

## CHAPTER 3

### Static and Comparative Static Equilibrium Analysis

#### Topics: Static and Comparative Static Equilibrium Analysis, PART1

##### Outline:

- Linear models in economics
- Simultaneous system of equations
- \* A partial-equilibrium market model: A model of price determination in an isolated market
- \* Excise Tax and Market Equilibrium
- What is elasticity ? How can we derive elasticity?
- \* Tax incidence and Elasticity

“Equilibrium” means

→ a situation that selected interrelated variables so adjusted to one another that **no tendency to change**

→ All variables in the model must be simultaneously endogenous in a state of rest

“Static” means

statics = equilibrium

Nongoal type of equilibrium: ⇒ Ch3, Ch4, Ch6, 8

use matrix to solve equilibrium optimization

goal-type equilibrium

↳ The equilibrium that is not a result of any particular objective, but is derived from an impersonal process of interaction

⇒ we could have underemployment equilibrium level of national income

Linear economic model vs. Nonlinear economic model

→ $Q^D = Q^S$	① ② ③	$Q^D = Q^S$
→ $Q^D = a - bp$		$Q^D = a - bp^2$
→ $Q^S = -c + dp$		$Q^S = -c + dp^2$

“Simultaneous system of equations” means

system of equations in which each equation is considered to be related

→ e.g. finding equilibrium = finding solution to the system of equations  
The solution to system of equations must make every equations true simultaneously

### 3.1

#### A partial-equilibrium market model: A model of price determination in an isolated market

Suppose we are interested in one commodity, energy drink. Since only one commodity is being considered, the economic model for this market is comprised of:

1.  $Q^d$
2.  $Q^s$
3.  $P$

After having chosen the variables, we next make certain assumptions regarding the working of the market. First, we must specify an equilibrium condition- something indispensable in an equilibrium model. The standard assumption is that equilibrium occurs in the market if and only if the excess demand is zero, that is, if and only if the market is cleared. The Clearing Market Condition can be written as:

$$Q^D = Q^S$$

to note:  $p^d = p^s$  (1)

Equation (1.) is conditional equation of the market. The model requires that we specify behavioral equations to explain how exactly the demand and supply are each determined.

use (\*) (\*)

**Demand for energy drink**

We assume that  $Q_d$  is a decreasing linear function of  $P$ .

$$Q^D = a - bP, \quad b > 0 \quad \text{--- (*)}$$

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to solve for  
 $Q^*, P^*$   
 $Q^D = Q^S$   
indicate  
(2) restriction on  
such that  $a, b, c, d$   
 $Q^*, P^*$  can  
happen  
↑

**Supply for energy drink**

We assume that  $Q_s$  is an increasing linear function of  $P$ .

$$Q^S = -c + dP, \quad d > 0, \quad c > 0 \quad (*)$$

(3)

In all, the model will contain one equilibrium condition plus two behavioral equations which govern the demand and supply sides of the market.

$$\begin{aligned} Q_d = Q_s &\Rightarrow 1 \text{ Conditional equation} \\ \left. \begin{aligned} Q_d = a - bP \quad (a, b > 0) \\ Q_s = -c + dP \end{aligned} \right\} & 2 \text{ Behavioral equations} \end{aligned} \quad (4)$$

The next step is to obtain the solution values of the three endogenous variables, \_\_\_\_\_.

The solution values are those values that satisfy the three equations in (4) simultaneously.

We usually denote the solution value of an endogenous variable with an asterisk. Thus, the solution values of  $Q_d, Q_s, P$  are denoted by \_\_\_\_\_.

Since  $Q_d^* = Q_s^*$ , they can be replaced by a single symbol  $Q^*$ .

Hence, an equilibrium solution of the model may simply be denoted by an ordered pair \_\_\_\_\_.

Solution by Elimination of Variables:

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Additional restriction for an economically meaningful solution:

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Note: Compare between partial equilibrium and general equilibrium model

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### 3.2

#### Excise Tax and Market Equilibrium

We will use a partial-equilibrium market model from previous section in an analysis of the impact of excise tax.

Definition of an excise tax:

**Excise taxes** are narrowly based taxes on consumption, levied on specific goods, services, and activities. They can be either a per unit tax (such as the per gallon tax on gasoline) or a percentage of price (such as the airline ticket tax). Generally, excise taxes are collected from producers or wholesalers, and are embedded in the price paid by final consumers.

(a.) **Specific Tax** or per unit tax or unit tax: is a tax that is defined as a fixed amount for each unit of a good or service sold, such as cents per kilogram.

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(b.) **Ad Valorem Tax** is a tax whose amount is based on the value of a transaction or of property. It is a charge based on a fixed percentage of the product value. It is typically imposed at the time of a transaction, as in the case of a sale or value-added tax (VAT).

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Tax can be collected from buyers or producers, depending on convenience and efficacy of tax collection. Either way, market equilibrium will change. We can compare *market equilibrium before tax to market equilibrium after tax*, and analyze how the change is. This is called “Comparative Static Analysis”.

**Comparative statics**, as the name suggested, is concerned with the comparison of different equilibrium states that are associated with different sets of values of parameters and exogeneous variables.

### CASE 1: Specific tax

Collect tax  $t$  baht per unit of energy drink, e.g.  $t$  baht per bottle

#### CASE 1.1: Collect from producers/suppliers



Market equilibrium before tax

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Market equilibrium after tax

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Tax revenue is equal to:

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Tax burden on consumers/buyers

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Tax burden on producers/sellers

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**CASE 1.2: Collect from consumers/buyers**



Market equilibrium before tax

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Market equilibrium after tax

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Tax revenue is equal to:

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Tax burden on consumers/buyers

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Tax burden on producers/sellers

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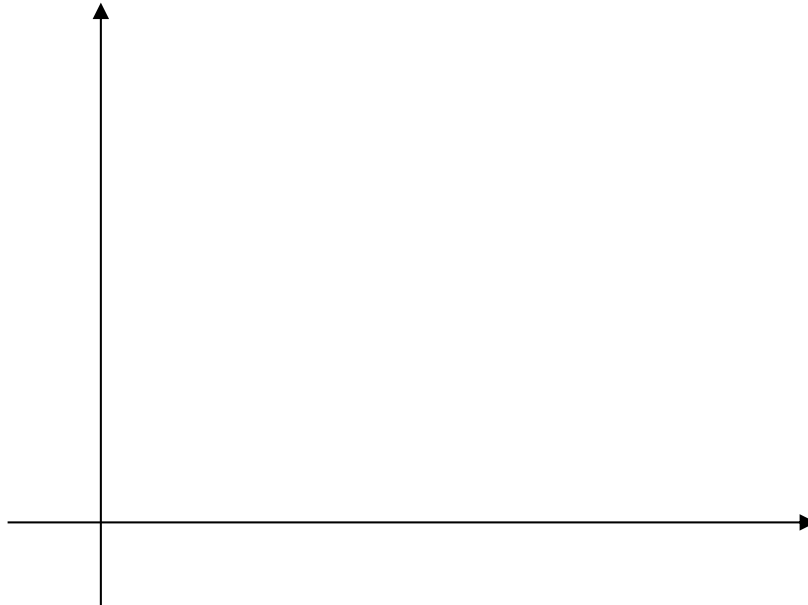
*OBSERVATION:*

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**CASE 2: Ad Valorem tax**

Collect tax  $t\%$  of price, e.g. 7% of price per bottle

**CASE 2.1: Collect from producers/suppliers**



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Market equilibrium after tax

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Tax revenue is equal to:

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Tax burden on consumers/buyers

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Tax burden on producers/sellers

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**CASE 2.2: Collect from consumers/buyers**



Market equilibrium before tax

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Market equilibrium after tax

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Tax revenue is equal to:

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Tax burden on consumers/buyers

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Tax burden on producers/sellers

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*OBSERVATION:*

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Tax incidence (or incidence of tax) is an economic term for understanding the division of a tax burden between buyers and sellers or producers and consumers.

Tax incidence is related to the price elasticity of supply and demand. When supply is more elastic than demand, the tax burden falls on the buyers. If demand is more elastic than supply, producers will bear the cost of the tax.

**Digression**

**What is elasticity ? How can we derive elasticity?**

From linear demand function in (2):

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With  $P$  on Y-axis and  $Q$  on x-axis, the inverse demand function is:

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From linear supply function in (3):

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The inverse supply function is:

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$-b$  is

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$-d$  is

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To be able to compare how responsive of change in quantity to change in price across different commodities, the concept of “elasticity” comes in handy.

**Elasticity** is the measurement of the percentage change of one economic variable in response to one percentage change in another.

(4)

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The price elasticity of demand is:

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The price elasticity of supply is:

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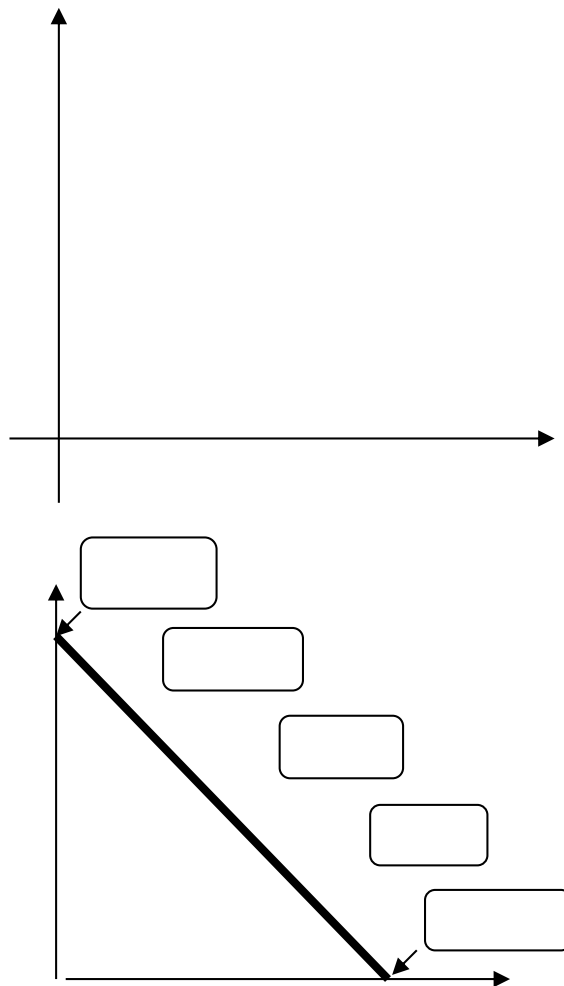
Inelastic vs. Elastic vs. Unit elastic

$$E_p < 1$$

$$E_p > 1$$

$$E_p = 1$$

Price Elasticity of Demand at different point on inverse demand function:

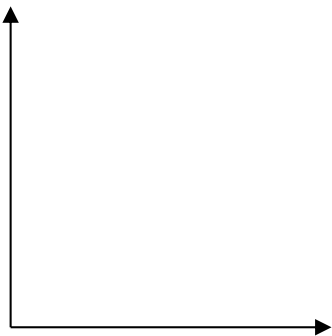
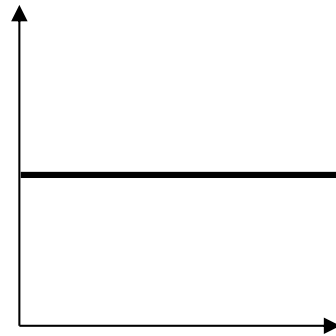
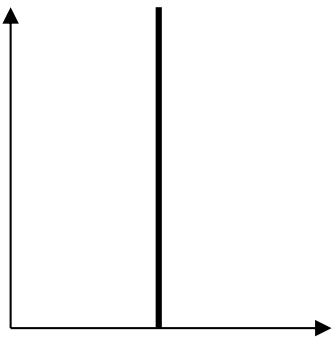


The price elasticity of demand at each point of linear demand function, with negative slope, is not equal to other point. This is because:

$$\frac{P}{Q}$$

$$\frac{\Delta Q}{\Delta P} = -b$$

In which case are the price elasticities of demand for different points equal?



### Tax incidence and Elasticity

Whoever cannot adjust themselves instantaneously to change in price will have to bear a larger portion of the tax burden.

