

1.1

No. Because, there are 3 endogenous variables, but the question only provides us 2 equations. Therefore we need one more equation which is an equilibrium condition, $Y = C + I$.

1.2

$$\begin{aligned} Y - C - I &= 0 \\ C - 0.3Y &= C_0 - k_1r \\ I - 0.2Y &= I_0 - k_2r \end{aligned}$$

$$\begin{bmatrix} 1 & -1 & -1 \\ -0.3 & 1 & 0 \\ -0.2 & 0 & 1 \end{bmatrix} \begin{bmatrix} Y \\ C \\ I \end{bmatrix} = \begin{bmatrix} 0 \\ C_0 - k_1r \\ I_0 - k_2r \end{bmatrix}$$

1.3

The solution is unique when $\det(A) \neq 0$.

$$\begin{vmatrix} 1 & -1 & -1 \\ -0.3 & 1 & 0 \\ -0.2 & 0 & 1 \end{vmatrix} = 1 + 0 + 0 - 0.2 - 0.3 = 1 - 0.5 = 0.5$$

1.4

$$\begin{aligned} C &= \frac{\begin{vmatrix} 1 & 0 & -1 \\ -0.3 & C_0 - k_1r & 0 \\ -0.2 & I_0 - k_2r & 1 \end{vmatrix}}{\det(A)} \\ &= \frac{(C_0 - k_1r) + 0.3(I_0 - k_2r) - 0.2(C_0 - k_1r)}{0.5} \\ &= \frac{0.8(C_0 - k_1r) + 0.3(I_0 - k_2r)}{0.5} \\ &= 1.6(C_0 - k_1r) + 0.6(I_0 - k_2r) \end{aligned}$$