

Assignment #2

Instructions:

- For all questions, answer up to 4 decimal places.
- This assignment is due on **Thursday, May 20, 2021 before 23.59**.
- Write your answer in either digital or ordinary paper. For digital paper, export pages into a single PDF file. For ordinary paper, take photos of your writing and convert them into a single PDF file as well.
- There is no need to rewrite the question. Assign number item, i.e. 1 a., clearly before your answer is sufficient.
- Submit your assignment into Moodle.
- Name your file as StudentID_Nickname (in Thai) such as 123456789_น้อย. **Please follow this instruction strictly since it will help me a lot with file management.**

Question 1. The data set CEOSAL1.DTA contains information on 209 CEOs for the year 1990; these data were obtained from Business Week (5/6/1991). To study effect of firm performances and types of industry where CEOs work on CEO compensation, the CEO salary regression is proposed as follows:

$$\log(\text{salary}_i) = \beta_0 + \beta_1 \log(\text{sales}_i) + \beta_2 \text{ROE}_i + \beta_3 \text{finance}_i + \beta_4 \text{consprod}_i + \beta_5 \text{utility}_i + u_i$$

where

- $\log(\text{salary}_i)$ = logarithm of CEO annual salary (in 1,000 USD)
- $\log(\text{sales}_i)$ = logarithm of firms' sale (in 1 million USD)
- ROE_i = average return on equity for the CEO's firm for the previous three years (Return on equity is defined in terms of net income as a percentage of common equity)
- finance_i = 1 if in financial industry, = 0 otherwise
- consprod_i = 1 if in consumer product industry, = 0 otherwise
- utility_i = 1 if in utility industry, = 0 otherwise

dummy {

(finance_i , consprod_i , and utility_i are binary variables indicating the financial, consumer products, and utilities industries. The omitted industry is transportation.

Using STATA, the estimation result is shown below. Answer the following questions.

Source	SS	df	MS	Number of obs = 209		
Model	23.8109943	5	4.76219887	F(5, 203)	=	22.53
Residual	42.9111689	203	.211385068	Prob > F	=	0.0000
-----				R-squared	=	0.3569
Total	66.7221632	208	.320779631	Adj R-squared	=	0.3410
-----				Root MSE	=	.45977

lsalary	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]	
lsales	.2571917	.0320348	8.03	0.000	.0194282	.3203553
roe	.0111517	.3342996	2.59	0.010	.0026742	.0196293
finance	.1579564	.0890017	1.77	0.077	-.0175299	.3334426
consprod	.1808917	.0847683	2.13	0.034	.0137524	.3480311
utility	-.2830015	.0992337	-2.85	0.005	-.4786624	-.0873405
_cons	4.588101	.2950221	15.55	0.000	4.0064	5.169801

- Write out the estimated regression equation for $\log(\text{salary}_i)$. Interpret the estimated coefficient associated with $\log(\text{sales}_i)$.
- What is the overall significance of the regression? What test do you use? Which of the coefficients are individually statistically significant at the 5 percent level? State **the critical value** for hypothesis testing to receive full points.
- Compute the approximate percentage difference in estimated salary between the utility and transportation sector, holding sales_i and ROE_i fixed.
- Why can't we put all the sector dummies (i.e. finance_i , consprod_i , utility_i and transport_i) in the equation? What would happen if we put all the sector dummies in the equation and use STATA run the regression anyway?
- In the above model, is there any benefit if we add interaction terms between roe and sector dummies, i.e. $\text{ROE}_i * \text{finance}_i$ and/or $\text{ROE}_i * \text{consprod}_i$ and/or $\text{ROE}_i * \text{utility}_i$?

$$\log(\text{salary}_i) = \beta_0 + \beta_1 \log(\text{sales}_i) + \beta_2 \text{ROE}_i + \beta_3 \text{finance}_i + \beta_4 \text{consprod}_i + \beta_5 \text{utility}_i + u_i$$

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lsalary	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]
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_cons	4.588101	.2950221	15.55	0.000	4.0064 5.169801

Number of obs = 209
 F(5, 203) = 22.53
 Prob > F = 0.0000
 R-squared = 0.3569
 Adj R-squared = 0.3410
 Root MSE = .45977

a. Write out the estimated regression equation for $\log(\text{salary}_i)$. Interpret the estimated coefficient associated with $\log(\text{sales}_i)$.

$$\log(\text{salary}_i) = 4.5881 + 0.2572 \log(\text{sales}_i) + 0.0112 \text{ROE}_i + 0.1580 \text{Finance}_i + 0.1809 \text{Consprod}_i - 0.2830 \text{Utility}_i$$

- The intercept is 4.5881 where whether we get sales, have ROE, etc. or not, we still get salary by $\log(\text{salary}_i) = 4.5881$ or $\log^{-1}(4.5881)$.

- If $\log(\text{sales}_i)$ increase by 1 unit, $\log(\text{salary}_i)$ would increase by 0.2572 unit given other things constant.

b. What is the overall significance of the regression? What test do you use? Which of the coefficients are individually statistically significant at the 5 percent level? State the critical value for hypothesis testing to receive full points.

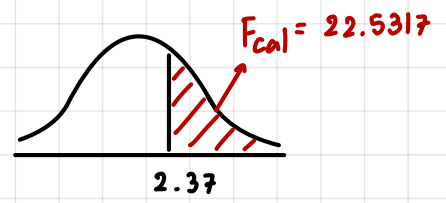
Overall significance test by using F-test :

$$H_0: \beta_0 = \beta_1 = \beta_2 = \beta_3 = \beta_4 = \beta_5 = 0$$

H_a : Otherwise

$$F_{cal} = \frac{R^2 / k}{(1 - R^2) / (n - k - 1)} = \frac{0.3569 / 5}{1 - 0.3569 / 209 - 5 - 1} = 22.5317$$

$$F_{cri} = F(k, n - k - 1)_{\alpha = 0.05} = F(5, 203)_{\alpha = 0.05} = 2.37$$



$F_{cal} > F_{cri}$: can reject H_0 at the significant level of 0.05, heteroscedasticity

- significant (α) = 0.05 since CI = 95%

- Use t-test where set $\beta = 0$

- significant: All coefficients are significant

$$\beta_0: \text{cons} : t_{\text{cal}} = 4.5881 / 0.2950 = 15.5529$$

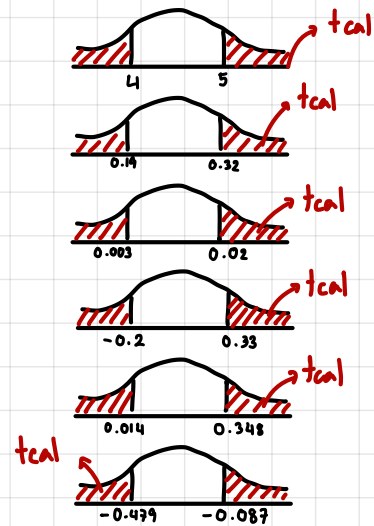
$$\beta_1: \text{sales} : t_{\text{cal}} = 0.2572 / 0.0320 = 8.0375$$

$$\beta_2: \text{ROE} : t_{\text{cal}} = 0.0112 / 0.3343 = 0.03350$$

$$\beta_3: \text{Finance} : t_{\text{cal}} = 0.1580 / 0.0890 = 1.7753$$

$$\beta_4: \text{Consprod} : t_{\text{cal}} = 0.1809 / 0.0848 = 2.1333$$

$$\beta_5: \text{Utility} : t_{\text{cal}} = -0.2830 / 0.0992 = -2.8528$$



T-testing of the model where $\alpha = 0.05$

$$\text{d.f.} = n - k = 209 - 5 = 204$$

$$t_{\text{lower}} : t_{\frac{\alpha}{2}} = t_{\frac{0.05}{2}} \quad | \quad t_{\text{lower}} = -1.96$$

$$t_{\text{upper}} : t_{\frac{\alpha}{2}} = t_{\frac{0.05}{2}} \quad | \quad t_{\text{upper}} = 1.96$$

$$\hat{\beta}_0 = 15.5529$$

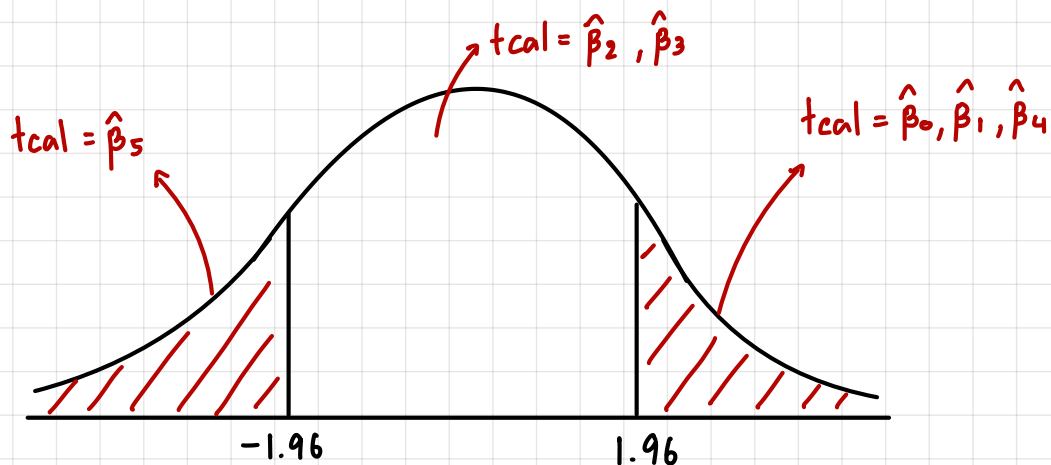
$$\hat{\beta}_1 = 8.0375$$

$$\hat{\beta}_2 = 0.03350$$

$$\hat{\beta}_3 = 1.7753$$

$$\hat{\beta}_4 = 2.1333$$

$$\hat{\beta}_5 = -2.8528$$



\therefore We cannot reject Null hypothesis of ROE & Finance at the significant level of 0.05

- c. Compute the approximate percentage difference in estimated salary between the utility and transportation sector, holding $sales_i$ and ROE_i fixed.

Take a partial derivative of $\log(\text{salary})$ to utility

$$\rightarrow \frac{\partial \log(\text{salary})}{\partial \text{Utility}} = \beta_s \text{Utility} = (0.2830) \text{Utility}$$

$$\rightarrow \text{Transportation is the base line (intercept)} = \ln(4.5881) \rightarrow \text{real number: } e^{4.5881} = 98.3075$$

$$\rightarrow \text{intercept of Utility} = \ln(4.5881 - 0.2830) = \ln(4.3051) \rightarrow e^{4.3051} = 74.0766$$

$$e^{(4.5881)} = 98.3075$$

$$e^{(4.3051)} = 74.0766$$

$$\therefore \text{Percentage different} : \frac{98.3075 - 74.0766}{98.3075} = 0.2465 \quad \text{or} \quad 24.6481\%$$

- d. Why can't we put all the sector dummies (i.e. $finance_i$, $consprod_i$, $utility_i$ and $transport_i$) in the equation? What would happen if we put all the sector dummies in the equation and use STATA run the regression anyway?

- We don't put $transportation_i$ in the equation as it's already the baseline to the salary of the CEO. If we put into equation and run stata anyway, the result is that we will have more errors. Further more, the result of dummy will not be 1 nor 0.

- e. In the above model, is there any benefit if we add interaction terms between roe and sector dummies, i.e. $ROE_i * finance_i$ and/or $ROE_i * consprod_i$ and/or $ROE_i * utility_i$?

To make the interaction with dummies would effect the model that it will may or may not increase the R^2 of the relevant to the model. To test whether to make the interaction or not can be test by "Marginal Contribution". If the result in this test is to reject Null hypothesis test means that the interaction is benefit to the model

[H_0 : Interaction (variables) has no marginal contribution to the model .

H_a : otherwise]

Question 2. Birth weight has been used by officials as one of the main determinants of health. Data set BWGHT.DTA contains data on infant birth weights in ounces ($bwght_i$), average number of cigarettes mother smoked per day during pregnancy ($cigs$), family income ($faminc_i$), father's year of education ($fatheduc_i$), and mother's year of education ($motheduc_i$). The following two regressions were estimated using data on $n = 1191$ births:

Model 2.1: $bwght_i = \beta_0 + \beta_1 cigs_i + \beta_2 faminc_i + u_i$

regress bwght cigs faminc					
Source	SS	df	MS		
Model	14536.9538	2	7268.47691	Number of obs =	1191
Residual	468209.738	1188	394.115941	F(2, 1188) =	18.44
Total	482746.692	1190	405.669489	Prob > F =	0.0000
				R-squared =	0.0301
				Adj R-squared =	0.0285
				Root MSE =	19.852
bwght	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]
cigs	-.5876985	.1090181			
faminc	.0624684	.0324438			
_cons	118.5568	1.234278			

Omitted for the purpose of this exam.

Model 2.2: $bwght_i = \beta_0 + \beta_1 cigs_i + \beta_2 faminc_i + \beta_3 fatheduc_i + \beta_4 motheduc_i + u_i$

regress bwght cigs faminc fatheduc motheduc					
Source	SS	df	MS		
Model	15827.6593	4	3956.91482	Number of obs =	1191
Residual	466919.033	1186	393.69227	F(4, 1186) =	10.05
Total	482746.692	1190	405.669489	Prob > F =	0.0000
				R-squared =	0.0328
				Adj R-squared =	0.0295
				Root MSE =	19.842
bwght	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]
cigs	-.5894954	.1106172			
faminc	.0538254	.0366502			
fatheduc	.4936695	.2832896			
motheduc	-.4379234	.3197377			
_cons	118.0741	3.500291			

Omitted for the purpose of this exam.

- where $bwght_i$ = birth weight, ounces (**02**)
- $cigs_i$ = average number of cigarettes the mother smoked per day while pregnant
- $faminc_i$ = 1988 family income, \$1000s
- $fatheduc_i$ = father's years of education
- $motheduc_i$ = mother's years of education

Answer the following questions.

- a. Based on **Model 2.1**, test whether smoking has an impact on birth weight. Show your work. (use $\alpha = 0.05$)
- b. Based on **Model 2.1**, construct a 99% confidence interval for β_2 .
- c. Would your conclusion in a) change if you use the result from **Model 2.2**? Show your work. (use $\alpha = 0.05$)
- d. What is the overall significance of the regression from **Model 2.2**? What test do you use? Which of the coefficients are individually statistically significant at the 5 percent level? State the critical value for hypothesis testing to receive full points.
- e. If we are interested in testing whether “**parents’ education**” has an impact on birth weight at all, what kind of null/alternative hypothesis would we be testing? Perform the test and discuss your finding. (use $\alpha = 0.05$)

a. Based on Model 2.1, test whether smoking has an impact on birth weight. Show your work.

(use $\alpha = 0.05$) assume $\beta_1 = 0$

Model 2.1: $bwght_i = \beta_0 + \beta_1 cigs_i + \beta_2 faminc_i + u_i$ $H_0 : \beta_1 = 0$ $H_a : \beta_1 \neq 0$

regress bwght cigs faminc				$k=3$	
Source	SS	df	MS	Number of obs	= 1191
Model	14536.9538	2	7268.47691	F(2, 1188)	= 18.44
Residual	468209.738	1188	394.115941	Prob > F	= 0.0000
Total	482746.692	1190	405.669489	R-squared	= 0.0301
				Adj R-squared	= 0.0285
				Root MSE	= 19.852

bwght	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]
cigs	-.5876985	.1090181			Omitted for the purpose of this exam.
faminc	.0624684	.0324438			
_cons	118.5568	1.234278			

$$bwght_i = 118.5568 - 0.5877 cigs_i + 0.0625 faminc_i$$

$$d.f. = n - k = 1191 - 3 = 1188$$

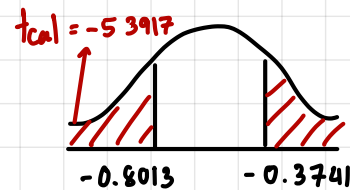
$$t_{cal} = \frac{-0.5877 - 0}{0.1090} = -5.3917 \quad \text{significant}$$

$$t_{\frac{\alpha}{2}} = t_{\frac{0.05}{2}} = 1.96$$

$$\rightarrow P[\hat{\beta}_1 - (t_{\frac{\alpha}{2}} \times \hat{\sigma}_{\hat{\beta}_1}) \leq \hat{\beta}_1 \leq \hat{\beta}_1 + (t_{\frac{\alpha}{2}} \times \hat{\sigma}_{\hat{\beta}_1})]$$

$$\text{Lower: } (-0.5877) - (1.96)(0.1090) = -0.8013$$

$$\text{Upper: } (-0.5877) + (1.96)(0.1090) = -0.3741$$



\therefore we can say that smoking has effect on birth weight 95 out of 100 times

b. Based on Model 2.1, construct a 99% confidence interval for β_2 . assume $\beta_2 = 0$

Model 2.1: $bwght_i = \beta_0 + \beta_1 cigs_i + \beta_2 faminc_i + u_i$ $H_0 : \beta_2 = 0$ $H_a : \beta_2 \neq 0$

regress bwght cigs faminc					
Source	SS	df	MS	Number of obs	= 1191
Model	14536.9538	2	7268.47691	F(2, 1188)	= 18.44
Residual	468209.738	1188	394.115941	Prob > F	= 0.0000
Total	482746.692	1190	405.669489	R-squared	= 0.0301
				Adj R-squared	= 0.0285
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bwght	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]
cigs	-.5876985	.1090181			Omitted for the purpose of this exam.
faminc	.0624684	.0324438			
_cons	118.5568	1.234278			

$$bwght_i = 118.5568 - 0.5877 cigs_i + 0.0625 faminc_i$$

$$d.f. = n - k = 1191 - 3 = 1188$$

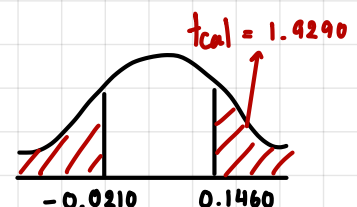
$$t_{cal} = \frac{0.0625 - 0}{0.0324} = 1.9290 \quad \text{significant}$$

$$t_{\frac{\alpha}{2}} = t_{\frac{0.01}{2}} = 2.576$$

$$\rightarrow P[\hat{\beta}_2 - (t_{\frac{\alpha}{2}} \times \hat{\sigma}_{\hat{\beta}_2}) \leq \hat{\beta}_2 \leq \hat{\beta}_2 + (t_{\frac{\alpha}{2}} \times \hat{\sigma}_{\hat{\beta}_2})]$$

$$\text{Lower: } (0.0625) - (2.576)(0.0324) = -0.0210$$

$$\text{Upper: } (0.0625) + (2.576)(0.0324) = 0.1460$$



\therefore we can say that family income effect the birth weighted in significant level of 0.01.

c. Would your conclusion in a) change if you use the result from Model 2.2? Show your work.

(use $\alpha = 0.05$)

$$H_0 : \beta_1 = 0 \quad H_a : \beta_1 \neq 0$$

Model 2.2: $bwght_i = \beta_0 + \beta_1cigs_i + \beta_2faminc_i + \beta_3fathereduc_i + \beta_4mothereduc_i + u_i$

regress bwght cigs faminc fatheduc motheduc				$k = 5$	
Source	SS	df	MS		
Model	15827.6593	4	3956.91482	Number of obs =	1191
Residual	466919.033	1186	393.69227	F(4, 1186) =	10.05
Total	482746.692	1190	405.669489	Prob > F =	0.0000
				R-squared =	0.0328
				Adj R-squared =	0.0295
				Root MSE =	19.842

	bwght	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]
cigs		-0.5894954	0.1106172			
faminc		0.0538254	0.0366502			
fatheduc		0.4936695	0.2832896			
motheduc		-0.4379234	0.3197377			
_cons		118.0741	3.500291			

$$bwght_i = 118.5568 - 0.5877cigs_i + 0.0625faminc_i + 0.4937fathereduc_i - 0.4379mothereduc_i$$

$$t_{cal} = \frac{-0.5895 - 0}{0.1106} = -5.3300 \quad \text{significant}$$

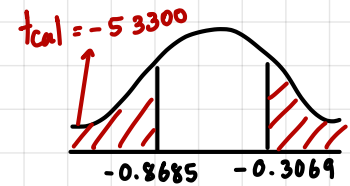
$$d.f. = n - k = 1191 - 5 = 1,186$$

$$t_{\frac{\alpha}{2}} = t_{\frac{0.05}{2}} = 2.576$$

$$\rightarrow P[\hat{\beta}_1 - (t_{\frac{\alpha}{2}} \times \delta\hat{\beta}_1) \leq \hat{\beta}_1 \leq \hat{\beta}_1 + (t_{\frac{\alpha}{2}} \times \delta\hat{\beta}_1)]$$

$$\text{Lower: } (-0.5877) - (2.576)(0.1090) = -0.8685$$

$$\text{Upper: } (-0.5877) + (2.576)(0.1090) = -0.3069$$



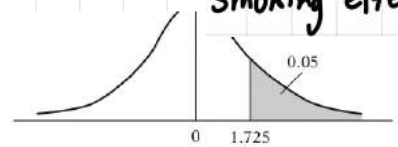
\therefore We reject null hypothesis at the significant level of 0.05 where we can conclude that

Smoking effect the birth weighted.

Percentage Points of the t Distribution

Source: From E. S. Pearson and H. O. Hartley, eds., *Biometrika Tables for Statisticians*, vol. 1, 3d ed., table 12, Cambridge University Press, New York, 1966. Reproduced by permission of the editors and trustees of *Biometrika*.

$\Pr(t > 2.086) = 0.025$
 $\Pr(t > 1.725) = 0.05$ for $df = 20$
 $\Pr(|t| > 1.725) = 0.10$



Pr	0.25	0.10	0.05	0.025	0.01	0.005	0.001
df	0.50	0.20	0.10	0.05	0.02	0.010	0.002
1	1.000	3.078	6.314	12.706	31.821	63.657	318.31
2	0.816	1.886	2.920	4.303	6.965	9.925	22.327
3	0.765	1.638	2.353	3.182	4.541	5.841	10.214
4	0.741	1.533	2.132	2.776	3.747	4.604	7.173
5	0.727	1.476	2.015	2.571	3.365	4.032	5.893
6	0.718	1.440	1.943	2.447	3.143	3.707	5.208
7	0.711	1.415	1.895	2.365	2.998	3.499	4.785
8	0.706	1.397	1.860	2.306	2.896	3.355	4.501
9	0.703	1.383	1.833	2.262	2.821	3.250	4.297
10	0.700	1.372	1.812	2.228	2.764	3.169	4.144
11	0.697	1.363	1.796	2.201	2.718	3.106	4.025
12	0.695	1.356	1.782	2.179	2.681	3.055	3.930
13	0.694	1.350	1.771	2.160	2.650	3.012	3.852
14	0.692	1.345	1.761	2.145	2.624	2.977	3.787
15	0.691	1.341	1.753	2.131	2.602	2.947	3.733
16	0.690	1.337	1.746	2.120	2.583	2.921	3.686
17	0.689	1.333	1.740	2.110	2.567	2.898	3.646
18	0.688	1.330	1.734	2.101	2.552	2.878	3.610
19	0.688	1.328	1.729	2.093	2.539	2.861	3.579
20	0.687	1.325	1.725	2.086	2.528	2.845	3.552
21	0.686	1.323	1.721	2.080	2.518	2.831	3.527
22	0.686	1.321	1.717	2.074	2.508	2.819	3.505
23	0.685	1.319	1.714	2.069	2.500	2.807	3.485
24	0.685	1.318	1.711	2.064	2.492	2.797	3.467
25	0.684	1.316	1.708	2.060	2.485	2.787	3.450
26	0.684	1.315	1.706	2.056	2.479	2.779	3.435
27	0.684	1.314	1.703	2.052	2.473	2.771	3.421
28	0.683	1.313	1.701	2.048	2.467	2.763	3.408
29	0.683	1.311	1.699	2.045	2.462	2.756	3.396
30	0.683	1.310	1.697	2.042	2.457	2.750	3.385
40	0.681	1.303	1.684	2.021	2.423	2.704	3.307
60	0.679	1.296	1.671	2.000	2.390	2.660	3.232
120	0.677	1.289	1.658	1.980	2.358	2.617	3.160
∞	0.674	1.282	1.645	1.960	2.326	2.576	3.090

- d. What is the overall significance of the regression from Model 2.2? What test do you use? Which of the coefficients are individually statistically significant at the 5 percent level? State the critical value for hypothesis testing to receive full points. $\alpha = 0.05$

$k = 5$

Model 2.2: $bwght_i = \beta_0 + \beta_1cigs_i + \beta_2faminc_i + \beta_3fathereduc_i + \beta_4mothereduc_i + u_i$

regress bwght cigs faminc fatheduc motheduc				Number of obs = 1191	
Source	SS	df	MS	F(4, 1186)	Prob > F = 0.0000
Model	15827.6593	4	3956.91482	R-squared = 0.0328	
Residual	466919.033	1186	393.69227	Adj R-squared = 0.0295	
Total	482746.692	1190	405.669489	Root MSE = 19.842	

	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]
bwght					
cigs	-.5894954	.1106172			
faminc	.0538254	.0366502			
fatheduc	.4936695	.2832896			
motheduc	-.4379234	.3197377			
_cons	118.0741	3.500291			

Omitted for the purpose of this exam.

Using F-test for test overall significance : $H_1 : \beta_0 = \beta_1 = \beta_2 = \beta_3 = \beta_4 = 0$
 $H_a : \text{otherwise}$

$$F_{cal} = \frac{R^2 / k}{(1 - R^2) / (n - k - 1)} = \frac{0.0328 / 5}{(1 - 0.0328) / (1191 - 5 - 1)} = \frac{0.0066}{0.0008}$$

$$F_{cal} = 8.0862$$

$F_{cal} > F_{cri} : \text{can reject } H_0$

$$F_{cri} = F(k, n - k - 1) = F(5, 1185) = 2.37$$

$\alpha = 0.05$

heteroscedasticity

df for denominator N_2	Pr	k df for numerator N_1												
		1	2	3	4	5	6	7	8	9	10	11	12	
22	.25	1.40	1.48	1.47	1.45	1.44	1.44	1.42	1.41	1.40	1.39	1.39	1.38	1.37
	.10	2.95	2.56	2.35	2.22	2.13	2.06	2.01	1.97	1.93	1.90	1.88	1.88	1.86
	.05	4.30	3.44	3.05	2.82	2.66	2.55	2.46	2.40	2.34	2.30	2.26	2.26	2.23
	.01	7.95	5.72	4.82	4.31	3.99	3.76	3.59	3.45	3.35	3.26	3.18	3.18	3.12
24	.25	1.39	1.47	1.46	1.44	1.43	1.41	1.40	1.39	1.38	1.38	1.37	1.37	1.36
	.10	2.93	2.54	2.33	2.19	2.10	2.04	1.98	1.94	1.91	1.88	1.85	1.85	1.83
	.05	4.26	3.40	3.01	2.78	2.62	2.51	2.42	2.36	2.30	2.25	2.21	2.21	2.18
	.01	7.82	5.61	4.72	4.22	3.90	3.67	3.50	3.36	3.26	3.17	3.09	3.09	3.03
26	.25	1.38	1.46	1.45	1.44	1.42	1.41	1.39	1.38	1.38	1.37	1.37	1.36	1.35
	.10	2.91	2.52	2.31	2.17	2.08	2.01	1.96	1.92	1.88	1.86	1.84	1.84	1.81
	.05	4.23	3.37	2.98	2.74	2.59	2.47	2.39	2.32	2.27	2.22	2.18	2.18	2.15
	.01	7.72	5.53	4.64	4.14	3.82	3.59	3.42	3.29	3.18	3.09	3.02	3.02	2.96
28	.25	1.38	1.46	1.45	1.43	1.41	1.40	1.39	1.38	1.37	1.37	1.36	1.35	1.34
	.10	2.89	2.50	2.29	2.16	2.06	2.00	1.94	1.90	1.87	1.84	1.81	1.81	1.79
	.05	4.20	3.34	2.95	2.71	2.56	2.45	2.36	2.29	2.24	2.19	2.15	2.15	2.12
	.01	7.64	5.45	4.57	4.07	3.75	3.53	3.36	3.23	3.12	3.03	2.96	2.96	2.90
30	.25	1.38	1.45	1.44	1.42	1.41	1.39	1.38	1.37	1.36	1.35	1.35	1.35	1.34
	.10	2.88	2.49	2.28	2.14	2.05	1.98	1.93	1.88	1.85	1.82	1.79	1.79	1.77
	.05	4.17	3.32	2.92	2.69	2.53	2.42	2.33	2.27	2.21	2.16	2.13	2.13	2.09
	.01	7.56	5.39	4.51	4.02	3.70	3.47	3.30	3.17	3.07	2.98	2.91	2.91	2.84
40	.25	1.36	1.44	1.42	1.40	1.39	1.37	1.36	1.35	1.34	1.33	1.32	1.32	1.31
	.10	2.84	2.44	2.23	2.09	2.00	1.93	1.87	1.83	1.79	1.76	1.73	1.73	1.71
	.05	4.08	3.23	2.84	2.61	2.45	2.34	2.25	2.18	2.12	2.08	2.04	2.04	2.00
	.01	7.31	5.18	4.31	3.83	3.51	3.29	3.12	2.99	2.89	2.80	2.73	2.73	2.66
60	.25	1.35	1.42	1.41	1.38	1.37	1.35	1.33	1.32	1.31	1.30	1.29	1.29	1.29
	.10	2.79	2.39	2.18	2.04	1.95	1.87	1.82	1.77	1.74	1.71	1.68	1.68	1.66
	.05	4.00	3.15	2.76	2.53	2.37	2.25	2.17	2.10	2.04	1.99	1.95	1.95	1.92
	.01	7.08	4.98	4.13	3.65	3.34	3.12	2.95	2.82	2.72	2.63	2.56	2.56	2.50
120	.25	1.34	1.40	1.39	1.37	1.35	1.33	1.31	1.30	1.29	1.28	1.27	1.27	1.26
	.10	2.75	2.35	2.13	1.99	1.90	1.82	1.77	1.72	1.68	1.65	1.62	1.62	1.60
	.05	3.92	3.07	2.68	2.45	2.29	2.17	2.09	2.02	1.96	1.91	1.87	1.87	1.83
	.01	6.85	4.79	3.95	3.48	3.17	2.96	2.79	2.66	2.56	2.47	2.40	2.40	2.34
200	.25	1.33	1.39	1.38	1.36	1.34	1.32	1.31	1.29	1.28	1.27	1.26	1.26	1.25
	.10	2.73	2.33	2.11	1.97	1.88	1.80	1.75	1.70	1.66	1.63	1.60	1.60	1.57
	.05	3.89	3.04	2.65	2.42	2.26	2.14	2.06	1.98	1.93	1.88	1.84	1.84	1.80
	.01	6.76	4.71	3.88	3.41	3.11	2.89	2.73	2.60	2.50	2.41	2.34	2.34	2.27
∞	.25	1.32	1.39	1.37	1.35	1.33	1.31	1.29	1.28	1.27	1.25	1.24	1.24	1.24
	.10	2.71	2.30	2.08	1.94	1.85	1.77	1.72	1.67	1.63	1.60	1.57	1.57	1.55
	.05	3.84	3.00	2.60	2.37	2.21	2.10	2.01	1.94	1.88	1.83	1.79	1.79	1.75
	.01	6.63	4.61	3.78	3.32	3.02	2.80	2.64	2.51	2.41	2.32	2.25	2.25	2.18

$n - k - 1$

Using t-test for testing individually (Assume $\beta = 0$) $\alpha = 0.05$

Model 2.2: $bwght_i = \beta_0 + \beta_1cigs_i + \beta_2faminc_i + \beta_3fathereduc_i + \beta_4mothereduc_i + u_i$

regress bwght cigs faminc fathereduc mothereduc				
Source	SS	df	MS	
Model	15827.6593	4	3956.91482	Number of obs = 1191
Residual	466919.033	1186	393.69227	F(4, 1186) = 10.05
Total	482746.692	1190	405.669489	Prob > F = 0.0000
				R-squared = 0.0328
				Adj R-squared = 0.0295
				Root MSE = 19.842

	bwght	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]
β_1	cigs	-.5894954	.1106172			
β_2	faminc	.0538254	.0366502			
β_3	fathereduc	.4936695	.2832896			
β_4	mothereduc	-.4379234	.3197377			
β_0	_cons	118.0741	3.500291			

Omitted for the purpose of this exam.

$$d.f. = n - k = 1191 - 5 = 1,186$$

$$H_0 : \beta_0 = 0 \quad H_a : \beta_0 \neq 0$$

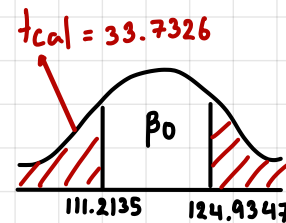
$$\text{Test } \hat{\beta}_0 ; t_{cal} = 118.0741 / 3.5003 = 33.7326 \text{ significant}$$

$$t_{\frac{\alpha}{2}} = \frac{t_{0.05}}{2} = 1.96$$

$$\rightarrow P[\hat{\beta}_0 - (t_{\frac{\alpha}{2}} \times \sigma_{\hat{\beta}_0}) \leq \hat{\beta}_0 \leq \hat{\beta}_0 + (t_{\frac{\alpha}{2}} \times \sigma_{\hat{\beta}_0})]$$

$$\text{Lower: } (118.0741) - (1.96)(3.5003) = 111.2135$$

$$\text{Upper: } (118.0741) + (1.96)(3.5003) = 124.9347$$



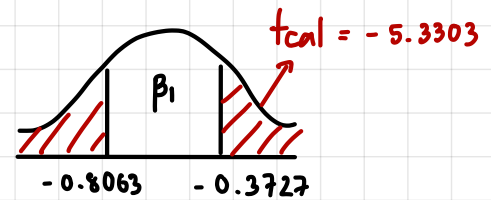
$$H_0 : \beta_1 = 0 \quad H_a : \beta_1 \neq 0$$

$$\text{Test } \hat{\beta}_1 ; t_{cal} = -0.5895 / 0.1106 = -5.3300 \text{ significant}$$

$$\rightarrow P[\hat{\beta}_1 - (t_{\frac{\alpha}{2}} \times \sigma_{\hat{\beta}_1}) \leq \hat{\beta}_1 \leq \hat{\beta}_1 + (t_{\frac{\alpha}{2}} \times \sigma_{\hat{\beta}_1})]$$

$$\text{Lower: } (-0.5895) - (1.96)(0.1106) = -0.8063$$

$$\text{Upper: } (-0.5895) + (1.96)(0.1106) = -0.3727$$



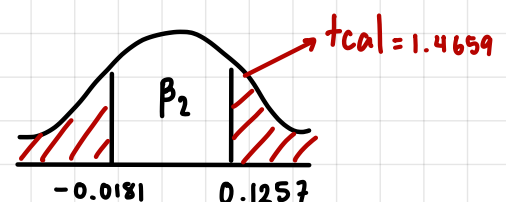
$$H_0 : \beta_2 = 0 \quad H_a : \beta_2 \neq 0$$

$$\text{Test } \hat{\beta}_2 ; t_{cal} = 0.0538 / 0.0367 = 1.4659 \text{ significant}$$

$$\rightarrow P[\hat{\beta}_2 - (t_{\frac{\alpha}{2}} \times \sigma_{\hat{\beta}_2}) \leq \hat{\beta}_2 \leq \hat{\beta}_2 + (t_{\frac{\alpha}{2}} \times \sigma_{\hat{\beta}_2})]$$

$$\text{Lower: } (0.0538) - (1.96)(0.0367) = -0.0181$$

$$\text{Upper: } (0.0538) + (1.96)(0.0367) = 0.1257$$



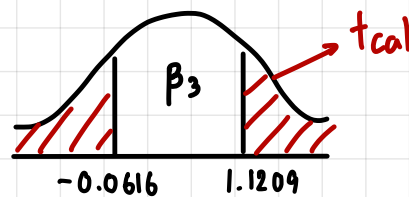
$$H_0 : \beta = 0 \quad H_a : \beta \neq 0$$

$$\text{Test } \hat{\beta}_3 ; t_{\text{cal}} = 0.4937 / 0.2833 = 1.7427 \quad \text{significant}$$

$$\rightarrow P[\hat{\beta}_3 - (t_{\frac{\alpha}{2}} \times \delta_{\hat{\beta}_3}) \leq \hat{\beta}_3 \leq \hat{\beta}_3 + (t_{\frac{\alpha}{2}} \times \delta_{\hat{\beta}_3})]$$

$$\text{Lower: } (0.4937) - (1.96)(0.2833) = -0.0616$$

$$\text{Upper: } (0.4937) + (1.96)(0.2833) = 1.1209$$



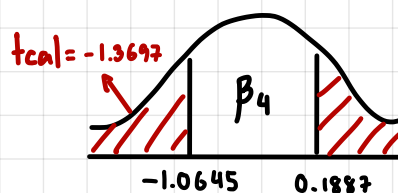
$$H_0 : \beta = 0 \quad H_a : \beta \neq 0$$

$$\text{Test } \hat{\beta}_4 ; t_{\text{cal}} = -0.4379 / 0.3197 = -1.3697$$

$$\rightarrow P[\hat{\beta}_4 - (t_{\frac{\alpha}{2}} \times \delta_{\hat{\beta}_4}) \leq \hat{\beta}_4 \leq \hat{\beta}_4 + (t_{\frac{\alpha}{2}} \times \delta_{\hat{\beta}_4})]$$

$$\text{Lower: } (-0.4379) - (1.96)(0.3197) = -1.0645$$

$$\text{Upper: } (-0.4379) + (1.96)(0.3197) = 0.1887$$

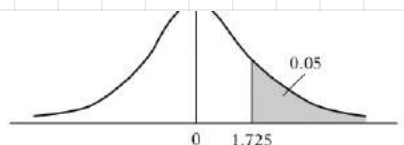


→ This is to find t-test and Confident Interval

Percentage Points of the t Distribution

Source: From E. S. Pearson and H. O. Hartley, eds., *Biometrika Tables for Statisticians*, vol. 1, 3d ed., table 12, Cambridge University Press, New York, 1966. Reproduced by permission of the editors and trustees of *Biometrika*.

$$\begin{aligned} \Pr(t > 2.086) &= 0.025 \\ \Pr(t > 1.725) &= 0.05 \quad \text{for } df = 20 \\ \Pr(|t| > 1.725) &= 0.10 \end{aligned}$$



Pr	0.25	0.10	0.05	0.025	0.01	0.005	0.001
df	0.50	0.20	0.10	0.05	0.02	0.010	0.002
1	1.000	3.078	6.314	12.706	31.821	63.657	318.31
2	0.816	1.886	2.920	4.303	6.965	9.925	22.327
3	0.765	1.638	2.353	3.182	4.541	5.841	10.214
4	0.741	1.533	2.132	2.776	3.747	4.604	7.173
5	0.727	1.476	2.015	2.571	3.365	4.032	5.893
6	0.718	1.440	1.943	2.447	3.143	3.707	5.208
7	0.711	1.415	1.895	2.365	2.998	3.499	4.785
8	0.706	1.397	1.860	2.306	2.896	3.355	4.501
9	0.703	1.383	1.833	2.262	2.821	3.250	4.297
10	0.700	1.372	1.812	2.228	2.764	3.169	4.144
11	0.697	1.363	1.796	2.201	2.718	3.106	4.025
12	0.695	1.356	1.782	2.179	2.681	3.055	3.930
13	0.694	1.350	1.771	2.160	2.650	3.012	3.852
14	0.692	1.345	1.761	2.145	2.624	2.977	3.787
15	0.691	1.341	1.753	2.131	2.602	2.947	3.733
16	0.690	1.337	1.746	2.120	2.583	2.921	3.686
17	0.689	1.333	1.740	2.110	2.567	2.898	3.646
18	0.688	1.330	1.734	2.101	2.552	2.878	3.610
19	0.688	1.328	1.729	2.093	2.539	2.861	3.579
20	0.687	1.325	1.725	2.086	2.528	2.845	3.552
21	0.686	1.323	1.721	2.080	2.518	2.831	3.527
22	0.686	1.321	1.717	2.074	2.508	2.819	3.505
23	0.685	1.319	1.714	2.069	2.500	2.807	3.485
24	0.685	1.318	1.711	2.064	2.492	2.797	3.467
25	0.684	1.316	1.708	2.060	2.485	2.787	3.450
26	0.684	1.315	1.706	2.056	2.479	2.779	3.435
27	0.684	1.314	1.703	2.052	2.473	2.771	3.421
28	0.683	1.313	1.701	2.048	2.467	2.763	3.408
29	0.683	1.311	1.699	2.045	2.462	2.756	3.396
30	0.683	1.310	1.697	2.042	2.457	2.750	3.385
40	0.681	1.303	1.684	2.021	2.423	2.704	3.307
60	0.679	1.296	1.671	2.000	2.390	2.660	3.232
120	0.677	1.289	1.658	1.980	2.358	2.617	3.160
∞	0.674	1.282	1.645	1.960	2.326	2.576	3.090

T-testing of the model where $\alpha = 0.05$

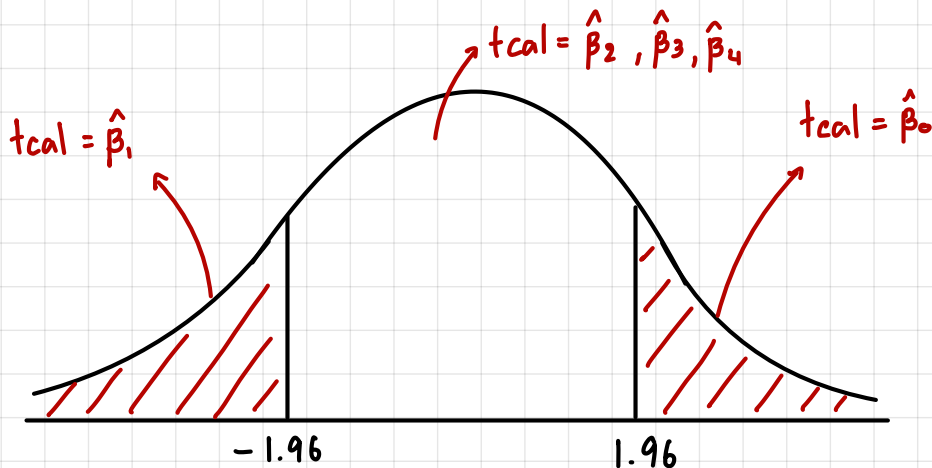
d.f. = $n - k = 209 - 5 = 204$

t_{lower} : $t_{\frac{\alpha}{2}} = t_{\frac{0.05}{2}} \quad | \quad t_{lower} = -1.96$

t_{upper} : $t_{\frac{\alpha}{2}} = t_{\frac{0.05}{2}} \quad | \quad t_{upper} = 1.96$

$\hat{\beta}_0 = 33.7326 \quad \hat{\beta}_1 = -5.3300 \quad \hat{\beta}_2 = 1.4659$

$\hat{\beta}_3 = 1.7427 \quad \hat{\beta}_4 = -1.3697$

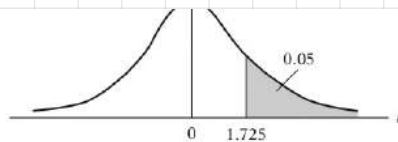


\therefore We cannot reject Null hypothesis of family income & Parents' education at the significant level of 0.05

Percentage Points of the *t* Distribution

Source: From E. S. Pearson and H. O. Hartley, eds., *Biometrika Tables for Statisticians*, vol. 1, 3d ed., table 12, Cambridge University Press, New York, 1966. Reproduced by permission of the editors and trustees of *Biometrika*.

$\Pr(t > 2.086) = 0.025$
 $\Pr(t > 1.725) = 0.05$ for $df = 20$
 $\Pr(|t| > 1.725) = 0.10$



level of 0.05
 (3 estimators)

Pr \ df	0.25	0.10	0.05	0.025	0.01	0.005	0.001
	0.50	0.20	0.10	0.05	0.02	0.010	0.002
1	1.000	3.078	6.314	12.706	31.821	63.657	318.31
2	0.816	1.886	2.920	4.303	6.965	9.925	22.327
3	0.765	1.638	2.353	3.182	4.541	5.841	10.214
4	0.741	1.533	2.132	2.776	3.747	4.604	7.173
5	0.727	1.476	2.015	2.571	3.365	4.032	5.893
6	0.718	1.440	1.943	2.447	3.143	3.707	5.208
7	0.711	1.415	1.895	2.365	2.998	3.499	4.785
8	0.706	1.397	1.860	2.306	2.896	3.355	4.501
9	0.703	1.383	1.833	2.262	2.821	3.250	4.297
10	0.700	1.372	1.812	2.228	2.764	3.169	4.144
11	0.697	1.363	1.796	2.201	2.718	3.106	4.025
12	0.695	1.356	1.782	2.179	2.681	3.055	3.930
13	0.694	1.350	1.771	2.160	2.650	3.012	3.852
14	0.692	1.345	1.761	2.145	2.624	2.977	3.787
15	0.691	1.341	1.753	2.131	2.602	2.947	3.733
16	0.690	1.337	1.746	2.120	2.583	2.921	3.686
17	0.689	1.333	1.740	2.110	2.567	2.898	3.646
18	0.688	1.330	1.734	2.101	2.552	2.878	3.610
19	0.688	1.328	1.729	2.093	2.539	2.861	3.579
20	0.687	1.325	1.725	2.086	2.528	2.845	3.552
21	0.686	1.323	1.721	2.080	2.518	2.831	3.527
22	0.686	1.321	1.717	2.074	2.508	2.819	3.505
23	0.685	1.319	1.714	2.069	2.500	2.807	3.485
24	0.685	1.318	1.711	2.064	2.492	2.797	3.467
25	0.684	1.316	1.708	2.060	2.485	2.787	3.450
26	0.684	1.315	1.706	2.056	2.479	2.779	3.435
27	0.684	1.314	1.703	2.052	2.473	2.771	3.421
28	0.683	1.313	1.701	2.048	2.467	2.763	3.408
29	0.683	1.311	1.699	2.045	2.462	2.756	3.396
30	0.683	1.310	1.697	2.042	2.457	2.750	3.385
40	0.681	1.303	1.684	2.021	2.423	2.704	3.307
60	0.679	1.296	1.671	2.000	2.390	2.660	3.232
120	0.677	1.289	1.658	1.980	2.358	2.617	3.160
∞	0.674	1.282	1.645	1.960	2.326	2.576	3.090

- e. If we are interested in testing whether “parents’ education” has an impact on birth weight at all, what kind of null/alternative hypothesis would we be testing? Perform the test and discuss your finding. (use $\alpha = 0.05$)

Model 2.1: $bwght_i = \beta_0 + \beta_1cigs_i + \beta_2faminc_i + u_i$

$k = 3$

source	SS	df	MS
Model	14536.9538	2	7268.47691
Residual	468209.738	1188	394.115941
Total	482746.692	1190	405.669489

Number of obs	= 1191
F(2, 1188)	= 18.44
Prob > F	= 0.0000
R-squared	= 0.0301
Adj R-squared	= 0.0285
Root MSE	= 19.852

bwght	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]
cigs	-.5876985	.1090181			
faminc	.0624684	.0324438			
_cons	118.5568	1.234278			

Omitted for the purpose of this exam.

Model 2.2: $bwght_i = \beta_0 + \beta_1cigs_i + \beta_2faminc_i + \beta_3fathereduc_i + \beta_4mothereduc_i + u_i$

$k = 5$

source	SS	df	MS
Model	15827.6593	4	3956.91482
Residual	466919.033	1186	393.69227
Total	482746.692	1190	405.669489

Number of obs	= 1191
F(4, 1186)	= 10.05
Prob > F	= 0.0000
R-squared	= 0.0328
Adj R-squared	= 0.0295
Root MSE	= 19.842

bwght	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]
cigs	-.5894954	.1106172			
faminc	.0538254	.0366502			
fathereduc	.4936695	.2832896			
mothereduc	-.4379234	.3197377			
_cons	118.0741	3.500291			

Omitted for the purpose of this exam.

We will test that the added estimators (Parents’ education) is fit regression or not by using “Marginal Contribution”

H_0 : weighted has no marginal contribution to the model

H_a : Otherwise

$$F_{cal} = \frac{R^2_{new} - R^2_{old} / (\# \text{ new regressor})}{1 - R^2_{new} / (n - k_{new})}$$

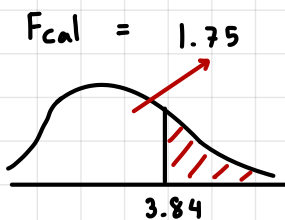
$$= \frac{0.0328 - 0.0301 / 5 - 3}{1 - 0.0328 / (1191 - 5)}$$

$$= \frac{0.0014}{0.0008}$$

$$F_{cri} (1, n-3) \xrightarrow{\alpha = 0.05} F_{cri} (1, 1188) \xrightarrow{\alpha = 0.05}$$

$$F_{cri} = 3.84$$

$F_{cal} < F_{cri}$ cannot reject Null hypothesis



\therefore We cannot reject Null hypothesis at the significant level of 0.05 where Parents’ education has no marginal contribution to the model

Using t-test for testing individually (Assume $\beta = 0$) $\alpha = 0.05$

Model 2.2: $bwght_i = \beta_0 + \beta_1cigs_i + \beta_2faminc_i + \beta_3fathereduc_i + \beta_4mothereduc_i + u_i$

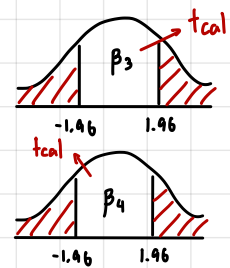
regress bwght cigs faminc fatheduc motheduc				
Source	SS	df	MS	
Model	15827.6593	4	3956.91482	Number of obs = 1191
Residual	466919.033	1186	393.69227	F(4, 1186) = 10.05
				Prob > F = 0.0000
				R-squared = 0.0328
				Adj R-squared = 0.0295
Total	482746.692	1190	405.669489	Root MSE = 19.842

bwght	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]
cigs	-.5894954	.1106172			
faminc	.0538254	.0366502			
fatheduc	.4936695	.2832896			
motheduc	-.4379234	.3197377			
_cons	118.0741	3.500291			

Omitted for the purpose of this exam.

Test $\hat{\beta}_3$; $t_{cal} = 0.4937 / 0.2833 = 1.7427$

Test $\hat{\beta}_4$; $t_{cal} = -0.4379 / 0.3197 = -1.3697$



$t_{lower} = t_{\frac{0.05}{2}}$ | $t_{lower} = -1.96$

$t_{upper} = t_{\frac{0.05}{2}}$ | $t_{upper} = 1.96$

\therefore we cannot reject Null hypothesis test or in other word we cannot say that Father and Mother education is significant at the level of 0.5

Question 3. A model of wage equation is given by

$$lwage_i = \beta_1 + \beta_2 exp_i + \beta_3 expsq_i + \beta_4 educ_i + \beta_5 age_i + \beta_6 kid6_i + \beta_7 kid18_i + u_i$$

where $lwage_i$ = natural log of hourly wage of married women
 exp_i = years of experience
 $expsq_i$ = years of experience squared
 $educ_i$ = years of education
 age_i = age
 $kid6_i$ = number of children aged 0-6 in a household
 $kid18_i$ = number of children aged 6-18 in a household

The regression result from OLS is shown in the table below and answer the following questions.

Source	SS	df	MS	Number of obs = 428		
Model	_____	_____	_____	F(____, _____)	=	13.19
Residual	_____	_____	.446526442	Prob > F	=	0.0000
				R-squared	=	0.1582
				Adj R-squared	=	_____
Total	223.327441	_____	_____	Root MSE	=	.66823

lwage	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]	
exper	.039819	.013393	2.97	0.003	.0134936	.0661444
expersq	-.0007812	.0004022	-1.94	0.053	-.0015718	9.37e-06
educ	.1078319	.0144021	7.49	0.000	.079523	.1361409
age	-.0014653	.0052925	-0.28	0.782	-.0118682	.0089377
kidslt6	-.0607106	.0887626	-0.68	0.494	-.2351836	.1137625
kidsge6	-.014591	.0278981	-0.52	0.601	-.069428	.0402459
_cons	-.4209078	.316905	-1.33	0.185	-1.043821	.2020053

- Figure out all the degrees of freedom in this model.
- Figure out all the sum of squares (ESS and RSS) and mean squares in this model.
- Figure out the adjusted R-squared (\bar{R}^2)
- Given that the model above is called 'Model 3.1', there is another competing model called 'Model 3.2' which an explanatory variable is excluded, compared to 'Model 3.1'. Though the result of estimating 'Model 3.2' is not shown here, what is the maximum value of R^2 from 'Model 3.2' which will make you conclude that the excluded variable has a significant contribution in 'Model 3.1', at the significance level of 0.05. (Hint: the critical value of the F-test at the significance level of 0.05 is $F_{1,421} = 3.84$)
- As you can see from the result, age is not significantly different from zero. In other words, age does not determine how much hourly wage would be. Does this make economic sense in your opinion? What do you think cause this insignificance?

a) Figure out all the degrees of freedom in this model.

model 3.1 included extended variables

$\frac{SS}{d.f.}$

Source	SS	df	MS
E Model	35.3304	6	5.8884
R Residual	187.9970	421	.446526442
T Total	223.327441	427	0.5230

Number of obs =	428
F(6, 421) =	13.19
Prob > F =	0.0000
R-squared =	0.1582
Adj R-squared =	0.1462
Root MSE =	.66823

lwage	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]
exper	.039819	.013393	2.97	0.003	.0134936 .0661444
expersq	-.0007812	.0004022	-1.94	0.053	-.0015718 9.37e-06
educ	.1078319	.0144021	7.49	0.000	.079523 .1361409
age	-.0014653	.0052925	-0.28	0.782	-.0118682 .0089377
kidslt6	-.0607106	.0887626	-0.68	0.494	-.2351836 .1137625
kidsge6	-.014591	.0278981	-0.52	0.601	-.069428 .0402459
_cons	-.4209078	.316905	-1.33	0.185	-1.043821 .2020053

$$d.f. \text{ model} = k - 1 = 7 - 1 = 6$$

$$d.f. \text{ Residual} = n - k = 428 - 7 = 421$$

b) Figure out all the sum of squares (ESS and RSS) and mean squares in this model.

$$R^2 = \frac{ESS}{TSS} \longrightarrow 0.1582 = \frac{ESS}{223.3274}$$

$$ESS = 35.3304 //$$

$$R^2 = 1 - \frac{RSS}{TSS} \longrightarrow 0.1582 = 1 - \frac{RSS}{223.3274}$$

$$RSS = 187.9970 //$$

$$MS = \frac{SS}{d.f.} \longrightarrow \frac{35.3304}{6} = 5.8884 // \text{ (Model)}$$

$$\longrightarrow \frac{223.3274}{427} = 0.5230 // \text{ (Residual)}$$

c) Figure out the adjusted R-squared (\bar{R}^2)

$$\bar{R}^2 = 1 - (1 - R^2) \frac{n-1}{n-k} \longrightarrow 1 - (1 - 0.1582) \left(\frac{428-1}{428-7} \right)$$

$$\bar{R}^2 = 0.1462 //$$

- d) Given that the model above is called 'Model 3.1', there is another competing model called 'Model 3.2' which an explanatory variable is excluded, compared to 'Model 3.1'. Though the result of estimating 'Model 3.2' is not shown here, what is the maximum value of R^2 from 'Model 3.2' which will make you conclude that the excluded variable has a significant contribution in 'Model 3.1', at the significance level of 0.05. (Hint: the critical value of the F-test at the significance level of 0.05 is $F_{1,421} = 3.84$)
- $k_{old} = k_{new} - 1 = 5$
- Find R^2_{old}

We estimate to whether add more variables in the model or not by using "Marginal Contribution"

H_0 : weighted has no marginal contribution to the model

H_a : Otherwise

$$F_{cal} = \frac{R^2_{new} - R^2_{old} / (\# \text{ new regressor})}{1 - R^2_{new} / (n - k_{new})} \quad \left| \quad F_{cri} (1, n-3) = F_{cri} (1, 425) \right.$$

$$\alpha = 0.05 \quad \left. \begin{matrix} = F_{cri} (1, 425) \\ d = 0.05 \\ = 3.84 \end{matrix} \right.$$

To maximize R^2 is $F_{cal} = F_{cri}$

$$3.84 = \frac{0.1582 - R^2_{old} / 6 - 5}{1 - 0.1582 / 428 - 6}$$

$$0.0077 = 0.1582 - R^2_{old}$$

$$R^2_{old} = 0.1505$$

∴ The maximum R^2 of model 3.2 is 0.1505

model 3.1 included extended variables

SS
d.f.

Source	SS	df	MS
E Model	35.3304	6	5.8884
R Residual	187.9970	421	.446526442
T Total	223.327441	427	0.5230

Number of obs =	428
F(6 , 421) =	13.19
Prob > F =	0.0000
R-squared =	0.1582
Adj R-squared =	0.1462
Root MSE =	.66823

R_{new}

lwage	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]
exper	.039819	.013393	2.97	0.003	.0134936 .0661444
expersq	-.0007812	.0004022	-1.94	0.053	-.0015718 9.37e-06
educ	.1078319	.0144021	7.49	0.000	.079523 .1361409
age	-.0014653	.0052925	-0.28	0.782	-.0118682 .0089377
kidslt6	-.0607106	.0887626	-0.68	0.494	-.2351836 .1137625
kidsge6	-.014591	.0278981	-0.52	0.601	-.069428 .0402459
_cons	-.4209078	.316905	-1.33	0.185	-1.043821 .2020053

TABLE D.3 Upper Percentage Points of the *F* Distribution (Continued)

df for denominator N_2	df for numerator N_1												
	Pr	1	2	3	4	5	6	7	8	9	10	11	12
22	.25	1.40	1.48	1.47	1.45	1.44	1.42	1.41	1.40	1.39	1.39	1.38	1.37
	.10	2.95	2.56	2.35	2.22	2.13	2.06	2.01	1.97	1.93	1.90	1.88	1.86
	.05	4.30	3.44	3.05	2.82	2.66	2.55	2.46	2.40	2.34	2.30	2.26	2.23
	.01	7.95	5.72	4.82	4.31	3.99	3.76	3.59	3.45	3.35	3.26	3.18	3.12
24	.25	1.39	1.47	1.46	1.44	1.43	1.41	1.40	1.39	1.38	1.38	1.37	1.36
	.10	2.93	2.54	2.33	2.19	2.10	2.04	1.98	1.94	1.91	1.88	1.85	1.83
	.05	4.26	3.40	3.01	2.78	2.62	2.51	2.42	2.36	2.30	2.25	2.21	2.18
	.01	7.82	5.61	4.72	4.22	3.90	3.67	3.50	3.36	3.26	3.17	3.09	3.03
26	.25	1.38	1.46	1.45	1.44	1.42	1.41	1.39	1.38	1.37	1.37	1.36	1.35
	.10	2.91	2.52	2.31	2.17	2.08	2.01	1.96	1.92	1.88	1.86	1.84	1.81
	.05	4.23	3.37	2.98	2.74	2.59	2.47	2.39	2.32	2.27	2.22	2.18	2.15
	.01	7.72	5.53	4.64	4.14	3.82	3.59	3.42	3.29	3.18	3.09	3.02	2.96
28	.25	1.38	1.46	1.45	1.43	1.41	1.40	1.39	1.38	1.37	1.36	1.35	1.34
	.10	2.89	2.50	2.29	2.16	2.06	2.00	1.94	1.90	1.87	1.84	1.81	1.79
	.05	4.20	3.34	2.95	2.71	2.56	2.45	2.36	2.29	2.24	2.19	2.15	2.12
	.01	7.64	5.45	4.57	4.07	3.75	3.53	3.36	3.23	3.12	3.03	2.96	2.90
30	.25	1.38	1.45	1.44	1.42	1.41	1.39	1.38	1.37	1.36	1.35	1.35	1.34
	.10	2.88	2.49	2.28	2.14	2.05	1.98	1.93	1.88	1.85	1.82	1.79	1.77
	.05	4.17	3.32	2.92	2.69	2.53	2.42	2.33	2.27	2.21	2.16	2.13	2.09
	.01	7.56	5.39	4.51	4.02	3.70	3.47	3.30	3.17	3.07	2.98	2.91	2.84
40	.25	1.36	1.44	1.42	1.40	1.39	1.37	1.36	1.35	1.34	1.33	1.32	1.31
	.10	2.84	2.44	2.23	2.09	2.00	1.93	1.87	1.83	1.79	1.76	1.73	1.71
	.05	4.08	3.23	2.84	2.61	2.45	2.34	2.25	2.18	2.12	2.08	2.04	2.00
	.01	7.31	5.18	4.31	3.83	3.51	3.29	3.12	2.99	2.89	2.80	2.73	2.66
60	.25	1.35	1.42	1.41	1.38	1.37	1.35	1.33	1.32	1.31	1.30	1.29	1.29
	.10	2.79	2.39	2.18	2.04	1.95	1.87	1.82	1.77	1.74	1.71	1.68	1.66
	.05	4.00	3.15	2.76	2.53	2.37	2.25	2.17	2.10	2.04	1.99	1.95	1.92
	.01	7.08	4.98	4.13	3.65	3.34	3.12	2.95	2.82	2.72	2.63	2.56	2.50
120	.25	1.34	1.40	1.39	1.37	1.35	1.33	1.31	1.30	1.29	1.28	1.27	1.26
	.10	2.75	2.35	2.13	1.99	1.90	1.82	1.77	1.72	1.68	1.65	1.62	1.60
	.05	3.92	3.07	2.68	2.45	2.29	2.17	2.09	2.02	1.96	1.91	1.87	1.83
	.01	6.85	4.79	3.95	3.48	3.17	2.96	2.79	2.66	2.56	2.47	2.40	2.34
200	.25	1.33	1.39	1.38	1.36	1.34	1.32	1.31	1.29	1.28	1.27	1.26	1.25
	.10	2.73	2.33	2.11	1.97	1.88	1.80	1.75	1.70	1.66	1.63	1.60	1.57
	.05	3.89	3.04	2.65	2.42	2.26	2.14	2.06	1.98	1.93	1.88	1.84	1.80
	.01	6.76	4.71	3.88	3.41	3.11	2.89	2.73	2.60	2.50	2.41	2.34	2.27
∞	.25	1.32	1.39	1.37	1.35	1.33	1.31	1.29	1.28	1.27	1.25	1.24	1.24
	.10	2.71	2.30	2.08	1.94	1.85	1.77	1.72	1.67	1.63	1.60	1.57	1.55
	.05	3.84	3.00	2.60	2.37	2.21	2.10	2.01	1.94	1.88	1.83	1.79	1.75
	.01	6.63	4.61	3.78	3.32	3.02	2.80	2.64	2.51	2.41	2.32	2.25	2.18

e) As you can see from the result, age is not significantly different from zero. In other words, age does not determine how much hourly wage would be. Does this make economic sense in your opinion? What do you think cause this insignificance?

In the economics, this making sense that the effect the hourly wage cannot say that age determined on that part since there are many ways to earn more money that the age doesn't really matter.