

Quiz 5

1. Find

$$\int \frac{3x}{e^{4x}} dx.$$

Solution: Consider $\int \frac{3x}{e^{4x}} dx = \int 3xe^{-4x} dx$. Integration by parts:

- Let $u = 3x$ and $dv = e^{-4x} dx$.
- Then $du = 3dx$ and
- $v = \int e^{-4x} dx = \int e^{-4x} \frac{d(-4x)}{-4} = \frac{e^{-4x}}{-4} + C$. By setting $C = 0 \Rightarrow v = \frac{e^{-4x}}{-4}$.

$$\begin{aligned} \int \frac{3x}{e^{4x}} dx &= \int 3xe^{-4x} dx = uv - \int v du \\ &= (3x) \left[\frac{e^{-4x}}{-4} \right] - \int \frac{e^{-4x}}{-4} 3dx \\ &= -\frac{3}{4}xe^{-4x} + \frac{3}{4} \int e^{-4x} dx \\ &= -\frac{3}{4}xe^{-4x} + \frac{3}{4} \int e^{-4x} \frac{d(-4x)}{-4} \\ &= -\frac{3}{4}xe^{-4x} + \frac{3}{4} \left[\frac{e^{-4x}}{-4} \right] + C \\ &= -\frac{3}{4}xe^{-4x} - \frac{3}{16}e^{-4x} + C \end{aligned}$$

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