chi^2_{K-1} = 1.0266$

- critical value  $\chi^2_{\alpha}$  and  $\alpha = 0.05$  is 3.84146

$\therefore LM_{cal} < \chi^2_{\alpha}$ , so we cannot reject  $H_0$  of homoscedasticity

(c) Since we cannot reject  $H_0$  in (4.b), therefore, we can make sure that BLUE property is not violated