

# CHAPTER 10

## Credit Risk: Individual Loan Risk



# Overview

- This chapter discusses types and characteristics of loans made by U.S. FIs, models for measuring credit risk, and applicable technological advances.
- Important for purposes of:
  - Pricing loans and bonds
  - Setting limits on credit risk exposure

# Credit Quality Problems

- Problems with junk bonds, LDC loans, and residential and farm mortgage loans
- Late 1990s, credit card and auto loans
- Crises in other countries such as Argentina, Brazil, Russia, and South Korea
- 2006-2007, mortgage delinquencies on subprime loans surged
- Emphasizes importance credit risk analysis

# Web Resources

- For further information on credit ratings visit:

Moody's

[www.moody's.com](http://www.moody's.com)

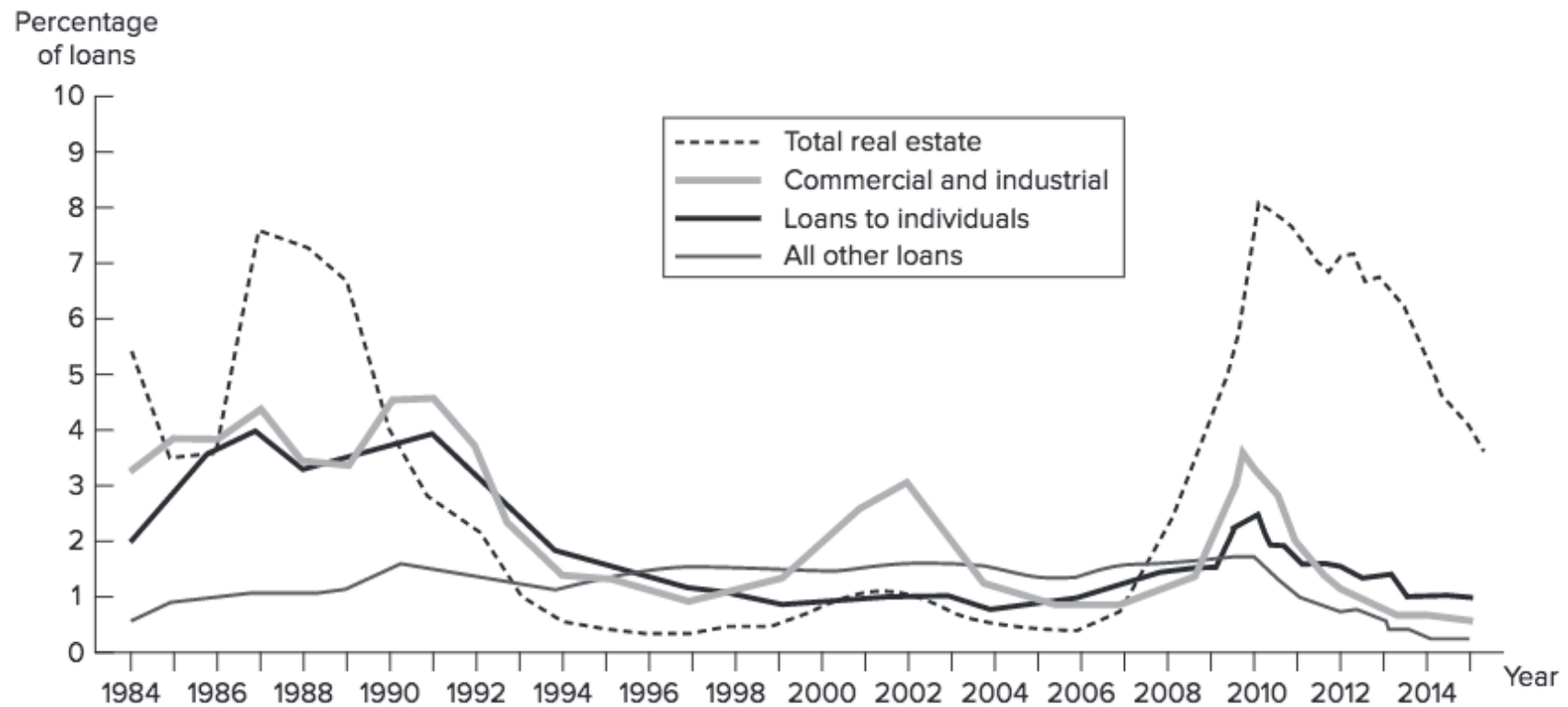
Standard & Poor's

[www.standardandpoors.com](http://www.standardandpoors.com)

# Credit Quality Problems Continued

- Over the early to mid 1990s, improvements in NPLs for large banks and overall credit quality
- Late 1990s and early 2000, Telecommunication and tech companies
- Mid 2000s, economic growth accompanied by reduction in NPL rates
- Mortgage crisis
- Increased emphasis on credit risk evaluation

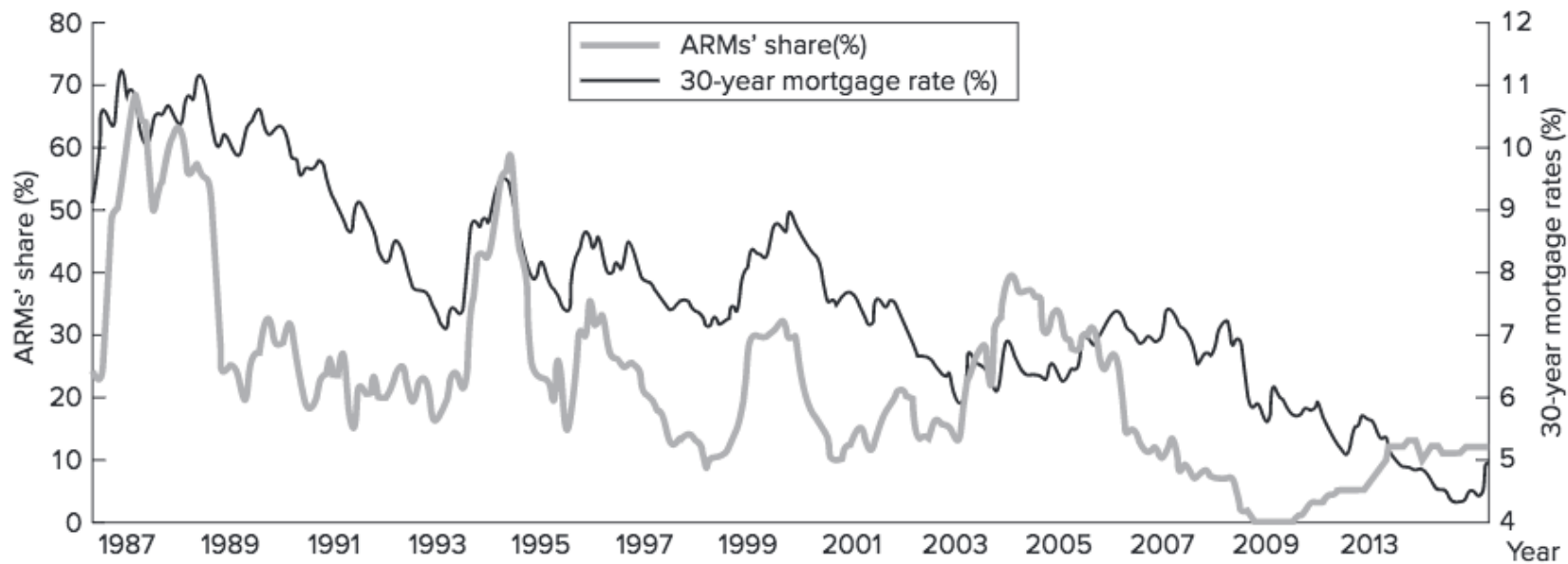
# Nonperforming Asset Ratio for U.S. Commercial Banks



# Types of Loans

- C&I loans: secured and unsecured
  - Syndication
  - Spot loans, loan commitments
  - Decline in C&I loans originated by commercial banks and growth in commercial paper market
  - Effect of financial crisis on commercial paper market
- RE loans: Primarily mortgages
  - Fixed-rate, ARMs
  - Mortgages can be subject to default risk when loan-to-value rises and house prices fall below amount of loan outstanding

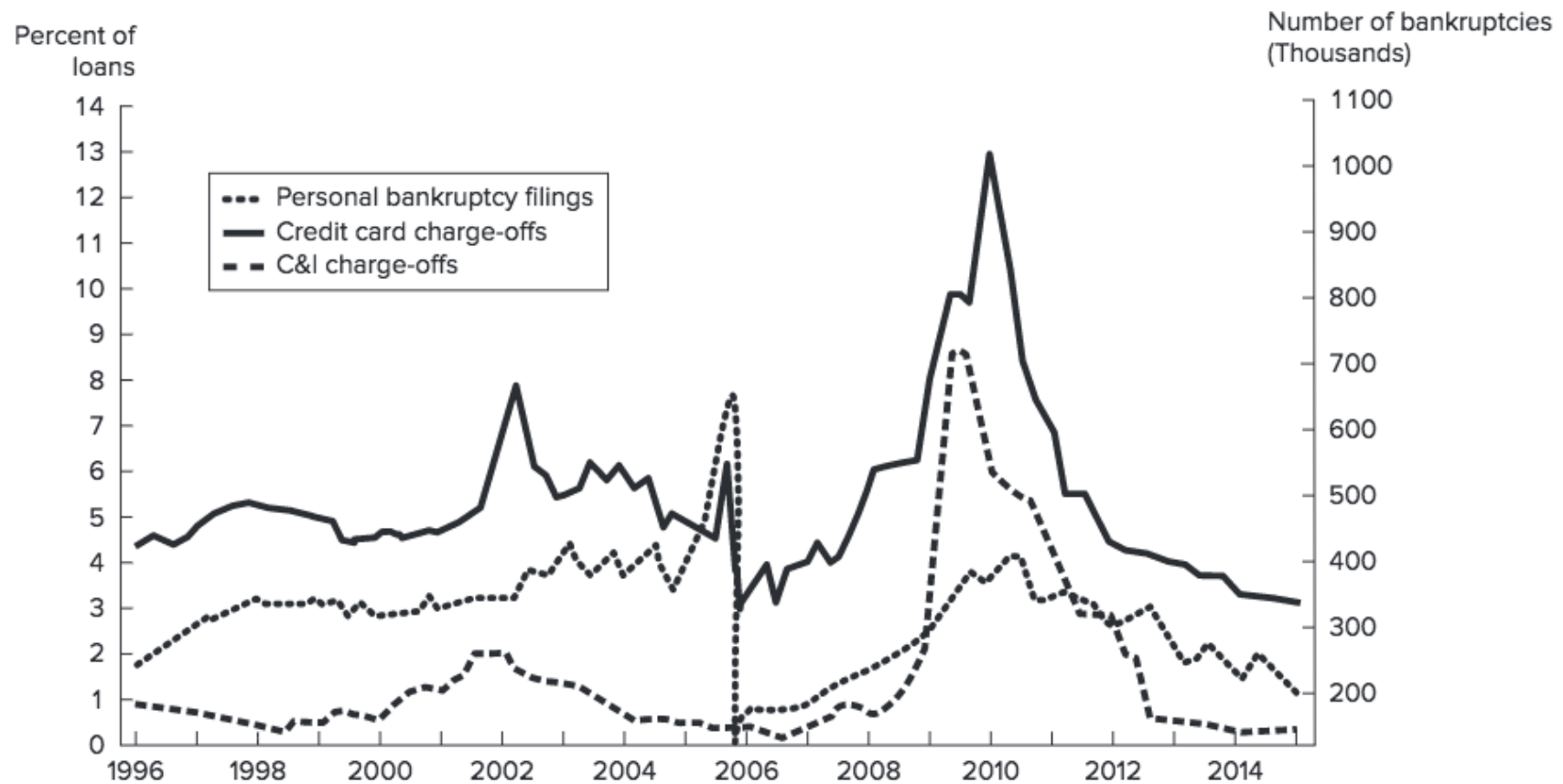
# ARMs' Share of Total Loans Closed, 1987-2014



# Individual (Consumer) Loans

- Consumer loans: personal, auto, credit card
  - Nonrevolving loans
    - ◆ Automobile, mobile home, personal loans
  - Revolving loans
    - ◆ Credit card debt (i.e., Visa, MasterCard)
    - ◆ Proprietary cards, such as Sears and AT&T
  - Risks affected by competitive conditions and usury ceilings
  - Bankruptcy Reform Act of 2005
- High default rates during finance crisis highlight the importance of risk evaluation prior to making a credit decision

# Annual Net Charge-Off Rates on Loans



# Other Loans

- Other loans include:
  - Farm loans
  - Other banks
  - Nonbank FIs, such as broker margin loans
  - Foreign banks and sovereign governments
  - State and local governments

# Calculating Return on a Loan

- Factors: Interest rate, fees, credit risk premium, collateral, and other nonprice terms, such as compensating balances and reserve requirements
- Return = inflow/outflow
$$1+k = 1+(of + (BR + \emptyset))/(1-[b(1-RR)])$$
- Expected return:  $1 + E(r) = p(1+k)$  where  $p$  equals probability of complete repayment
- Note that *realized* and *expected return* may not be equal

# Retail versus Wholesale Credit Decisions

- At retail
  - Usually a simple accept/reject decision rather than adjustments to the rate
  - Credit rationing
  - If accepted, customers sorted by loan quantity
  - For mortgages, discrimination occurs via loan-to-value rather than adjusting rates
- At wholesale
  - Use both quantity and pricing adjustments

# Risk Models

- Availability, quality, and cost of information are critical factors in credit risk assessment
  - Facilitated by technology and information
- Qualitative models consider borrower specific factors as well as market, or systematic, factors
  - Borrower-specific factors include reputation, leverage, volatility of earnings, and collateral
  - Market specific factors include business cycle and interest rate levels

# Linear Probability Model

- **Credit scoring models** are quantitative models that use borrower characteristics to gauge an applicant's probability of default

$$PD_i = \sum_{j=1}^n \beta_j X_{i,j} + \text{error}$$

- Major weakness is that estimated probabilities of default can often lie outside of the  $[0,1]$  interval
- Since superior statistical techniques are readily available, there is rarely justification for employing linear probability models

# Logit Model

- Logit models
  - Overcomes weakness of the linear probability model by restricting the estimated range of default probabilities from the linear regression model to lie between 0 and 1
- Quality of credit scoring models have improved, providing positive impact on controlling write-offs and default

# Altman's Discriminant Function

$$Z = 1.2X_1 + 1.4X_2 + 3.3X_3 + 0.6X_4 + 1.0X_5$$

Critical value of  $Z = 1.81$

- $X_1$  = Working capital/total assets ratio
- $X_2$  = Retained earnings/total assets ratio
- $X_3$  = EBIT/total assets ratio
- $X_4$  = Market value equity/ book value of total liabilities
- $X_5$  = Sales/total assets ratio

# Linear Discriminant Model

- Problems associated with discriminant analysis model:
  - Only considers two extreme cases (default/no default)
  - No reason to expect that the weights in a credit scoring model will be constant long-term; sensitivity to variable weights
  - Ignores hard to quantify factors, including business cycle effects and reputation
  - Database of defaulted loans is not available to benchmark the model

# Term Structure Derivation of Credit Risk

- If the risk premium is known, we can infer the probability of default
- Risk premium can be computed using Treasury strips and zero-coupon corporate bonds

$$p(1+k) = 1+i$$

# Mortality Rate Models

- Similar to the process employed by insurance companies to price policies; the probability of default is estimated from past data on defaults
- Marginal Mortality Rates:

$$\text{MMR}_1 = \frac{\text{(Value Grade B default in year 1)}}{\text{(Value Grade B outstanding yr.1)}}$$

$$\text{MMR}_2 = \frac{\text{(Value Grade B default in year 2)}}{\text{(Value Grade B outstanding yr.2)}}$$

- Has many of the problems associated with credit scoring models, such as sensitivity to the period chosen to calculate the MMRs

# RAROC Models

- Risk-adjusted return on capital
  - One of the most widely used models

$$RAROC = (One\ year\ NI\ on\ a\ loan) / (loan\ risk)$$

- Loan risk estimated from loan default rates, or using duration

# Using Duration to Estimate Loan Risk

- For denominator of RAROC, duration approach used to estimate loss in value of the loan:

$$\Delta LN / LN = -D_{LN} \times (\Delta R / (1 + R))$$

# Option Models

- Employ option pricing methods to evaluate the option to default
- Used by many of the largest banks to monitor credit risk
- KMV Corporation markets this model widely

# Applying Option Valuation Model

- Merton showed value of a risky loan:

$$L(\tau) = Be^{-i\tau}[(1/d)N(h_1) + N(h_2)]$$

- Written as a yield spread:

$$k(\tau) - i = (-1/\tau)\ln[N(h_2) + (1/d)N(h_1)]$$

where

$k(\tau)$  = Required yield on risky debt

$\ln$  = Natural logarithm

$i$  = Risk-free rate on debt of equivalent maturity

- $\tau$  = Remaining time to maturity

# Pertinent Websites

Federal Reserve Bank  
Comptroller of the  
Currency

[www.federalreserve.gov](http://www.federalreserve.gov)  
[www.occ.treas.gov](http://www.occ.treas.gov)

FDIC

[www.fdic.gov](http://www.fdic.gov)

Risk Management  
Association

[www.rmahq.org](http://www.rmahq.org)

Federal Housing  
Finance Agency

[www.fhfa.gov](http://www.fhfa.gov)

Moody's

[www.moody's.com](http://www.moody's.com)

Standard and Poor's

[www.standardandpoors.com](http://www.standardandpoors.com)

# Credit Analysis and Loan Underwriting

- Real Estate Lending
  - Two considerations dominate FI's decision to approve mortgage application:
    - Applicant's ability and willingness to make timely interest and principal repayments
    - Value of borrower's collateral

# Real Estate Lending

- Determining a customer's ability to maintain mortgage payments:

**GDS** = (Annual mortgage payments +  
Property taxes) / Annual gross  
income

**TDS** = Annual total debt payments /  
Annual gross income

# Lending

- Consumer and small-business
  - Similar techniques as mortgage loans
- Mid-market commercial and industrial
  - Annual sales revenues from \$5 million to \$100 million, recognizable corporate structure, but no access to liquid capital markets
- 5 C's of credit are: character, capacity, collateral, conditions, and capital

# Black-Scholes Option Pricing Model

- Model used to value European options:

$$C = N(d_1)S - E(e^{-rT})N(d_2)$$

$$d_1 = \frac{\ln(S/E) + (r + \sigma^2/2)T}{\sigma\sqrt{T}}$$

$$d_2 = d_1 - \sigma\sqrt{T}$$

# Model Assumptions

- Capital markets are frictionless
- Constant variability in underlying asset's return
- Log normal probability distribution of underlying asset's price
- Constant risk-free rate that is known over time
- No dividends on underlying asset
- No early exercise on option