

## Assignment 7

1. Test whether there exists significant ARCH effects.

```
. reg rfuture rspot if t>1
```

| Source   | SS         | df    | MS         | Number of obs | = | 7,683   |
|----------|------------|-------|------------|---------------|---|---------|
| Model    | .01531231  | 1     | .01531231  | F(1, 7681)    | = | 6787.70 |
| Residual | .017327485 | 7,681 | 2.2559e-06 | Prob > F      | = | 0.0000  |
|          |            |       |            | R-squared     | = | 0.4691  |
|          |            |       |            | Adj R-squared | = | 0.4691  |
| Total    | .032639795 | 7,682 | 4.2489e-06 | Root MSE      | = | .0015   |

| rfuture | Coef.    | Std. Err. | t     | P> t  | [95% Conf. Interval] |          |
|---------|----------|-----------|-------|-------|----------------------|----------|
| rspot   | .7889924 | .0095766  | 82.39 | 0.000 | .7702196             | .8077651 |
| _cons   | 7.58e-06 | .0000171  | 0.44  | 0.658 | -.000026             | .0000412 |

```
. estat archlm
```

LM test for autoregressive conditional heteroskedasticity (ARCH)

| lags(p) | chi2  | df | Prob > chi2 |
|---------|-------|----|-------------|
| 1       | 6.951 | 1  | 0.0084      |

H0: no ARCH effects vs. H1: ARCH(p) disturbance

From running ARCH effect test, it shows us that Prob>Chi2 is 0.0084 which is less than 0.05 significant level. Thus, we reject the H<sub>0</sub>: no ARCH effects. There is an ARCH.

2. Estimate GARCH(p,q) for spot return (rspot) using future return (rfuture) as explanatory variable for mean equation – determine the most appropriated order p and q for variance equation using SBIC given the maximum lag equals to 2.

```
. reg rspot rfuture if t>1
```

| Source   | SS         | df    | MS         | Number of obs | = | 7,683   |
|----------|------------|-------|------------|---------------|---|---------|
| Model    | .011539538 | 1     | .011539538 | F(1, 7681)    | = | 6787.70 |
| Residual | .013058198 | 7,681 | 1.7001e-06 | Prob > F      | = | 0.0000  |
|          |            |       |            | R-squared     | = | 0.4691  |
|          |            |       |            | Adj R-squared | = | 0.4691  |
| Total    | .024597736 | 7,682 | 3.2020e-06 | Root MSE      | = | .0013   |

| rspot   | Coef.    | Std. Err. | t     | P> t  | [95% Conf. Interval] |          |
|---------|----------|-----------|-------|-------|----------------------|----------|
| rfuture | .594594  | .007217   | 82.39 | 0.000 | .5804466             | .6087413 |
| _cons   | 8.01e-06 | .0000149  | 0.54  | 0.590 | -.0000212            | .0000372 |

```
. est store ols

. est table ols arch*, star(0.1 0.05 0.01) stat(N rss LL F chi2 aic bic)
```

| Variable   | ols          | arch1        | arch2        |
|------------|--------------|--------------|--------------|
| rfuture    | .59459397*** |              |              |
| _cons      | 8.007e-06    |              |              |
| rfuture    |              |              |              |
| rspot      |              | .81227442*** | .83565658*** |
| _cons      |              | -1.776e-06   | -.00001465   |
| ARCH       |              |              |              |
| arch       |              |              |              |
| L1.        |              | .23368968*** | .24680333*** |
| L2.        |              |              | .19149974*** |
| _cons      |              | 1.839e-06*** | 1.497e-06*** |
| Statistics |              |              |              |
| N          | 7683         | 7683         | 7683         |
| rss        | .0130582     |              |              |
| LL         |              |              |              |
| F          | 6787.7049    |              |              |
| chi2       |              | 110868.99    | 108339.96    |
| aic        | -80262.049   | -78428.289   | -78693.691   |
| bic        | -80248.155   | -78400.502   | -78658.957   |

legend: \* p<.1; \*\* p<.05; \*\*\* p<.01

```
. est table garch*, star(0.1 0.05 0.01) stat(N LL chi2 aic bic)
```

| Variable   | garch11      | garch21       | garch12      | garch22      |
|------------|--------------|---------------|--------------|--------------|
| rspot      |              |               |              |              |
| rfuture    | .64717084*** | .64002048***  | .62591038*** | .62371083*** |
| _cons      | 6.460e-07    | -2.531e-06    | -8.750e-06   | -.00001062   |
| ARCH       |              |               |              |              |
| arch       |              |               |              |              |
| L1.        | .18339114*** | .17044696***  | .10390572*** | .10141532*** |
| L2.        |              |               | .23783658*** | .29885683*** |
| garch      |              |               |              |              |
| L1.        | .60659952*** | .84899371***  | .34036795*** | .07659108*** |
| L2.        |              | -.20697486*** |              | .17715968*** |
| _cons      | 3.858e-07*** | 3.503e-07***  | 6.225e-07*** | 6.862e-07*** |
| Statistics |              |               |              |              |
| N          | 7683         | 7683          | 7683         | 7683         |
| LL         |              |               |              |              |
| chi2       | 126854.57    | 131273.47     | 127297.52    | 120955.35    |
| aic        | -81027.53    | -81061.507    | -81150.803   | -81192.527   |
| bic        | -80992.796   | -81019.826    | -81109.122   | -81143.899   |

legend: \* p<.1; \*\* p<.05; \*\*\* p<.01

```
//Estimate ARCH(q) using MLE
qui arch rfuture rspot, arch(1) nolog
est store arch1
qui arch rfuture rspot, arch(1/2) nolog
est store arch2
est table ols arch*, star(0.1 0.05 0.01) stat(N rss LL F chi2 aic bic)

//Estimate GARCH(p,q) using MLE
qui arch rspot rfuture, arch(1) garch(1) nolog
est store garch11
qui arch rspot rfuture, arch(1) garch(1/2) nolog
est store garch21
qui arch rspot rfuture, arch(1/2) garch(1) nolog
est store garch12
qui arch rspot rfuture, arch(1/2) garch(1/2) nolog
est store garch22
est table garch*, star(0.1 0.05 0.01) stat(N LL chi2 aic bic)
```

From GARCH table on the left, the model with the lowest BIC or SBIC (-81143.899), with the maximum lag equals to 2, is GARCH(2, 2). Thus, the most appropriated order of p, and q is 2 and 2, respectively.

3. From (2), predict the variance of future return (rfuture).

```
//Forecast using GARCH(2,2)
arch rspot rfuture, arch(1/2) garch(1/2) nolog
predict sigma2, variance
line sigma2 t
```

