



B.E. International Program
Faculty of Economics
Thammasat University



EE311 Microeconomics Theory, Semester 2/2019

Homework Assignment #8 | Due date: Monday 27 April 2020
(in-class submission, before lecture begins!)

Instruction:

- 1) Attempt all questions.
- 2) You may study and discuss in group but you have to write up your solutions independently and by handwriting only. Copying and/or Plagiarism is considered as a serious crime in academic arena and it will not be tolerated. If detected, all parties involved receive 'zero.'
- 3) If you have any questions, please feel free to email me at pongpalin@econ.tu.ac.th

Oligopoly (CH 13)

8. A homogeneous products duopoly faces a market demand function given by $P = 300 - 3Q$, where $Q = Q_1 + Q_2$. Both firms have a constant marginal cost $MC = 100$.
- a) What is Firm 1's profit-maximizing quantity, given that Firm 2 produces an output of 50 units per year? What is Firm 1's profit-maximizing quantity when Firm 2 produces 20 units per year?
 - b) Derive the equation of each firm's reaction curve and then graph these curves.
 - c) What is the Cournot equilibrium quantity per firm and price in this market?
 - d) What would the price in this market be if it were perfectly competitive?
 - e) What would the equilibrium price in this market be if the two firms colluded to set the monopoly price?
 - f) What is the Bertrand equilibrium price in this market?
(Hint: This is the case of Bertrand Duopoly with Homogeneous Product.)
 - g) What are the Cournot equilibrium quantities and industry price when one firm has a marginal cost of 100 but the other firm has a marginal cost of 90?

h) Assuming that Firm 1 is the Stackelberg leader, find the Stackelberg equilibrium quantities for each firm and the market price.

18. Suppose that the industry consists of a dominant firm, Braeutigam Cobalt (BC), which has a constant marginal cost equal to \$40 per unit. The market demand for cobalt is given by $Q = 200 - P$. There are 9 fringe producers, each of whom has a marginal cost curve $MC = 40 + 10q$, where q is the output of a typical fringe producer. Assume there are no fixed costs for any producer.

- What is the supply curve of the competitive fringe?
- What is BC's residual demand curve?
- Find BC's profit-maximizing output and price. What is BC's market share?
(Hint: Market Share of a firm = (Q of the firm) / (Total Q in the market).)

24. RyanAir and EasyJet both fly between London and Marrakech. Their demand curves for EasyJet and RyanAir are given, respectively, by $Q_E = 500 - 2P_E + P_R$ and $Q_R = 500 - 2P_R + P_E$. Q_E and Q_R stand for the number of passengers per day for EasyJet and RyanAir, respectively. The marginal cost of each carrier is £10 per passenger.

- If EasyJet sets a price of £100, what is the equation of RyanAir's demand curve and marginal revenue curve? What is RyanAir's profit-maximizing price when Easyjet sets a price of £100?
- Derive the equations for EasyJet's and RyanAir's price reaction curves.
- What is the Bertrand equilibrium in this market?

Monopsony (CH 10)

26. A coal mine operates with a production function $Q = L/2$, where L is the quantity of labor it employs and Q is total output. The firm is a price taker in the output market, where the price is currently 32. The firm is a monopsonist in the labor market, where the supply (AFC) curve for labor is $w = 4L$.

- What is the monopsonist's MFC?
- Calculate the monopsonist's optimal quantity of labor. What wage rate must the monopsonist pay to attract this quantity of labor?
- What would be the w^* and L^* if the factor market were competitive?

$$8a. P = 300 - 3Q_1 - 3Q_2 \quad Q_2 = 50$$

$$P = 300 - 3Q_1 - 3(50) \therefore P = 150 - 3Q_1$$

$$MR = MC \quad \therefore 150 - 6Q_1 = 100$$

$$Q_1 = 8.33$$

$$Q_2 = 20, P = 240 - 3Q_1, MR = MC$$

$$240 - 6Q_1 = 100$$

$$Q_1 = 23.33$$

$$b. \text{ Firm 1 } P = (300 - 3Q_2) - 3Q_1$$

$$MR = MC$$

$$(300 - 3Q_2) - 6Q_1 = 100 \therefore Q_1 = 33.33 - 0.5Q_2$$



$$c. Q_1 = Q_2$$

$$Q_2 = 33.33 - 0.5Q_2$$

$$Q_2 = 22.22$$

$$P = 300 - 3(44.44) = 166.67$$

d. Perfectly competitive: $P = MC = 100$

e. Monopoly price: $300 - 6Q = 100$

$$Q = 33.33$$

$$P = 300 - 3 \left(\frac{200}{6} \right) = 200$$

f. Bertrand oligopolists, $P = 100$

g. Firm 1 $MC = 100$ $P = (300 - 3Q_2) - 3Q_1$
Firm 2 $MC = 90$ $P = (300 - 3Q_1) - 3Q_2$

Firm 1 $MR = MC$:

$$(300 - 3Q_2) - 6Q_1 = 100$$

$$Q_1 = 33.33 - 0.5Q_2$$

Firm 2 $MR = MC$:

$$(300 - 3Q_1) - 6Q_2 = 90$$

$$Q_2 = 35 - 0.5Q_1$$

$$Q_1 = 21.11 \quad Q_2 = 24.44 \quad \therefore P = 63.36$$

h. Firm 1 leads \therefore Firm 2 $Q_2 = 33.33 - 0.5Q_1$
Firm 1 then $MC = MR$

$$TR_1 = PQ_1 = (300 - 3Q_1 - 100 + 1.5Q_1)Q_1 \\ = (200 - 1.5Q_1)Q_1$$

$$MR_1 = 200 - 3Q_1$$

$$MR_1 = MC: 200 - 3Q_1 = 100$$

$$Q_1 = 33.33$$

$$Q_2 = 33.33 - 0.5(33.33) = 0.5(33.33)$$

$$18a. MC = 40 + 10q \quad q = 0.1p - 4$$

$$S_f = \begin{cases} 0 & p \leq 40 \\ 0.9p - 36 & p > 40 \end{cases}$$

b. Residual demand:

$$Q_R = \begin{cases} 200 - p & p \leq 40 \\ 236 - 1.9p & p > 40 \end{cases}$$

c. Residual demand curve: $p = \left(\frac{10}{19}\right) (236 - Q_R)$

$$MR = \left(\frac{10}{19}\right) (236 - 2Q_R)$$

$$MR = MC$$

$$MR = 40$$

$$\left(\frac{10}{19}\right) (236 - 2Q_R) = 40$$

$$Q_R = 80$$

$$p = \left(\frac{10}{19}\right) (236 - 80)$$

$$p = 82.11$$

$$Q = 200 - 82.11 = 117.89$$

$$\text{Market share: } \frac{80}{117.89} = 0.68 = 68\%$$

$$29c. \quad P_{\text{EasyJet}} = 100$$

$$Q_R = 500 - 2P_R + 100$$

$$P_R = 300 - 0.5Q_R$$

$$MR = MC$$

$$MR_R: 300 - Q_R$$

$$300 - Q_R = 10$$

$$Q_R = 290$$

$$P_R = 155$$

$$b. \quad MR_E = MC_E = 10$$

$$Q_E = 500 - 2P_E + P_R$$

$$P_E = 250 - 0.5Q_E + 0.5P_R$$

$$TR_E = P_E Q_E = (250 - 0.5Q_E + 0.5P_R) Q_E$$

$$MR_E = 250 - Q_E + 0.5P_R$$

$$MR_E = MC_E = 10$$

$$250 - Q_E + 0.5P_R = 10$$

$$Q_E = 240 + 0.5P_R$$

$$Q_E = 500 - 2P_E + P_R$$

$$500 - 2P_E + P_R = 240 + 0.5P_R$$

$$260 + 0.5P_R = 2P_E$$

$$BR_E: P_E = (130 + 0.25P_R)$$

$$BR_R: P_R = 130 + 0.25P_f$$

c. Bertrand equilibrium:

$$P_f = 130 + 0.25(130 + 0.25P_f)$$

$$P_f = P_R = 175.71$$

26a. Monopsonist:

$$ME_L = w + L \frac{\Delta w}{\Delta L}$$

$$ME_L = 4L + L(4)$$

$$ME_L = 8L$$

b. Profit max Monopsonist: $MRP_L = ME_L$, $MRP_L = P \frac{\Delta Q}{\Delta L}$

$$\frac{\Delta Q}{\Delta L} = 0.5 \therefore MRP_L = 0.5P$$

$$P = 32, MRP_L = 16 \therefore 16 = 8L \therefore L = 2$$

$$Q \text{ Labour} = w = 4L = 8$$

c. Competitive labour market: $w = MPP_L$

Supply of Labour: $L = 4$

$$w = 4L = 16$$

