

Homework 3

Example 2.1: A monopolist firm faces the market demand given by $P = 10 - Q$. Consider the following questions if the cost function $C(Q) = 4Q$.

↪ TC

$P(Q)$

- What is the revenue-maximizing level of output?

revenue function

$$TR(Q) = P(Q) \times Q$$

$$= (10 - Q) \times Q$$

$$= 10Q - Q^2$$

At $Q = 5$, TR is max

$TR = 25$

slope = $\frac{dTR}{dQ} = 10 - 2Q$

maximum occurs

when $\frac{dTR}{dQ} = 0$

$$10 - 2Q = 0$$

$$Q = 5$$

- What is the break-even output? → Find point $\pi = 0 \rightarrow TR = TC$

HW.

$$TC = 4Q \times Q$$

$$TR = TC$$

$$10Q - Q^2 = 4Q \times Q$$

$$10Q - Q^2 = 4Q^2$$

$$10Q = 5Q^2$$

$$2 = \frac{Q^2}{Q}$$

$$2 = Q$$

HW.

- What is the profit-maximizing level of output?

① $MR = MC$

$$MC = \frac{\Delta TC}{\Delta Q} = 4$$

② $\pi = TR - TC$

$$\pi = 10Q - Q^2 - 4Q^2$$

$$= 10Q - 5Q^2$$

$$\frac{d\pi}{dQ} = 10 - 10Q$$

$$10 - 10Q = 0$$

$$10 = 10Q$$

$$Q = 1$$

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