

CAPM-FF

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Nested Models

$$Y_i = \beta_1 + \beta_2 X_{2i} + \beta_3 X_{3i} + \beta_4 X_{4i} + u_i \quad (1)$$

$$Y_i = \beta_1 + \beta_2 X_{2i} + \beta_4 X_{4i} + u_i \quad (2)$$

(1) & (2) are nested models.

$$Y_i = \beta_1 + \beta_2 X_{2i} + \beta_5 X_{5i} + \beta_6 X_{6i} + u_i \quad (3)$$

(3) isn't nested to (1) & (2)

CAPM $(r_j - r_f) = \alpha + \beta(r_m - r_f) + u_t$

$$Y_t = \alpha + \beta_1 X_{1t} + u_t$$

FF $(r_j - r_f) = \alpha + \beta_1(r_m - r_f) + \beta_2 \text{SMB} + \beta_3 \text{HML} + u_t$

$$Y_t = \alpha + \beta_1 X_{1t} + \beta_2 X_{2t} + \beta_3 X_{3t} + u_t$$

Test CAPM vs FF

$$H_0 : \beta_2 = \beta_3 = 0 \quad \text{or} \quad \beta_2 = 0 \quad \text{and} \quad \beta_3 = 0$$

Residual SS
 OLS
 ↓
 Min $\sum \hat{u}_t^2$
 RSS

Unrestricted Model FF: $RSS_{UR} \quad Y_t = \alpha + \beta_1 X_{1t} + \beta_2 X_{2t} + \beta_3 X_{3t} + u_t$

Restricted Model CAPM: $RSS_R \quad Y_t = \alpha + \beta_1 X_{1t} + u_t$

$$\frac{RSS_R - RSS_{UR} / m = 2}{RSS_{UR} / n - k} \sim F_{(m, n-k)}$$

$$RSS_{UR} / n - k$$

(m, n-k)

$\sim \chi^2_{(n-k)}$

UR FF $Y_t = \alpha + \beta_1 X_{1t} + \beta_2 X_{2t} + \beta_3 X_{3t} + u_t$

Overall Test

$H_0: \beta_1 = \beta_2 = \beta_3 = 0$

R $Y_t = \alpha + u_t$ RSS

$$TSS = \sum (Y_t - \bar{Y})^2 = \sum u_t^2$$

$$F = \frac{RSS_R - RSS_{UR} / (m-3) (k-1)}{RSS_{UR} / n - k}$$

Overall $F = \frac{ESS / k - 1}{RSS / n - k}$

