

HW Given  $y = 10 + \sqrt{x}$ ,

- a) Find the derivative  $f'(x)$ .  $\rightarrow \frac{1}{2\sqrt{x}}$   
 b) Fill in the table

Point	X	Y	$f'(x)$
	0	10	Undefined
A	1	11	$\frac{1}{2}$
B	2	11.414	$\frac{1}{2\sqrt{2}}$
C	3	11.732	$\frac{1}{\sqrt{3}}$



- c) Does the slope increase as  $x$  increases?  $\rightarrow$  when  $x$  increase slope is decrease  
 d) Approximate the change in  $Y$  when  $\Delta x = 0.2$  at  $x_1 = 3$ . Is the approximation under- or over-estimate?

$$\Delta Y \approx \frac{1}{2\sqrt{x}} \cdot (0.2) = \frac{\sqrt{3}}{30} = 0.05773502692 \quad \Delta Y = Y_2 - Y_1 = 11.78885438 - 11.732 = 0.056854382$$

Note: If the function  $f(x)$  is linear, the approximation is exact.

$0.057 > 0.056$	
↓	↓
Estimate	Real

Thus, we Overestimate the real change of  $y$

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