

Oct 29, 2019. ①

Today

1. Review U-max problem w/ SE. & IE.

2. Applications :

- Giffen good

- Subsidy

- Vouchers

- Work-leisure

- Intertemporal Consumption

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Consumer U-max problem

Given 2 goods: X & Y , Prices: P_x & P_y

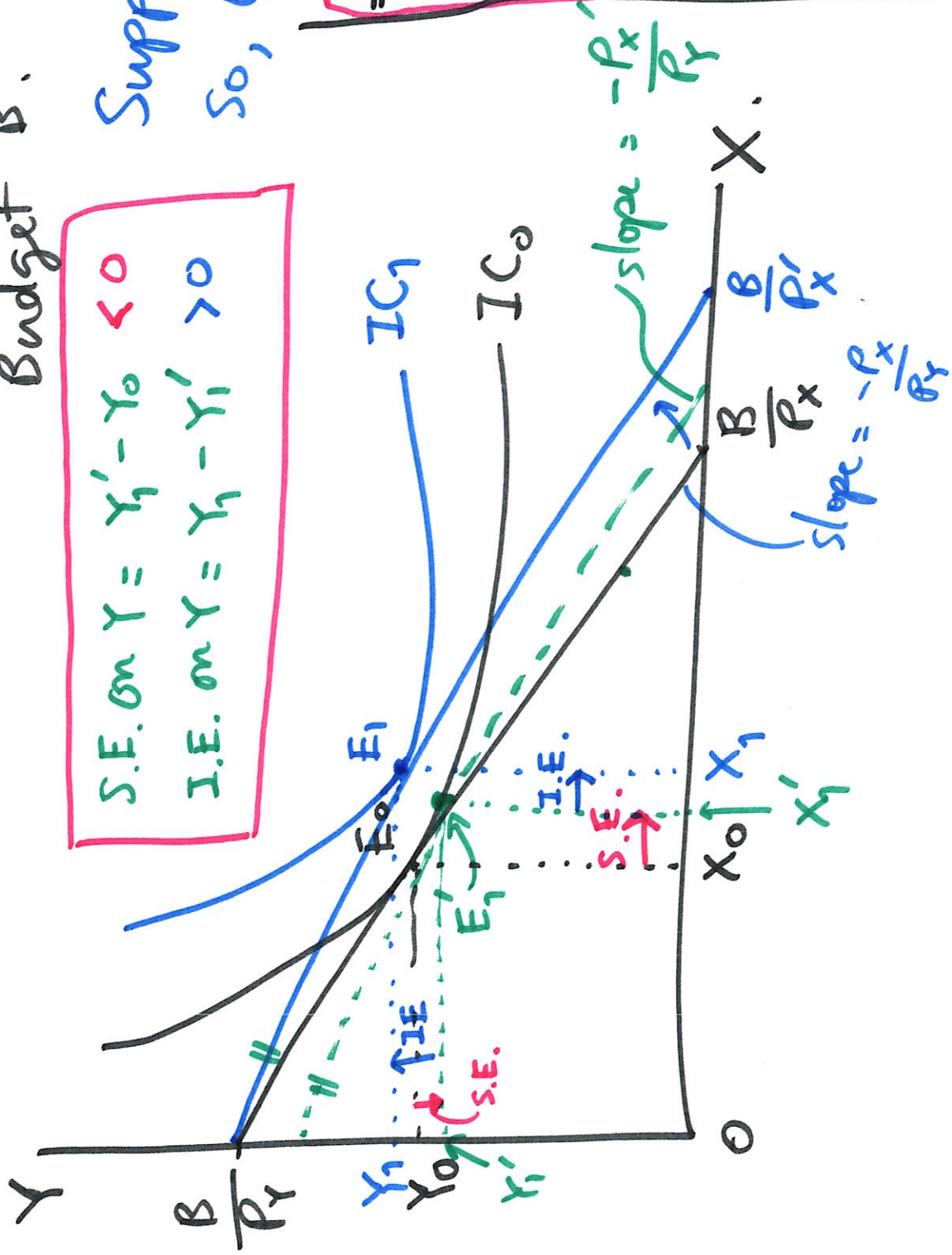
Budget B .

S.E. on $Y = Y_1 - Y_0 < 0$
 I.E. on $Y = Y_1 - Y_0 > 0$

decreases.

Suppose P_x ~~increases~~

So, $P_x' < P_x$



⇒ Substitution effect on X

$$= X_1' - X_0 > 0$$

⇒ Income effect on X

$$= X_1 - X_1' > 0$$

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Steps

1. Start with the original BL Δ IC. Call the optimal point $E_0 (X_0, Y_0)$.
2. Determine the impact of the change (say $P_x \downarrow$) on the BL.
3. Identify the new optimal point. Call $E_1 (X_1, Y_1)$.
4. Draw a hypothetical BL that has the same slope as the new BL. (i.e. slope = $-\frac{P_x'}{P_y}$).
Call the tangency $E_1' (X_1', Y_1')$ with the original IC.
5. S.E. on X = $X_1' - X_0$; IE on X = $X_1 - X_1'$

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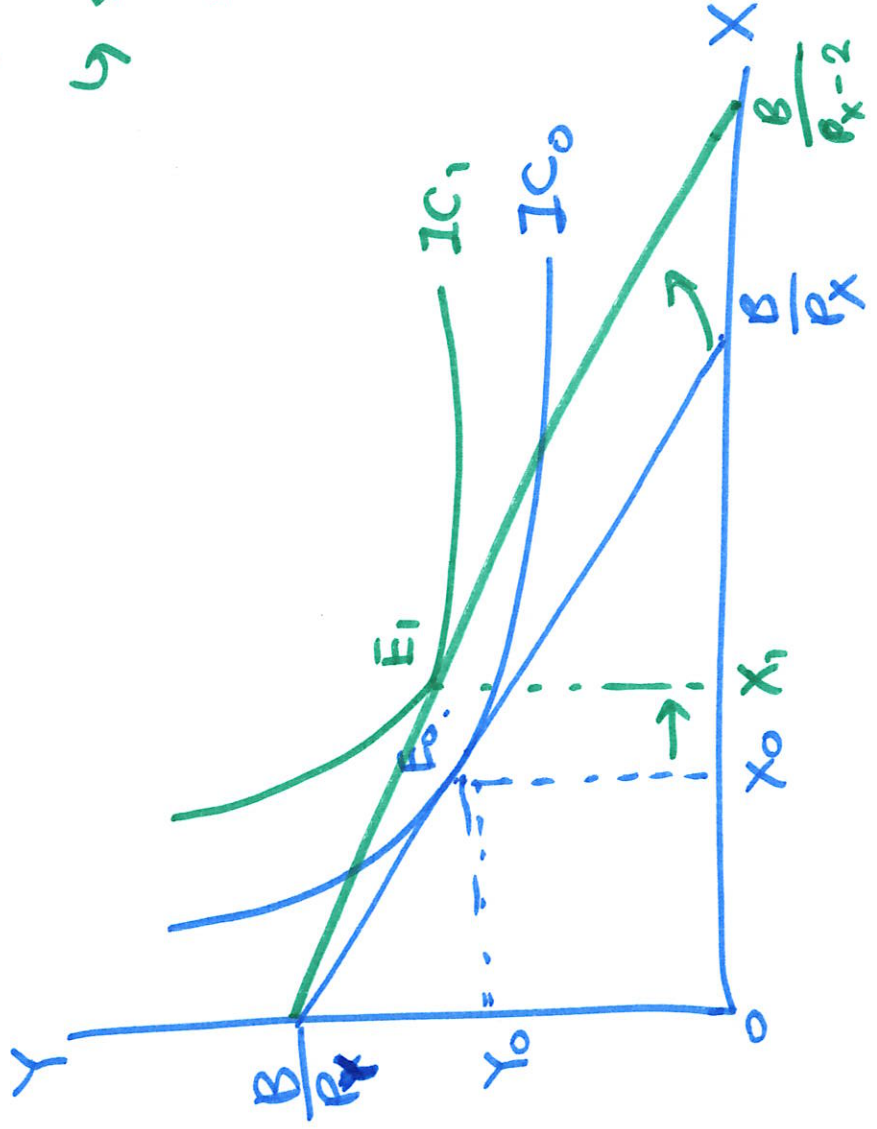
Application : Subsidy.

Suppose the gov't gives a \$2 per-unit subsidy for good X. Everything else constant.

$$P'_x = P_x - 2.$$

↳ same effect as a reduction in P_x .

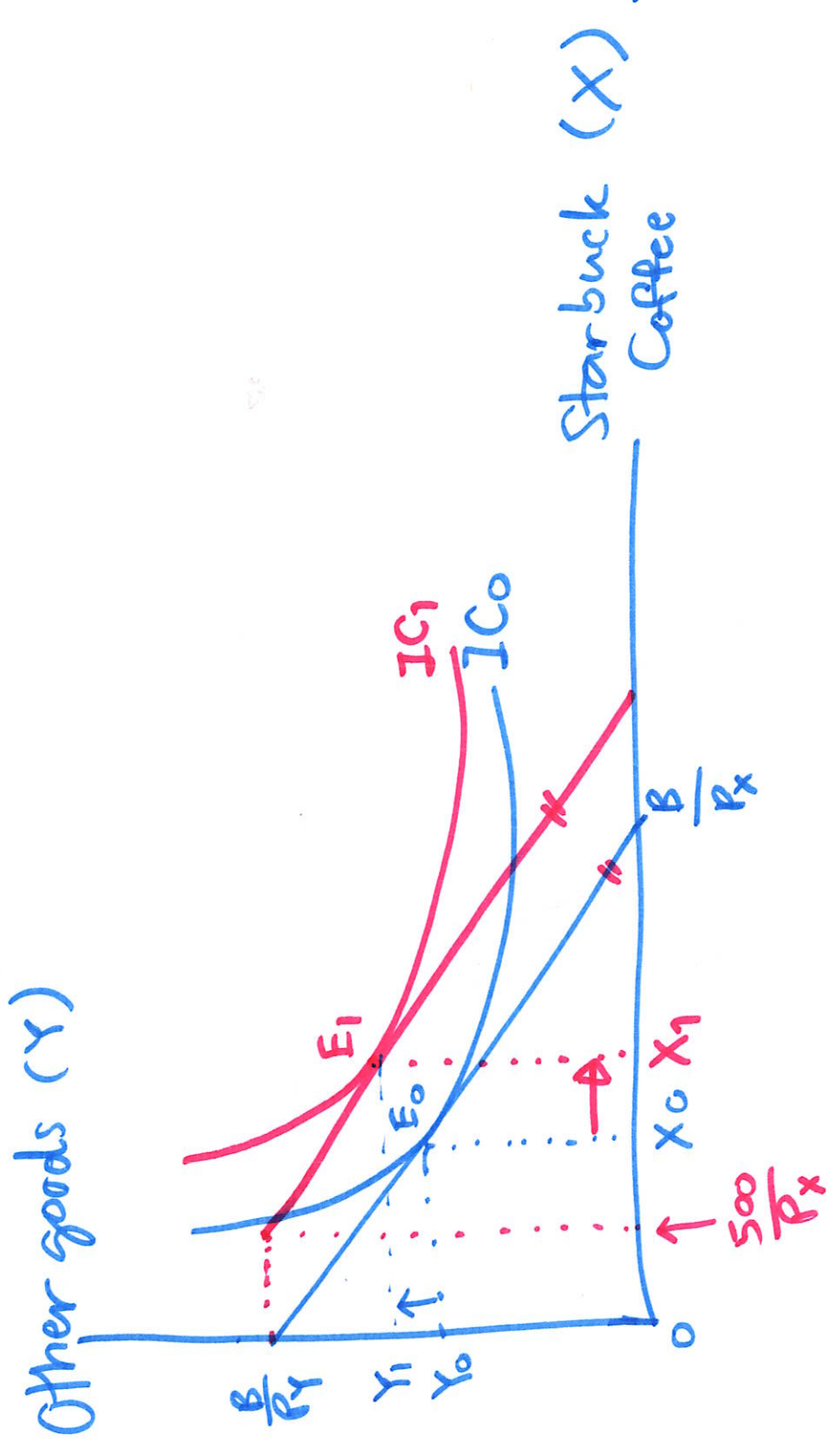
⇒ X^* increases but Impact on Y is arbitrary.



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Application : Voucher

Suppose you receive \$ 500 starbuck coupon; everything else constant.



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Application: Work - leisure Analysis

Consumer's utility depends on consumption of all goods (C) and leisure (L). Constraint is time.

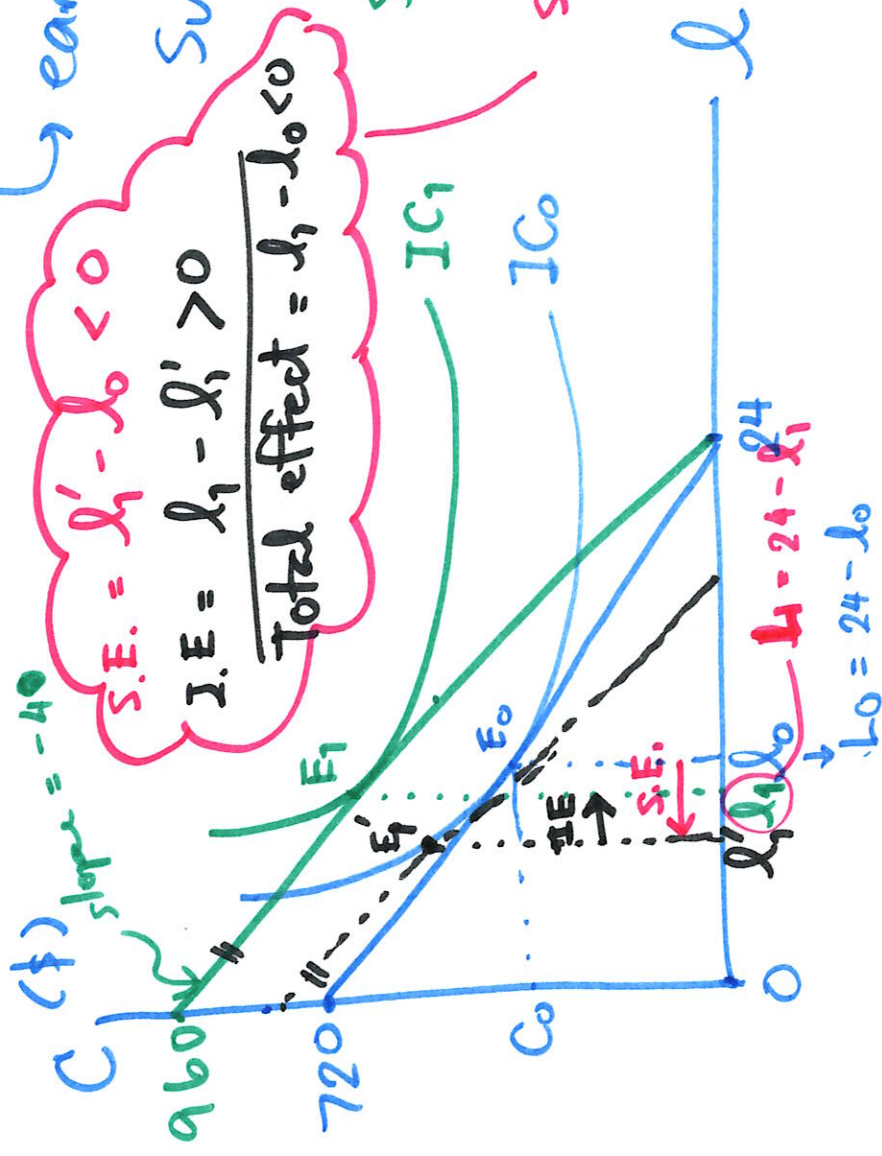
↳ Leisure: $L = 24 - L_1$, where $L =$ labor (working hours), L_1 = labor (working hours)

↳ earn wage (w) per hour.

Suppose $w = \$30/\text{hour}$
↳ $\max C = \$30 \times 24 = \720

Suppose $w' = \$40/\text{hour}$
↳ $\max C = \$960$

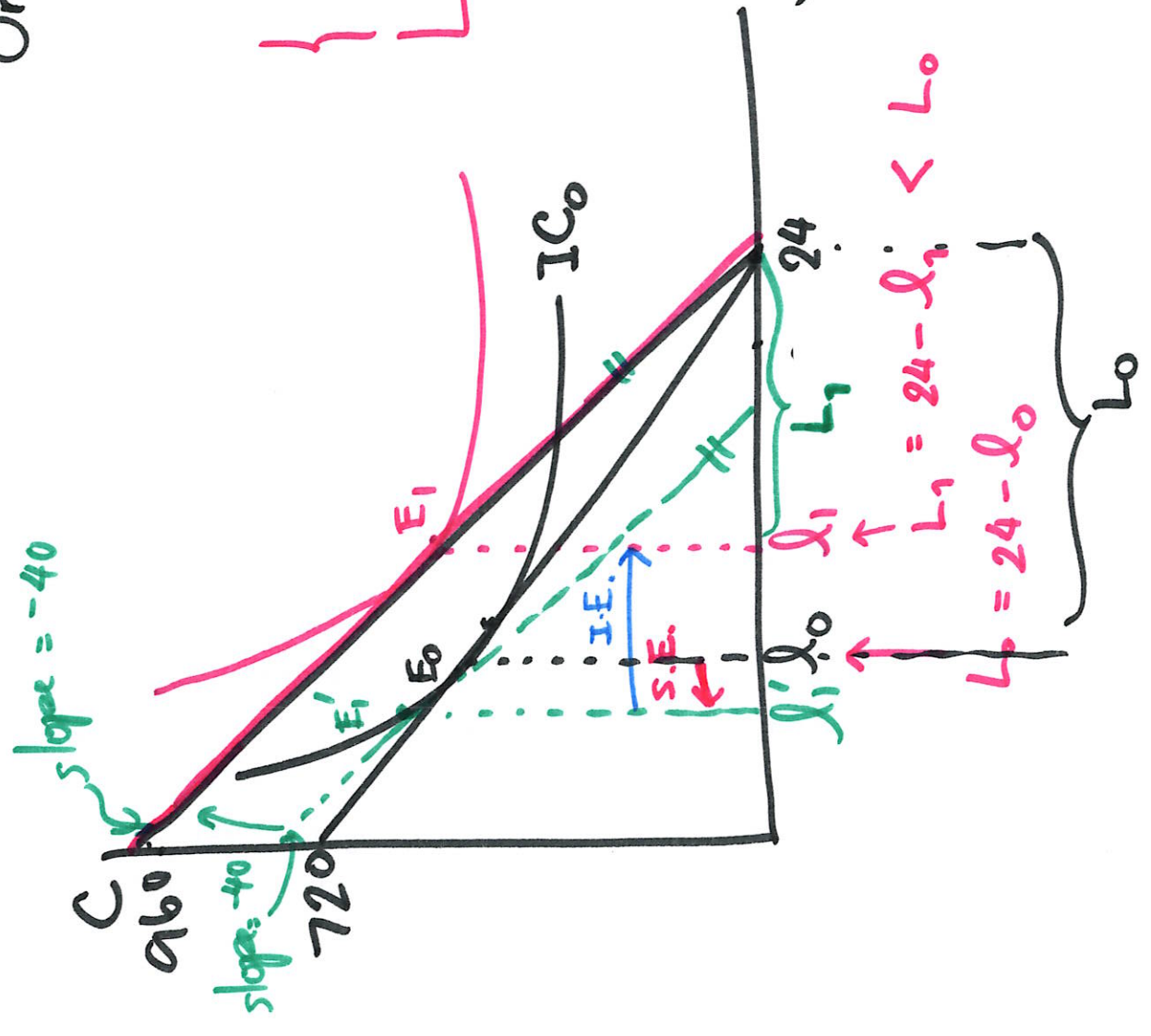
S.E. > I.E. → less leisure → more labor. ($L_1 > L_0$)



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Work - Leisure when $I.E. > S.E.$

Original $w = \$30 / \text{hour}$
 New $w' = \$40 / \text{hour}$



$S.E. \text{ on } l = l_1' - l_0 < 0$
 $I.E. \text{ on } l = l_1 - l_1' > 0$
 $|l_1 - l_1'| > |l_1' - l_0|$
 I.E. > S.E.



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Application: Intertemporal consumption

Let C_0 = consumption when young } Live for 2 periods
when old.

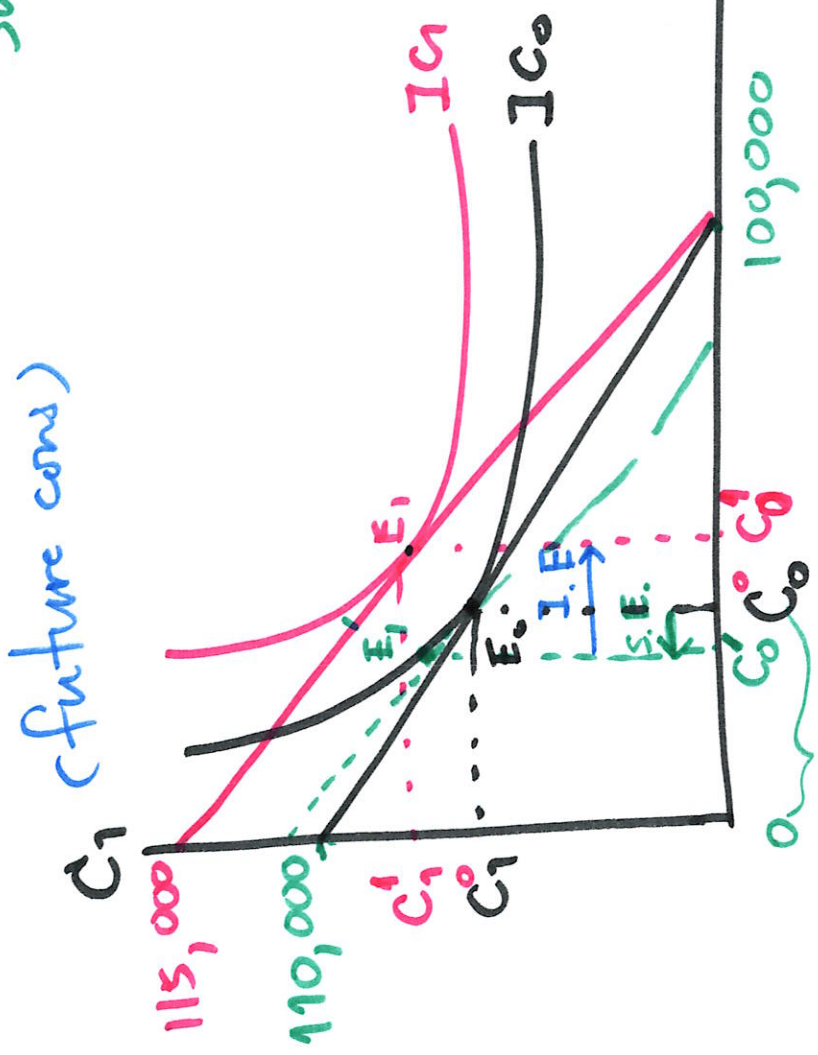
Let interest rate = r %. (saving rate), say $r = 10\%$.

Suppose $C_0 = 100,000$

$$C_1 = C_0 + (r \cdot C_0) \\ = (1 + r\%) C_0$$

Suppose $r \uparrow$ to $r' = 15\%$.

\Rightarrow S.E. on $C_0 = C_0' - C_0 < 0$
 \Rightarrow I.E. on $C_0 = C_0' - C_0' > 0$.
Total effect = $C_0' - C_0$ (current cons).



Practice: What if $S.E. > I.E.$?