

Example 2.I: A monopolist firm faces the market demand given by $P = 10 - Q$. Consider the following questions if the cost function $C(Q) = 4Q$.

- What is the revenue-maximizing level of output?

$$\begin{aligned}
 R(Q) &: \text{price per unit} \times \text{unit of output} \\
 & \quad P \quad \times \quad Q \\
 &= (10 - Q)Q \\
 &= 10Q - Q^2 \quad ; \text{ revenue f}^n \text{ is "quadratic function"} \\
 &= \frac{-b}{2a} \rightarrow Q \quad \left| \begin{array}{l} = R(Q) \\ = 10(5) - (5)^2 \\ = 50 - 25 = 25 \# \end{array} \right. \\
 &= \frac{-10}{2(-1)} = 5
 \end{aligned}$$

- What is the break-even output?

$$\begin{aligned}
 (\pi &= 0) \\
 \pi &= R - C \\
 &= (10Q - Q^2) - (4Q) \\
 &= 10Q - Q^2 - 4Q = 0 \quad \left| \begin{array}{l} Q : 0, 6 \# \\ 6Q - Q^2 = 0 \\ Q(6 - Q) = 0 \end{array} \right.
 \end{aligned}$$

- What is the profit-maximizing level of output?

$$\begin{aligned}
 \pi(Q) &= 6Q - Q^2 \\
 a &= -1 ; b = 6, c = 0 \\
 (Q) &: \frac{-b}{2a} \rightarrow \frac{-6}{2(-1)} = 3 \text{ unit} \quad \left| \begin{array}{l} \text{Maximizing profit} : \pi(3) \\ = 6(3) - 3^2 \\ = 9 \end{array} \right.
 \end{aligned}$$