

Exercise 2 c: Show that in the competitive equilibrium, the period-0 price of period-2 goods is $1/R$

Answer:

Consumers buy x units at price p		
$t=0$	$t=1$	$t=2$
Invest $1-px$		Get x

If patient		$R(1-px)+x$
If impatient	liquidate $(1-px)$	
	Sell claims x at price $1/R$	
	(period-1 price of period-2 goods)	

Expected utility is therefore:

$$tu(1-px + x/R) + (1-t) u(R(1-px)+x) = t u(1+ x (1/R - p)) + (1-t) u(R+x(1-Rp))$$

market clearing price : $p = 1/R$ identical under autarky (hence, no trade)