

1. Table 9.1 Public school teachers' salaries (Dollars) by geographical region. Consider and estimate the following model with the dummy variable:

$$Y_i = \beta_1 + \beta_2 D_{2i} + \beta_3 D_{3i} + u_i$$

Where Y = (average) salary of public school teacher in state i

$$D_{2i} = 1 \text{ if the state is in the Northeast or North Central} \\ = 0 \text{ otherwise}$$

$$D_{3i} = 1 \text{ if the state is in the South} \\ = 0 \text{ otherwise}$$

t = time

$$D = 1 \text{ for observations in 1970-1981} \\ = 0 \text{ otherwise}$$

Find the mean salary of public school teacher in the South and the mean salary of public school teacher in the Northeast or North Central.

## 2. The Use of Dummy Variables in Seasonal Analysis

Table 9.4 U.S. Refrigerator Sales (thousands), 1978-1985 (quarterly)

- a. Consider and estimate the following model with the dummy variable:

$$Y_t = \beta_1 D_{1t} + \beta_2 D_{2t} + \beta_3 D_{3t} + \beta_4 D_{4t} + u_t$$

Where Y = refrigerator sales, thousands

$$D_{1t} = 1 \text{ if in the First quarter} \\ = 0 \text{ otherwise}$$

$$D_{2t} = 1 \text{ if in the Second quarter} \\ = 0 \text{ otherwise}$$

$$D_{3t} = 1 \text{ if in the Third quarter} \\ = 0 \text{ otherwise}$$

$$D_{4t} = 1 \text{ if in the Fourth quarter} \\ = 0 \text{ otherwise}$$

t = time

- b. Instead of assigning a dummy for each quarter and suppressing the intercept term to avoid the dummy variable trap, what should we do?
  - c. Since the models a. and b. do not contain any covariates, will the picture change if we bring in a quantitative regressor in the model?
3. Table 8.9 Savings and Personal Disposable income (billions of dollars), United States, 1970-1995.

- a. Given the data in the table, estimate the following linear savings function using personal disposable income

$$\text{Time period 1970-1981: } Y_t = \lambda_1 + \lambda_2 X_t + u_{1t} \quad n_1 = 12$$

$$\text{Time period 1982-1995: } Y_t = \gamma_1 + \gamma_2 X_t + u_{2t} \quad n_2 = 14$$

$$\text{Time period 1970-1995: } Y_t = \alpha_1 + \alpha_2 X_t + u_{3t} \quad n_1 + n_2 = 26$$

- b. On the basis of the Chow test that there was a difference in the regression of savings on income between the two periods. Consider and estimate the following model with the dummy variable:

$$Y_t = \alpha_1 + \alpha_2 D_t + \beta_1 X_t + \beta_2 (D_t X_t) + u_t$$

Where Y = Savings

X = Personal disposable income

t = time

D = 1 for observations in 1982-1995

= 0 otherwise

- i. Test the coefficients individually statistically significant at the 5 percent level? From this test, how would you describe the difference in the two regressions (coincident regression, parallel regression, concurrent regression, dissimilar regression)?
  - ii. Write down the mean personal savings function for 1970-1981 and the mean personal savings function for 1982-2005.
4. Table 10.5 Hypothetical Data on Consumption Expenditure in Relation to Income and Wealth. Consider and estimate the following model:

$$Y_i = \beta_1 + \beta_2 X_{2i} + \beta_3 X_{3i}$$

Where

$Y_i = \text{Consumption Expenditure}(\$)$

$X_{2i} = \text{Income}(\$)$

$X_{3i} = \text{Wealth}(\$)$

- i. Estimate the parameters of this model using the data
- ii. Do you expect to face the multicollinearity problem? Why?
- iii. If you do expect to face the multicollinearity problem, how will you go about resolving the problem?