

Assignment #2

Instructions:

- For all questions, answer up to 4 decimal places.
 - This assignment is due on **Thursday, May 20, 2021 before 23.59.**
 - Write your answer in either digital or ordinary paper. For digital paper, export pages into a single PDF file. For ordinary paper, take photos of your writing and convert them into a single PDF file as well.
 - There is no need to rewrite the question. Assign number item, i.e. 1 a., clearly before your answer is sufficient.
 - Submit your assignment into Moodle.
 - Name your file as StudentID_Nickname (in Thai) such as 123456789_น้อย. **Please follow this instruction strictly since it will help me a lot with file management.**
-

Question 1. The data set CEOSAL1.DTA contains information on 209 CEOs for the year 1990; these data were obtained from Business Week (5/6/1991). To study effect of firm performances and types of industry where CEOs work on CEO compensation, the CEO salary regression is proposed as follows:

$$\log(\text{salary}_i) = \beta_0 + \beta_1 \log(\text{sales}_i) + \beta_2 \text{ROE}_i + \beta_3 \text{finance}_i + \beta_4 \text{consprod}_i + \beta_5 \text{utility}_i + u_i$$

where

- $\log(\text{salary}_i)$ = logarithm of CEO annual salary (in 1,000 USD)
- $\log(\text{sales}_i)$ = logarithm of firms' sale (in 1 million USD)
- ROE_i = average return on equity for the CEO's firm for the previous three years (Return on equity is defined in terms of net income as a percentage of common equity)
- finance_i = 1 if in financial industry, = 0 otherwise
- consprod_i = 1 if in consumer product industry, = 0 otherwise
- utility_i = 1 if in utility industry, = 0 otherwise

(finance_i , consprod_i , and utility_i are binary variables indicating the financial, consumer products, and utilities industries. The omitted industry is transportation.

Using STATA, the estimation result is shown below. Answer the following questions.

Source	SS	df	MS	Number of obs = 209		
Model	23.8109943	5	4.76219887	F(5, 203)	=	22.53
Residual	42.9111689	203	.211385068	Prob > F	=	0.0000
Total	66.7221632	208	.320779631	R-squared	=	0.3569
				Adj R-squared	=	0.3410
				Root MSE	=	.45977

lsalary	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]	
lsales	.2571917	.0320348	8.03	0.000	.0194282	.3203553
roe	.0111517	.3342996	2.59	0.010	.0026742	.0196293
finance	.1579564	.0890017	1.77	0.077	-.0175299	.3334426
consprod	.1808917	.0847683	2.13	0.034	.0137524	.3480311
utility	-.2830015	.0992337	-2.85	0.005	-.4786624	-.0873405
_cons	4.588101	.2950221	15.55	0.000	4.0064	5.169801

- Write out the estimated regression equation for $\log(\text{salary}_i)$. Interpret the estimated coefficient associated with $\log(\text{sales}_i)$.
- What is the overall significance of the regression? What test do you use? Which of the coefficients are individually statistically significant at the 5 percent level? State **the critical value** for hypothesis testing to receive full points.
- Compute the approximate percentage difference in estimated salary between the utility and transportation sector, holding sales_i and ROE_i fixed.
- Why can't we put all the sector dummies (i.e. finance_i , consprod_i , utility_i and transport_i) in the equation? What would happen if we put all the sector dummies in the equation and use STATA run the regression anyway?
- In the above model, is there any benefit if we add interaction terms between roe and sector dummies, i.e. $\text{ROE}_i * \text{finance}_i$ and/or $\text{ROE}_i * \text{consprod}_i$ and/or $\text{ROE}_i * \text{utility}_i$?

a)

$$\log(\text{salary}_i) = \beta_0 + \beta_1 \log(\text{sale}_i) + \beta_2 \text{roe}_i + \beta_3 \text{finance} + \beta_4 \text{consprod} - \beta_5 \text{utility}$$

$\beta_1 = 0.2572$ If we change sale by one percent, we'd expect salary to change by 0.2572 percent

b)

Overall significance \rightarrow f-test

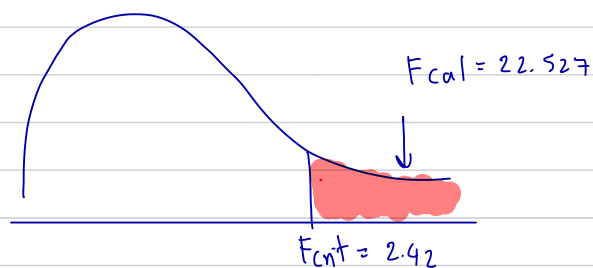
$$H_0: \beta_0 = \beta_1 = \beta_2 = \beta_3 = \beta_4 = \beta_5$$

H_1 : at least one parameter not equal 0

$$\alpha = 0.05$$

$$F_{\text{crit}} = F_{5, 203} \approx 2.42$$

$$F_{\text{cal}} = \frac{4.7622}{0.2114} = 22.527$$



$$F_{\text{cal}} > F_{\text{crit}} : 22.527 > 2.42$$

The critical F value for 5 df in the numerator and 203 df in the denominator is 2.42 at 5% level of significance. So, Reject null hypothesis. There is evidence that not all parameter is equal to zero.

individually

T-test : $\log(\text{sale})$

$$H_0 : \beta_1 = 0$$

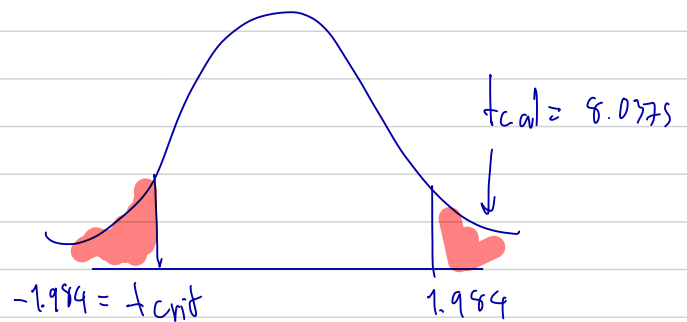
$$H_1 : \beta_1 \neq 0$$

$$\alpha = 0.05$$

$$\begin{aligned} df &= n - k \\ &= 209 - 6 \\ &= 203 \end{aligned}$$

$$t_{\text{crit}} : t_{0.025, 203} = 1.984$$

$$\begin{aligned} t_{\text{cal}} &= \frac{\hat{\beta}_1 - \beta_1}{\text{se}_{\hat{\beta}_1}} = \frac{0.2572}{0.032} \\ &= 8.0375 \end{aligned}$$



$$\therefore |t_{\text{cal}}| > |t_{\text{crit}}| : |8.0375| > |1.984|$$

So, reject null hypothesis that enough evidence to said that logarithm firms'sale significant affect on logarithm of CEO annual salary at 5 percent level.

t-test : ROE

$$H_0 : \beta_1 = 0$$

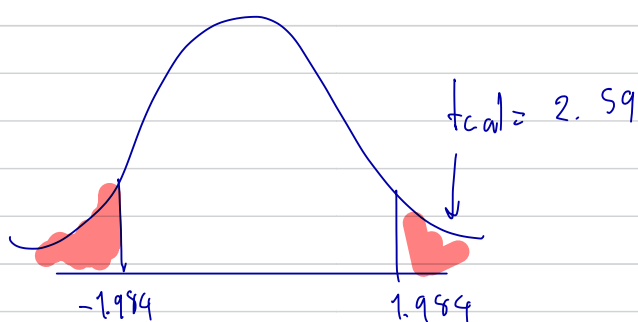
$$H_1 : \beta_2 \neq 0$$

$$\alpha = 0.05$$

$$df = 203$$

$$t_{crit} = 1.984$$

$$t_{cal} = \frac{\hat{\beta}_2 - \beta_2}{se_{\hat{\beta}_2}}$$
$$= 2.59$$



$$|t_{cal}| > |t_{crit}| : |2.59| > |1.984|$$

So, reject null hypothesis that enough evidence to said that average ROE for the CEO's firm the previous three years significant affect on logarithm of CEO annual salary at 5 percent level.

t-test : finance

$$H_0 : \beta_3 = 0$$

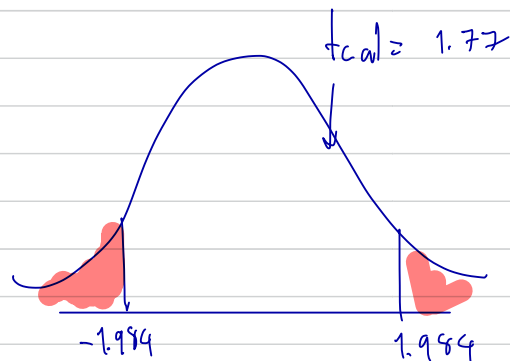
$$H_1 : \beta_3 \neq 0$$

$$\alpha = 0.05$$

$$df = 203$$

$$t_{crit} = 1.984$$

$$\begin{aligned} t_{cal} &= \frac{\hat{\beta}_3 - \beta_3}{se_{\hat{\beta}_3}} \\ &= \frac{0.158}{0.089} \\ &= 1.7753 \end{aligned}$$



$$|t_{cal}| < |t_{crit}| : |1.7753| < |1.984|$$

So, fail to reject null hypothesis that enough evidence to said working in financial industry has no significant affect on $\log(\text{salary})$ at the 5 percent level.

t-test : consprod

$$H_0: \beta_4 = 0$$

$$H_1: \beta_4 \neq 0$$

$$\alpha = 0.05$$

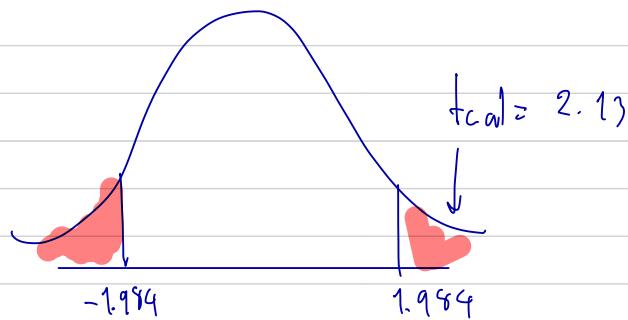
$$df = 203$$

$$t_{crit} = 1.984$$

$$t_{cal} = \frac{\hat{\beta}_4 - \beta_4}{se_{\hat{\beta}_4}}$$

$$= \frac{0.1509}{0.0546}$$

$$= 2.13$$



$$|t_{cal}| > |t_{crit}| : |2.13| > |1.984|$$

So, reject null hypothesis that enough evidence to said work in consumer product industry significant affect on log (salary) at 5 percent level

t-test : utility

$$H_0 : \beta_5 = 0$$

$$H_1 : \beta_5 \neq 0$$

$$\alpha = 0.05$$

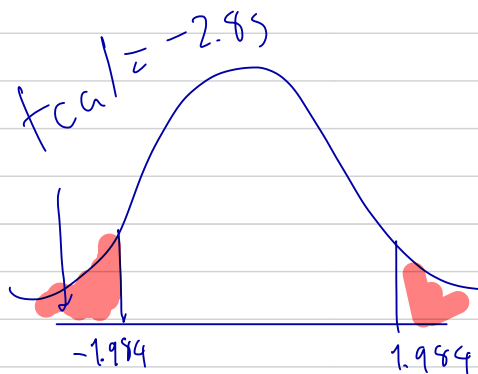
$$df = 203$$

$$t_{crit} = 1.984$$

$$t_{cal} = \frac{\hat{\beta}_5 - \beta_5}{SE_{\hat{\beta}_5}}$$

$$= \frac{-0.283}{0.0992}$$

$$= -2.85$$



$$|t_{cal}| > |t_{crit}| : |-2.85| > |1.984|$$

∴, reject null hypothesis that enough evidence to said working in utility industry significant affect on $\log(\text{salary})$ at 5 percent level.

(.)

salary in transport industry \Rightarrow finance, consprod, and utility = 0

$$\therefore \log(\text{salary}) = 4.5881 + 0.2572 \log(\text{sales}) + 0.0112 \text{roe}$$

salary in Utility industry \Rightarrow utility = 1, finance and consprod = 0

$$\therefore \log(\text{salary}) = 4.5881 + 0.2572 \log(\text{sales}) + 0.0112 \text{roe} - 0.283 \quad (1)$$

$$= 4.3051 + 0.2572 \log(\text{sales}) + 0.0112 \text{roe}$$

∴. Salary in transport industry more than 0.283% to utility industry

d) we can't put all section dummies example finance, consprod, utility and transport in the equation because it will make the curse become perfect collinearity

If we were to run the program using stata, the computer would be unable to run it. When you have dummy variable for each category or group and also an intercept, you will have a case of perfect collinearity.

e). We need to check Dummy variable which interaction relationship each others or not

Question 2. Birth weight has been used by officials as one of the main determinants of health. Data set BWGHT.DTA contains data on infant birth weights in ounces ($bwght_i$), average number of cigarettes mother smoked per day during pregnancy ($cigs$), family income ($faminc_i$), father's year of education ($fatheduc_i$), and mother's year of education ($motheduc_i$). The following two regressions were estimated using data on $n = 1191$ births:

Model 2.1: $bwght_i = \beta_0 + \beta_1cigs_i + \beta_2faminc_i + u_i$

regress bwght cigs faminc					
Source	SS	df	MS		
Model	14536.9538	2	7268.47691	Number of obs =	1191
Residual	468209.738	1188	394.115941	F(2, 1188) =	18.44
				Prob > F =	0.0000
				R-squared =	0.0301
				Adj R-squared =	0.0285
Total	482746.692	1190	405.669489	Root MSE =	19.852

bwght	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]
cigs	-.5876985	.1090181			
faminc	.0624684	.0324438			
_cons	118.5568	1.234278			

Omitted for the purpose of this exam.

Model 2.2: $bwght_i = \beta_0 + \beta_1cigs_i + \beta_2faminc_i + \beta_3fatheduc_i + \beta_4motheduc_i + u_i$

regress bwght cigs faminc fatheduc motheduc					
Source	SS	df	MS		
Model	15827.6593	4	3956.91482	Number of obs =	1191
Residual	466919.033	1186	393.69227	F(4, 1186) =	10.05
				Prob > F =	0.0000
				R-squared =	0.0328
				Adj R-squared =	0.0295
Total	482746.692	1190	405.669489	Root MSE =	19.842

bwght	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]
cigs	-.5894954	.1106172			
faminc	.0538254	.0366502			
fatheduc	.4936695	.2832896			
motheduc	-.4379234	.3197377			
_cons	118.0741	3.500291			

Omitted for the purpose of this exam.

- where $bwght_i$ = birth weight, ounces
- $cigs_i$ = average number of cigarettes the mother smoked per day while pregnant
- $faminc_i$ = 1988 family income, \$1000s
- $fatheduc_i$ = father's years of education
- $motheduc_i$ = mother's years of education

Answer the following questions.

- a. Based on **Model 2.1**, test whether smoking has an impact on birth weight. Show your work. (use $\alpha = 0.05$)
- b. Based on **Model 2.1**, construct a 99% confidence interval for β_2 .
- c. Would your conclusion in a) change if you use the result from **Model 2.2**? Show your work. (use $\alpha = 0.05$)
- d. What is the overall significance of the regression from **Model 2.2**? What test do you use? Which of the coefficients are individually statistically significant at the 5 percent level? State the critical value for hypothesis testing to receive full points.
- e. If we are interested in testing whether “**parents’ education**” has an impact on birth weight at all, what kind of null/alternative hypothesis would we be testing? Perform the test and discuss your finding. (use $\alpha = 0.05$)

a) Smoking $\Rightarrow \beta_1$ (Cigs)

$$H_0: \beta_1 = 0$$

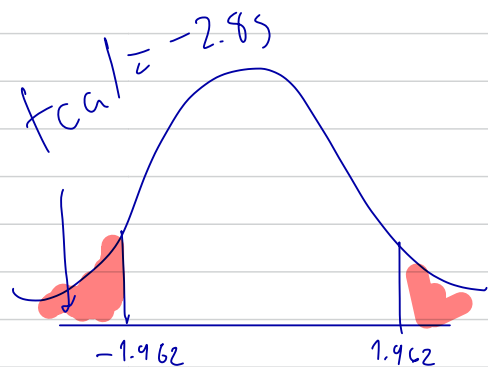
$$H_1: \beta_1 \neq 0$$

$$\alpha = 0.05$$

$$\begin{aligned} df &= n - k \\ &= 1191 - 3 \\ &= 1188 \end{aligned}$$

$$t_{crit} = 1.962$$

$$\begin{aligned} t_{cal} &= \frac{\hat{\beta}_1 - \beta_1}{SE_{\hat{\beta}_1}} \\ &= \frac{-0.5577}{0.109} \\ &= -5.117 \end{aligned}$$



$$|t_{cal}| > |t_{crit}| : |-2.85| > |1.96|$$

So, reject null hypothesis that enough evidence to say that average number of cigarettes the mother smoked per day while pregnant significantly affect on birth weight at 5 percent level

$$b) \quad \alpha = 0.01$$

$$\frac{\alpha}{2} = 0.005$$

$$df = 1148$$

$$t_{0.005, 1148} = 2.581$$

$$\hat{\beta}_2 - t_{\frac{\alpha}{2}} \text{se}(\hat{\beta}_2) \leq \beta_2 \leq \hat{\beta}_2 + t_{\frac{\alpha}{2}} \text{se}(\hat{\beta}_2)$$

$$0.0625 - (2.581)(0.0324) \leq \beta_2 \leq 0.0625 + (2.581)(0.0324)$$

$$0.0625 - 0.0836 \leq \beta_2 \leq 0.0625 + 0.0836$$

$$-0.0211 \leq \beta_2 \leq 0.1461$$

C). t-test : β_1

$$H_0 : \beta_1 = 0$$

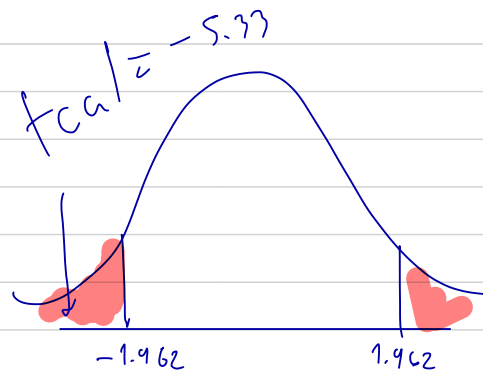
$$H_1 : \beta_1 \neq 0$$

$$\alpha = 0.05$$

$$\begin{aligned} df &= n - k \\ &= 1,191 - 5 \\ &= 1,186 \end{aligned}$$

$$t_{\text{crit}} = 1.962$$

$$\begin{aligned} t_{\text{cal}} &= \frac{\hat{\beta}_1 - \beta_1}{\text{se } \hat{\beta}_1} \\ &= \frac{-0.5595}{0.1106} \\ &= -5.33 \end{aligned}$$



$$|t_{\text{cal}}| > |t_{\text{crit}}| \quad ; \quad |-5.33| > |-1.962|$$

So, reject null hypothesis. Don't change from Model, 2.1

d). overall $\Rightarrow F$ -test

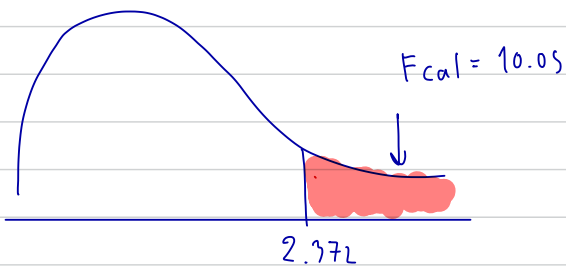
$$H_0: \beta_1 = \beta_2 = \beta_3 = \beta_4 = 0$$

H_1 : at least one parameter not equal zero

$$\alpha = 0.05$$

$$f_{\text{crit}} = f_{0.05, 4, 1196} = 2.372$$

$$f_{\text{cal}} = \frac{3956.9149}{393.6922} \\ = 10.05$$



$$f_{\text{cal}} > f_{\text{crit}} : 10.05 > 2.372$$

The critical F value for 4 df in the numerator and 1196 df in the denominator is 2.372 at 5% level of significance. So, Reject null hypothesis. There is evidence that not all parameter is equal to zero.

individually Model 2.2

T-test : cigs

$$H_0 : \beta_1 = 0$$

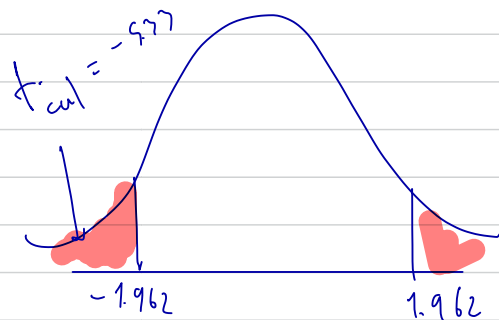
$$H_1 : \beta_1 \neq 0$$

$$\alpha = 0.05$$

$$\begin{aligned} df &= n - k \\ &= 1191 - 5 \\ &= 1186 \end{aligned}$$

$$t_{crit} : t_{0.025, 1186} = 1.962$$

$$\begin{aligned} t_{cal} &= \frac{\hat{\beta}_1 - \beta_1}{se_{\hat{\beta}_1}} = \frac{-0.5895}{0.1106} \\ &= -5.33 \end{aligned}$$



$$\therefore |t_{cal}| > |t_{crit}| : |5.0375| > |1.962|$$

So, reject null hypothesis that enough evidence to said that average number of cigarettes the mother smoked per day while pregnant affect on birth weight at 5 percent level of significant

t-test : famin

$$H_0 : \beta_2 = 0$$

$$H_1 : \beta_2 \neq 0$$

$$\alpha = 0.05$$

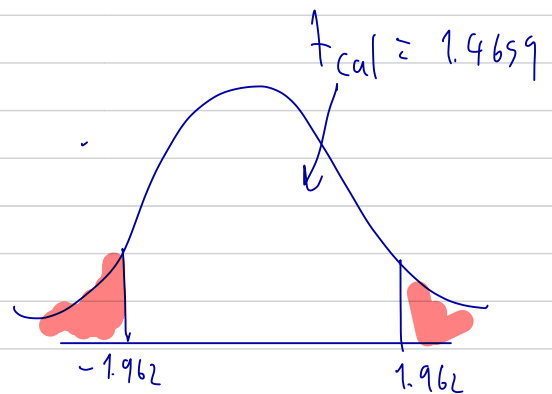
$$df = 1186$$

$$t_{crit} = 1.962$$

$$t_{cal} = \frac{\hat{\beta}_2 - \beta_2}{se_{\hat{\beta}_2}}$$

$$= \frac{0.0539}{0.0367}$$

$$= 1.4659$$



$$|t_{cal}| < |t_{crit}| : |1.4659| < |1.962|$$

So, fail to reject null hypothesis that enough evidence to said that 1984-family income has no affect on birth weight at the 5 percent level of significant.

t-test : fatheredu

$$H_0 : \beta_3 = 0$$

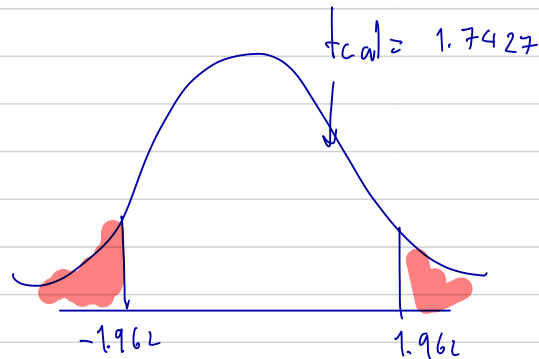
$$H_1 : \beta_3 \neq 0$$

$$\alpha = 0.05$$

$$df = 1186$$

$$t_{crit} = 1.962$$

$$\begin{aligned} t_{cal} &= \frac{\hat{\beta}_3 - \beta_3}{se_{\hat{\beta}_3}} \\ &= \frac{0.4937}{0.2833} \\ &= 1.7427 \end{aligned}$$



$$|t_{cal}| < |t_{crit}| : |1.7427| < |1.962|$$

So, fail to reject null hypothesis that enough evidence to said that father's years of education has no affect on birth weight at the 5 percent level of significant.

t-test : motheredu

$$H_0: \beta_4 = 0$$

$$H_1: \beta_4 \neq 0$$

$$\alpha = 0.05$$

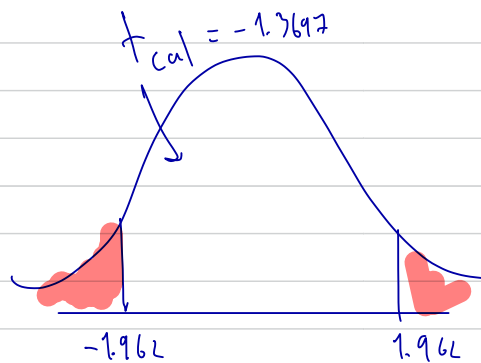
$$df = 203$$

$$t_{crit} = 1.962$$

$$t_{cal} = \frac{\hat{\beta}_4 - \beta_4}{se_{\hat{\beta}_4}}$$

$$= \frac{-0.4379}{0.3147}$$

$$= -1.3697$$



$$|t_{cal}| < |t_{crit}| : |2.13| < |1.962|$$

So, fail to reject null hypothesis that enough evidence to said that mother's years of education has no affect on birth weight at the 5 percent level of significant.

e) parents' education used model 2.2

father's year education

$$H_0: \beta_3 = 0$$

$$H_1: \beta_3 \neq 0$$

$$\alpha = 0.05$$

$$df = 1186$$

$$t_{\text{crit}} = 1.962$$

$$t_{\text{cal}} = 1.7427$$

fail null hypothesis

mother's year education

$$H_0: \beta_4 = 0$$

$$H_1: \beta_4 \neq 0$$

$$\alpha = 0.05$$

$$df = 1186$$

$$t_{\text{crit}} = 1.962$$

$$t_{\text{cal}} = -1.7697$$

fail null hypothesis

After used model 2.2 testing parents' education has not an impact on birth weight at all on 5 percent level of significant.

Question 3. A model of wage equation is given by

$$lwage_i = \beta_1 + \beta_2 exp_i + \beta_3 expsq_i + \beta_4 educ_i + \beta_5 age_i + \beta_6 kid6_i + \beta_7 kid18_i + u_i$$

where $lwage_i$ = natural log of hourly wage of married women
 exp_i = years of experience
 $expsq_i$ = years of experience squared
 $educ_i$ = years of education
 age_i = age
 $kid6_i$ = number of children aged 0-6 in a household
 $kid18_i$ = number of children aged 6-18 in a household

The regression result from OLS is shown in the table below and answer the following questions.

Source	SS	df	MS	Number of obs = 428		
Model	35.1394	6	5.89	F(6, 421)	=	13.19
Residual	197.9876	421	.446526442	Prob > F	=	0.0000
Total	223.327441	427		R-squared	=	0.1582
	223.3274			Adj R-squared	=	
				Root MSE	=	.66823

lwage	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]	
exper	.039819	.013393	2.97	0.003	.0134936	.0661444
expersq	-.0007812	.0004022	-1.94	0.053	-.0015718	9.37e-06
educ	.1078319	.0144021	7.49	0.000	.079523	.1361409
age	-.0014653	.0052925	-0.28	0.782	-.0118682	.0089377
kidslt6	-.0607106	.0887626	-0.68	0.494	-.2351836	.1137625
kidsge6	-.014591	.0278981	-0.52	0.601	-.069428	.0402459
_cons	-.4209078	.316905	-1.33	0.185	-1.043821	.2020053

- Figure out all the degrees of freedom in this model.
- Figure out all the sum of squares (ESS and RSS) and mean squares in this model.
- Figure out the adjusted R-squared (\bar{R}^2)
- Given that the model above is called ‘**Model 3.1**’, there is another competing model called ‘**Model 3.2**’ which an **explanatory variable is excluded**, compared to ‘**Model 3.1**’. Though the result of estimating ‘**Model 3.2**’ is not shown here, **what is the maximum value of R^2 from ‘Model 3.2’** which will make you conclude that the excluded variable has a significant contribution in ‘**Model 3.1**’, at the significance level of 0.05. (**Hint:** the critical value of the F-test at the significance level of 0.05 is $F_{1,421} = 3.84$)
- As you can see from the result, age is not significantly different from zero. In other words, age does not determine how much hourly wage would be. Does this make economic sense in your opinion? What do you think cause this insignificance?

$$a) \quad n = 429$$

$$k = 7$$

$$df_1 = k - 1 = 7 - 1 = 6$$

$$df_2 = n - k = 429 - 7 = 421$$

$$b) \quad RSS = MSR \times df_2$$

$$= 0.4465 \times 421$$

$$= 187.9765$$

$$TSS = ESS + RSS$$

$$223.3279 = ESS + 187.9765$$

$$ESS = 223.3279 - 187.9765$$

$$= 35.3509$$

$$c) \quad \text{adjusted } R\text{-squared} = 1 - (1 - R^2) \left[\frac{n-1}{n-k} \right]$$

$$= 1 - (1 - (0.15827)) \left(\frac{429-1}{429-7} \right)$$

$$= 1 - (0.84173) (1.0143)$$

$$= 1 - 0.8534$$

$$= 0.1466$$

d) Accept Model when $F_{cal} > F_{crit}$

$$F_{cal} > 3.84$$

$$\frac{R^2 / (k-1)}{(1-R^2) / (n-k)} > 3.84$$

$$\frac{R^2 / 6}{(1-R^2) / 421} > 3.84$$

$$\frac{R^2}{1-R^2} > \frac{3.84(6)}{421}$$

$$R^2 > 0.0547 - 0.0547R^2$$

$$1.0547 R^2 > 0.0547$$

$$R^2 > 0.0518$$

e) I think this has mistake about all independent variable don't transform in logarithm follow variable of wage. Wage transform in logarithm form this result affect all variable insignificant. I advise first transform all variable in logarithm second, analysis in logarithm form and final read result again. I think have some variable impact on $\log(\text{wage})$