

# EE312 Macroeconomic Theory

## Chapter 8

### A Real Intertemporal Model with Investment (Part 3)

# Exogenous shocks in the model

- A shock in the model occurs when one of **exogenous variables** changes, causing endogenous variables to change accordingly.
- The macro effect depends on whether it is temporary or permanent.
- An expected shock in the future has effects in the current period.

# Shock experiments

- Current government purchases increase temporarily ( $G$ );
- Current capital stock decreases due to a natural disaster or war ( $K$ );
- A temporary increase in current total factor productivity ( $z$ );
- An increase in future total factor productivity ( $z'$ ).

# A temporary increase in $G$

- Assume an increase in  $G$  with  $G'$  unchanged.
- **Keynesian (EE212) analysis:**
  - A higher  $G$  causes the demand for goods to increase.
  - Output and income increases.
  - Part of the increase in income is spent on consumption goods --- more demand for output.
  - Direct and indirect increases in the demand for output --- **the multiplier effect.**

# The Keynesian $Y^d$ multiplier

$$\Delta Y^d = \Delta G$$

$$\Delta C = MPC \Delta Y^d \text{ where } 0 < MPC < 1$$

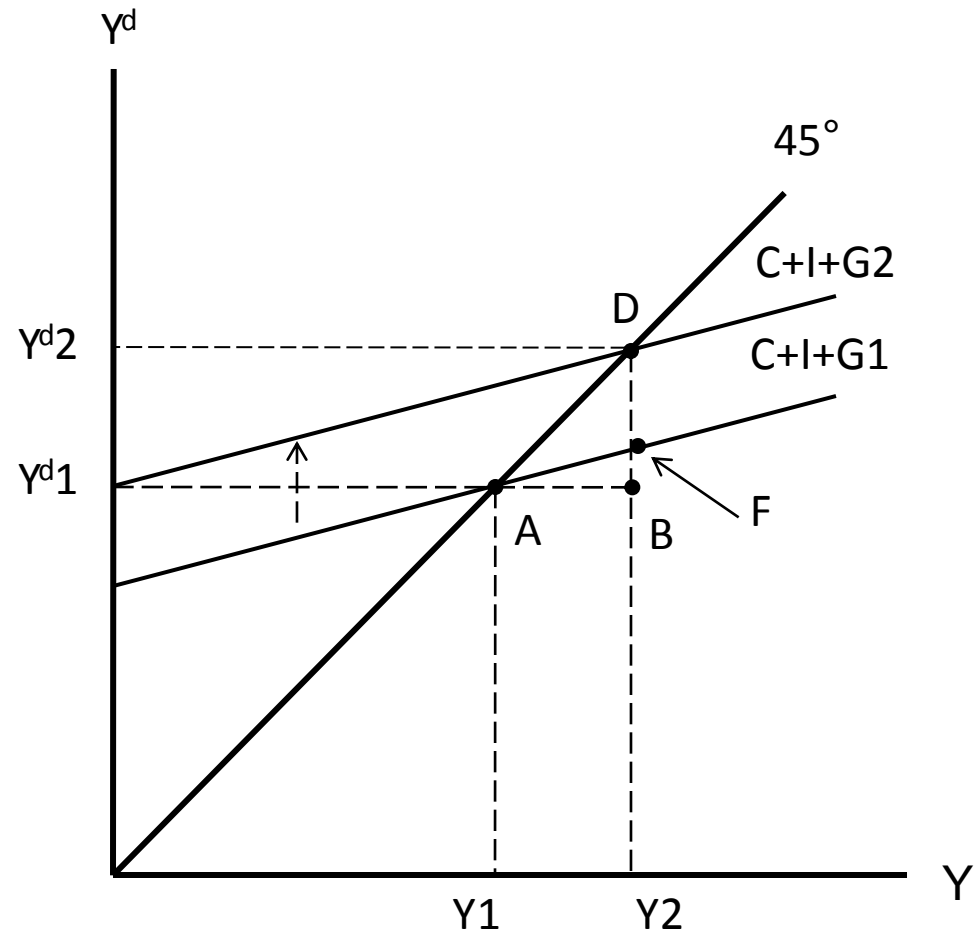
$$\Delta Y^d = \Delta G + MPC \Delta Y^d$$

$$\Delta Y^d = \frac{1}{1 - MPC} \Delta G$$

- The larger is MPC, the larger the  $Y^d$  multiplier, and the more powerful  $\Delta G$ !

# The Keynesian $Y^d$ multiplier $> 1$

- Assume constant MPC.
- $\Delta G = DF$
- $\Delta Y = \Delta Y^d = AB = DB$
- But  $DB > DF$
- So  $\Delta Y / \Delta G > 1!$



# Keynesian assumptions

- The increase in  $G$  has no negative effect on lifetime wealth and consumption spending.
  - But PV of taxes must rise and lifetime wealth falls.
- Total income or output ( $Y$ ) increases by the same amount as the demand for goods ( $Y^d$ ).
- The effect on the real interest rate?
- Increases in  $C$  and  $Y$  come as a free lunch!

# Demand multiplier = 1

- The increase in total current demand for goods ( $Y^d$ ):
  - The increase in government spending =  $\Delta G$ .
  - The multiplier effect =  $MPC\Delta G$ .
  - Lifetime wealth drops = PV of taxes =  $\Delta G$ ; so current consumption falls by  $-MPC\Delta G$ .

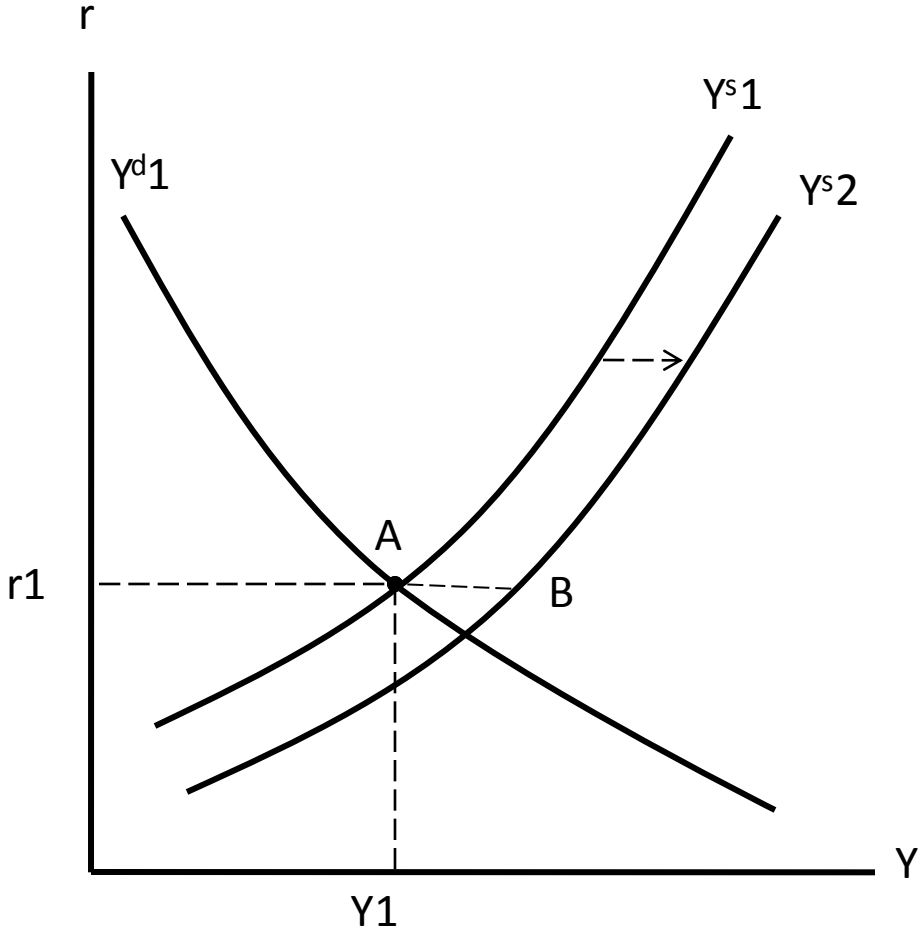
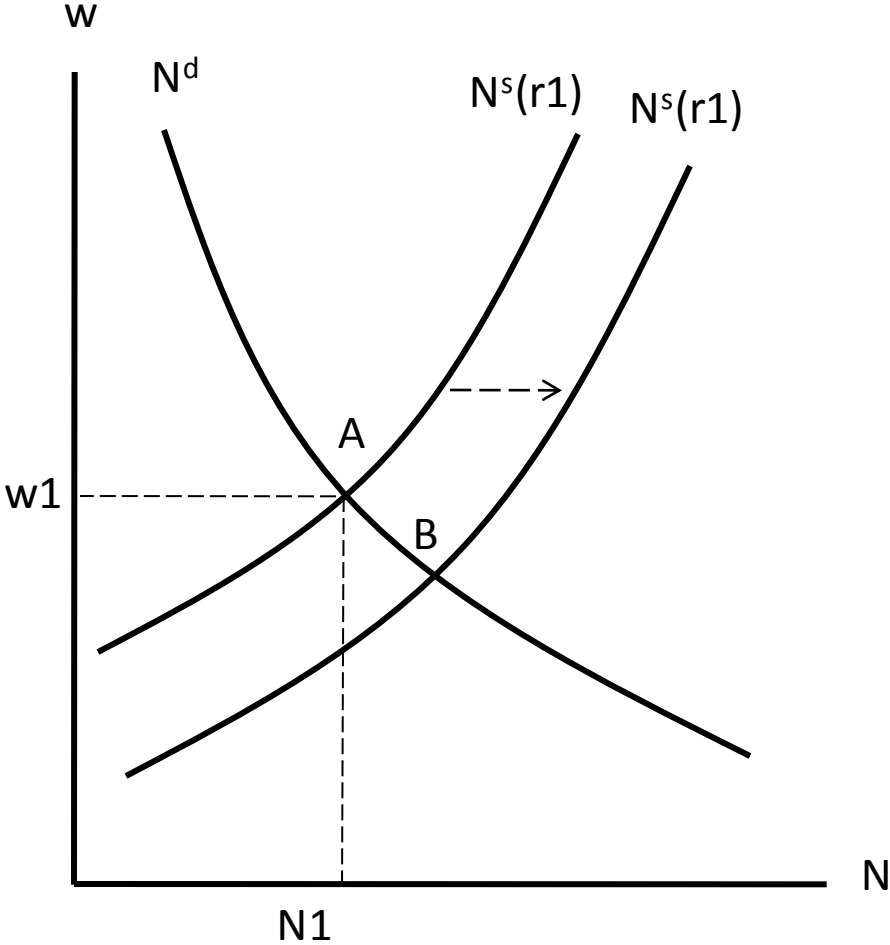
$$\Delta Y^d = \Delta G + MPC\Delta G - MPC\Delta G$$

$$\Delta Y^d = \Delta G$$

# Intertemporal model analysis

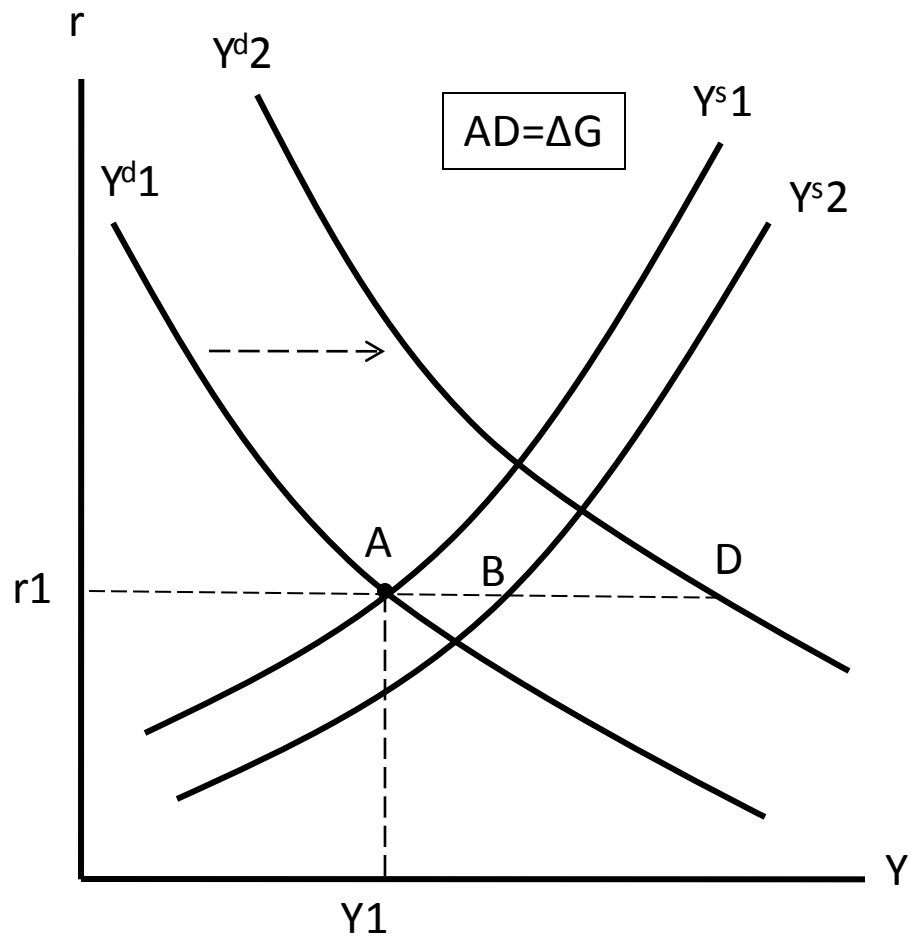
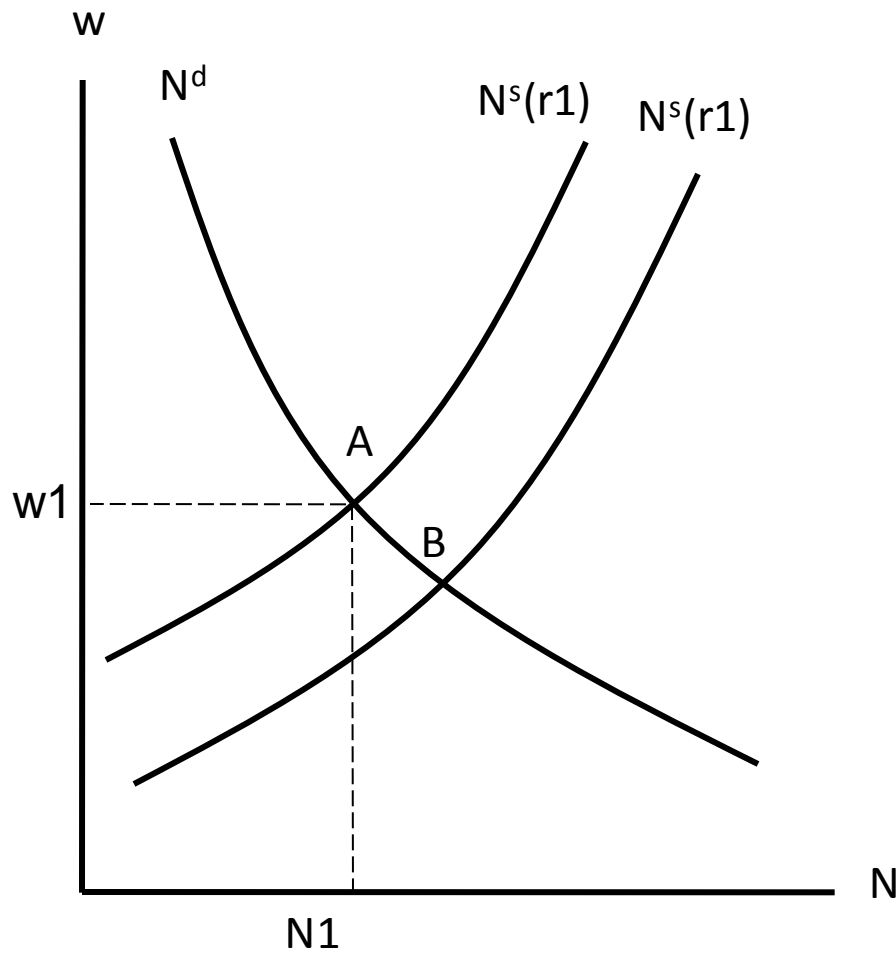
- **Step 1:** direct effect of  $\Delta G$ :
- **Effects on  $Y^s$ :**
  - The PV of taxes rises; the consumer's lifetime wealth falls.
  - Leisure decreases and **labor supply** increases, given the real wage.
  - The output supply curve shifts rightwards.

# Step 1 An increase in G: $Y^s$ shift



- **Effects on  $Y^d$ :**
  - Government's demand for output ( $G$ ) increases.
  - Falling lifetime wealth reduces the consumer's demand for current consumption goods ( $C^d$ ).
  - **Current demand for goods** increases by the amount of  $\Delta Y^d = \Delta G$ ; the  $Y^d$  multiplier = 1 .
  - $Y^d$  shifts rightwards by the amount of  $\Delta G$ .
- Both  $Y^s$  and  $Y^d$  shift to the right; what happens to the real interest rate?

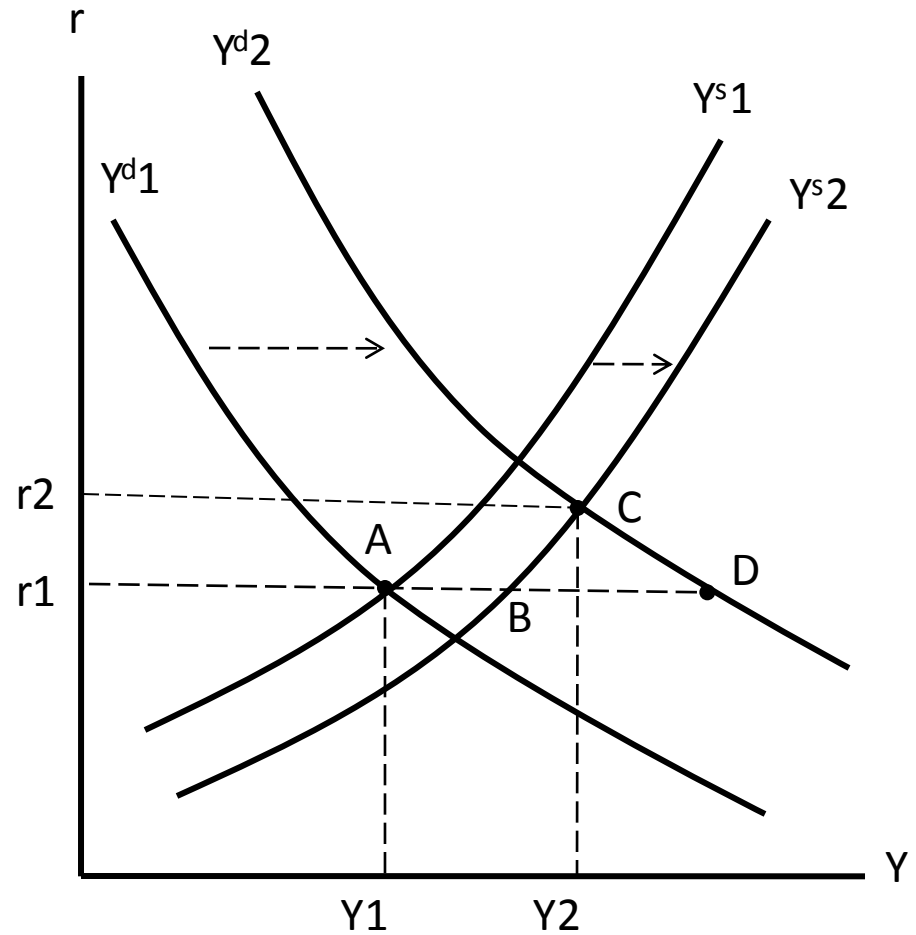
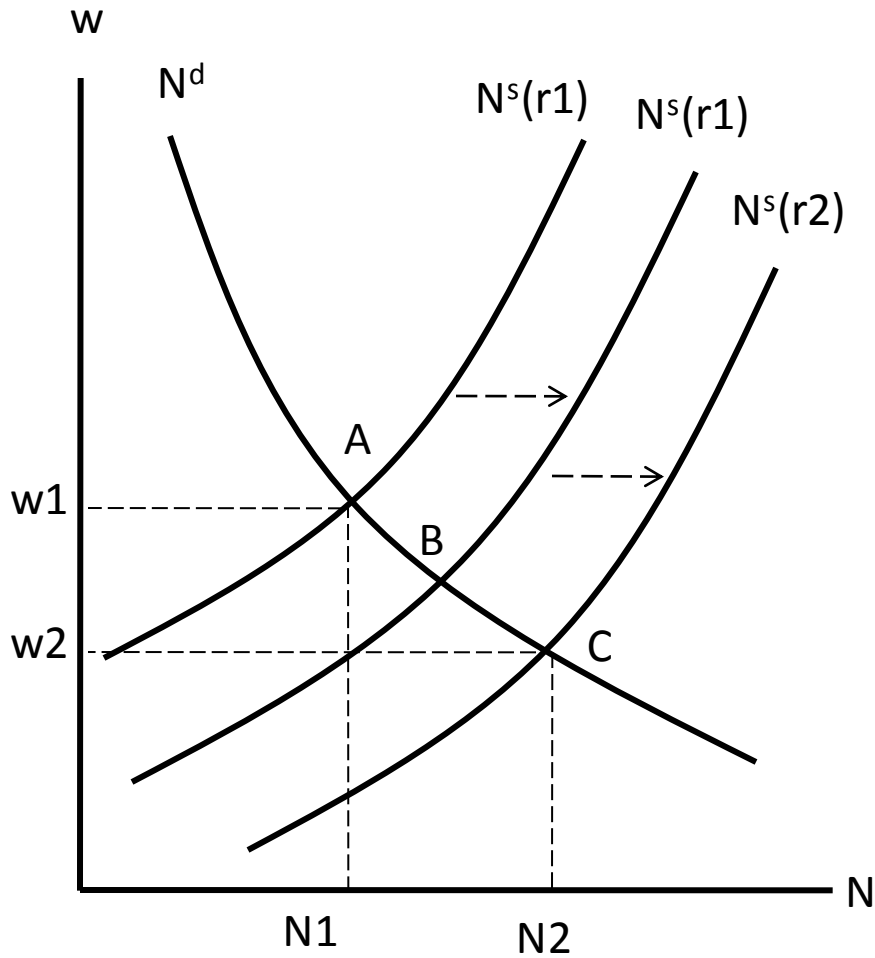
# Step 1 An increase in $G$ : $Y^d$ shift



- The real interest rate increases as  **$Y^d$  shifts more than  $Y^s$** .
  - $\Delta G$  is temporary and has a small negative effect on lifetime wealth.
  - A small decrease in leisure, and small increases in labor supply and output supply (small  $Y^s$  shift).
  - A small decrease in current consumption while the increase in  $G$  remains large (larger  $Y^d$  shift).
- **Step 2:** effect of the rising  $r$ .
  - A higher  $r$  reduces leisure, current consumption and investment.

- Leisure falls and **labor supply** increases again.
  - The real wage falls further; employment and output increase, a movement along the  $Y^s$  (BC).
- **Investment** decreases due to the higher real interest rate (DC).
- **Current consumption** falls (DC):
  - Falling lifetime wealth reduces current consumption while higher income raises it --- small net effect.
  - The higher  $r$  also reduces it --- dominant effect.

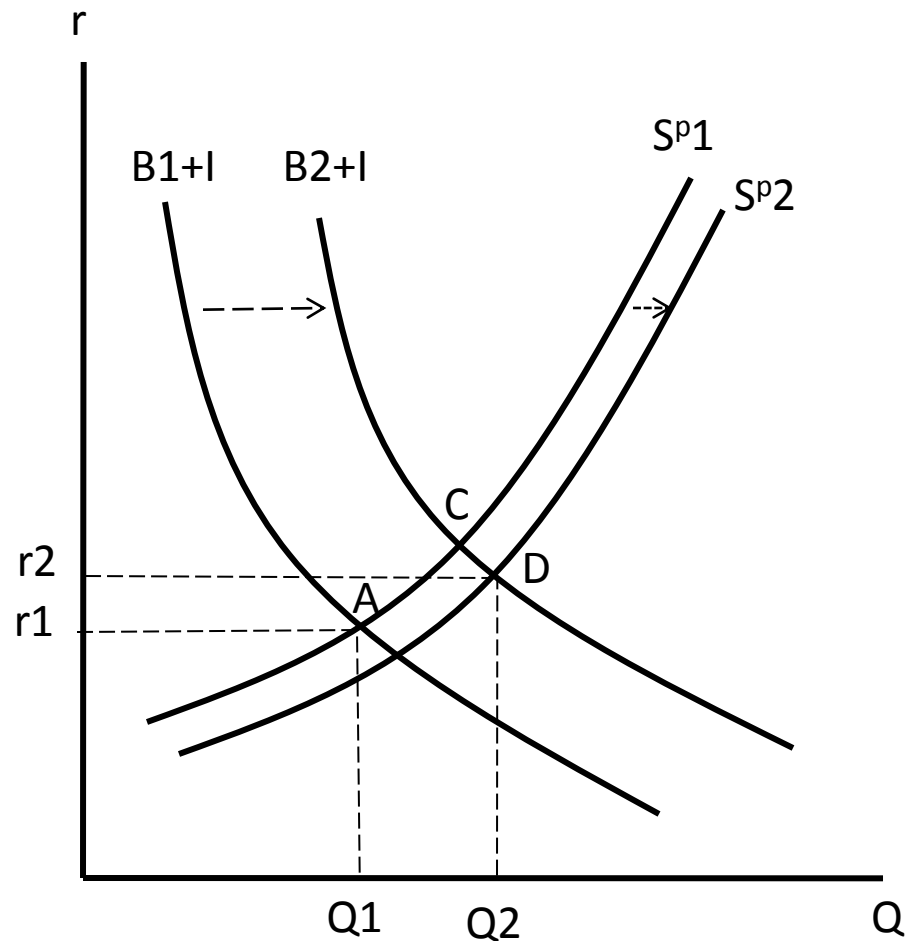
# Step 2 An increase in G: rising r



- Assume the government finances the spending increase by bond sale in the credit market ( $\Delta G = \Delta B$ ).
- Private savings increase:
  - Larger current income ( $Y$ ) and lower current consumption raise private savings.
  - $\Delta S^p = \Delta Y - \Delta T - \Delta C$  where  $\Delta T = 0$  and  $\Delta C < 0$ .
- The increase in bond sale raises the real interest rate.

# The credit market

- The government increases current borrowing ( $B$ ).
- Savings increase from higher  $r$  ( $AC$ ) and larger  $Y$  ( $CD$ ).
- The real interest rate increases.



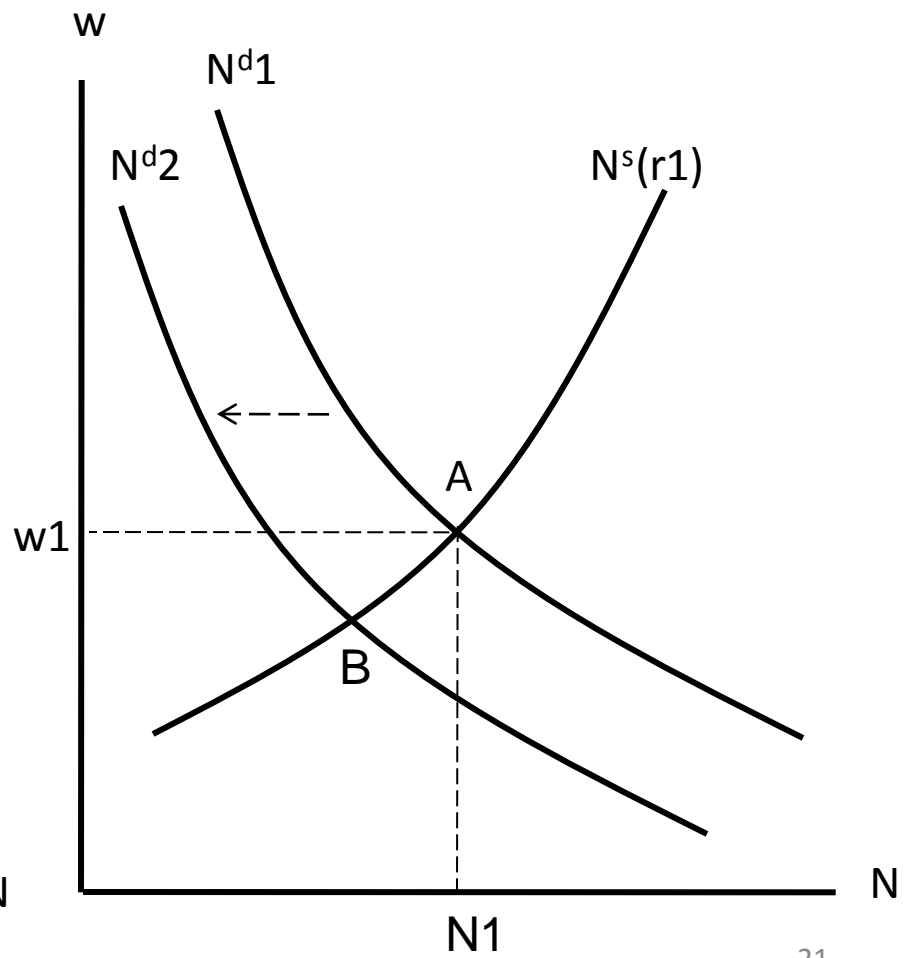
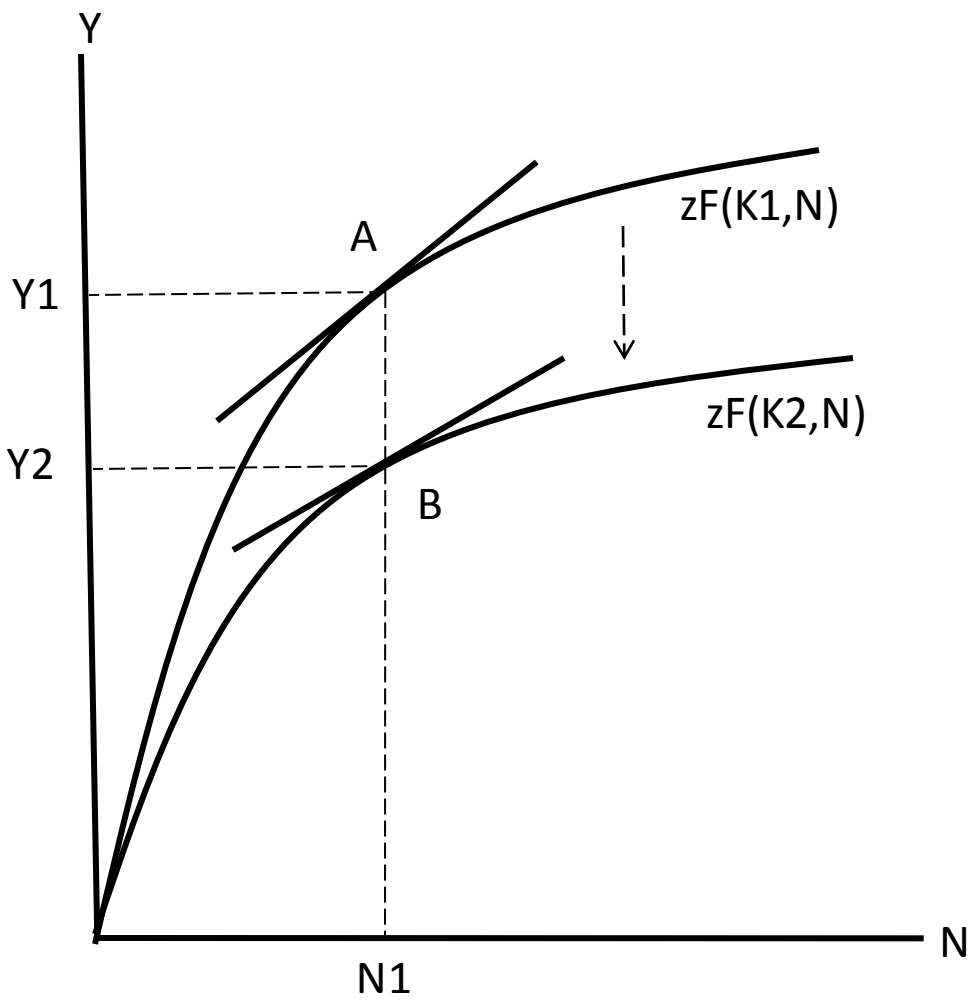
- The **total output multiplier** is less than 1.
  - $\Delta Y^d = \Delta G = AD > Y1Y2$ .
  - So  $\Delta Y/\Delta G < 1$ ; income increases less than the increase in government spending.
  - Although income increases, both current consumption and investment decrease from the higher real interest rate (**the crowding-out effect**).
  - Employment increases but the real wage drops.
  - Private savings increase to pay for higher future taxes.

- **The crowding-out effect** on private spendings.
  - A temporary increase in  $G$  *crowds out* both current consumption and investment by raising the real interest rate.
  - The consumer works more for a lower real wage and consumes less.
  - Lower investment means lower future capital stock and future productive capacity.
- Higher government spending and larger output come at a cost --- no free lunch!

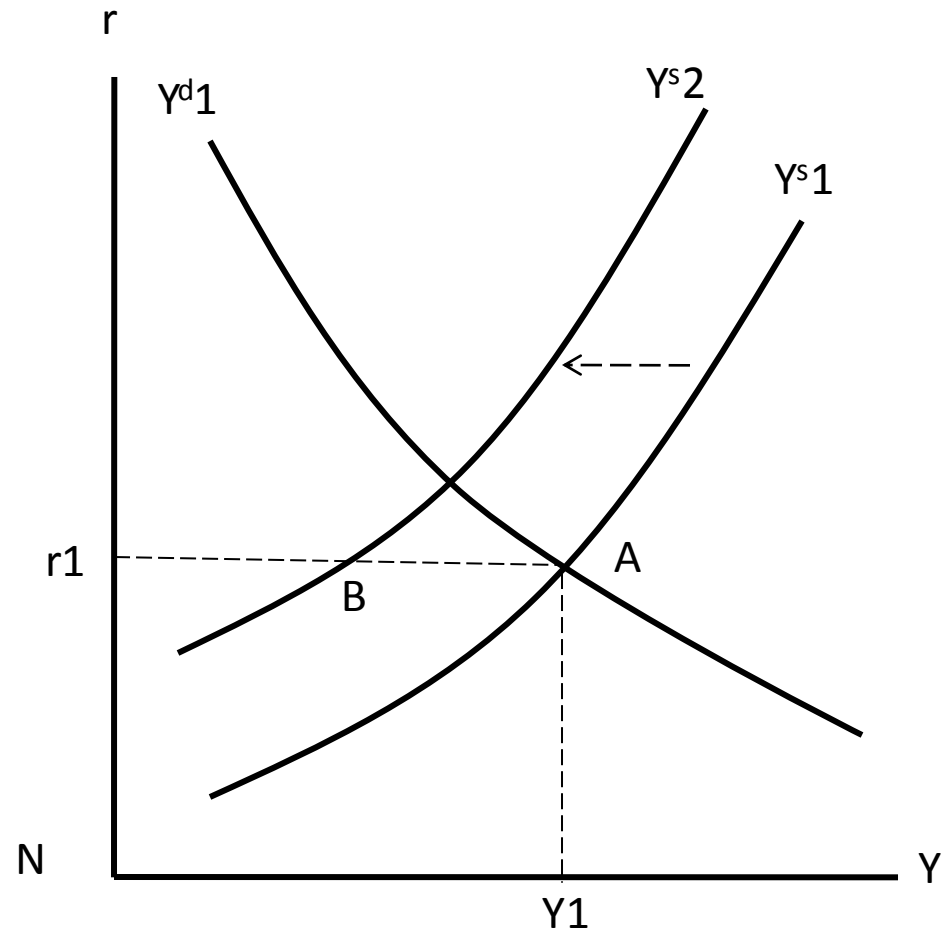
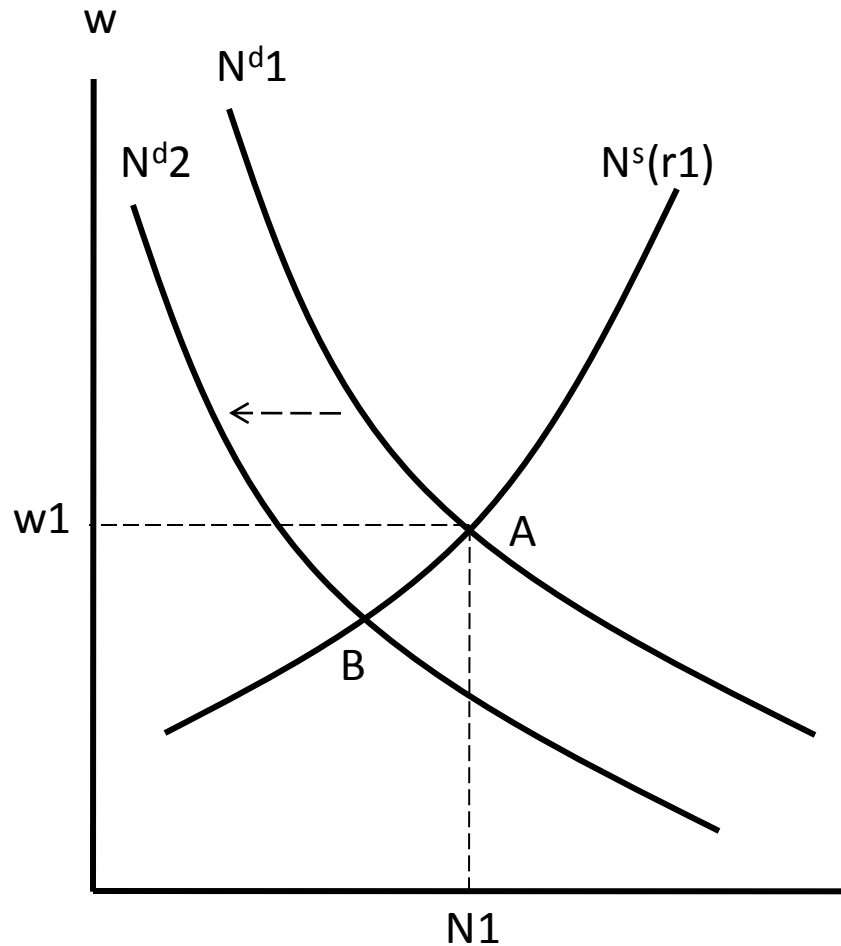
# A decrease in current capital stock

- Reduction in current capital stock ( $K$ ) due to a natural disaster or war.
- **Step 1: Effect on  $Y^s$ :**
  - A smaller  $K$  with the same  $N$ , current  $MP_N$  drops.
  - The firm reduces its demand for labor. The labor demand curve shifts left (given  $w$ ).
  - The output supply curve ( $Y^s$ ) shifts left.

# Step 1 A lower K reduces $MP_N$

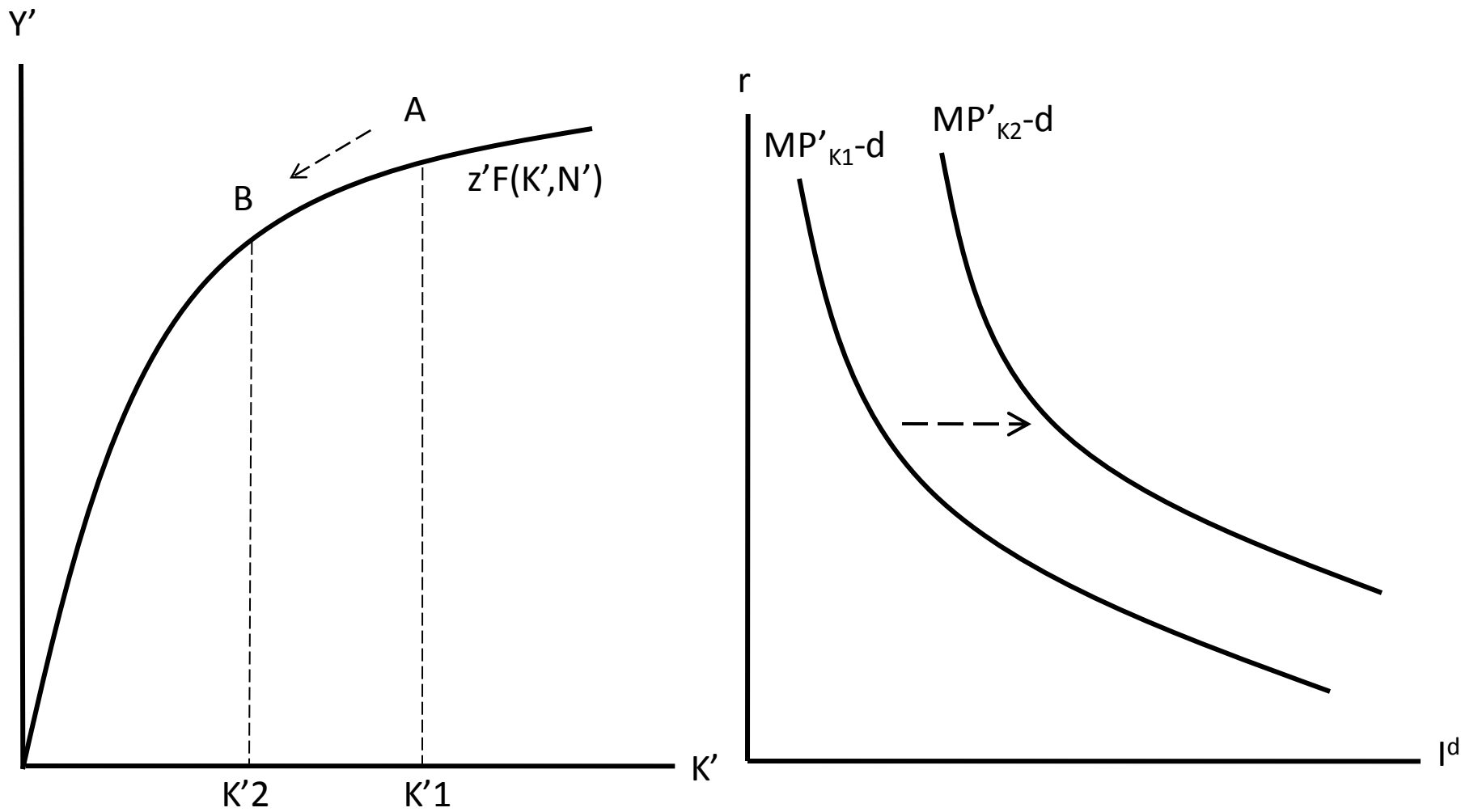


# Step 1 Lower $N^d$ : $Y^s$ shifts left.

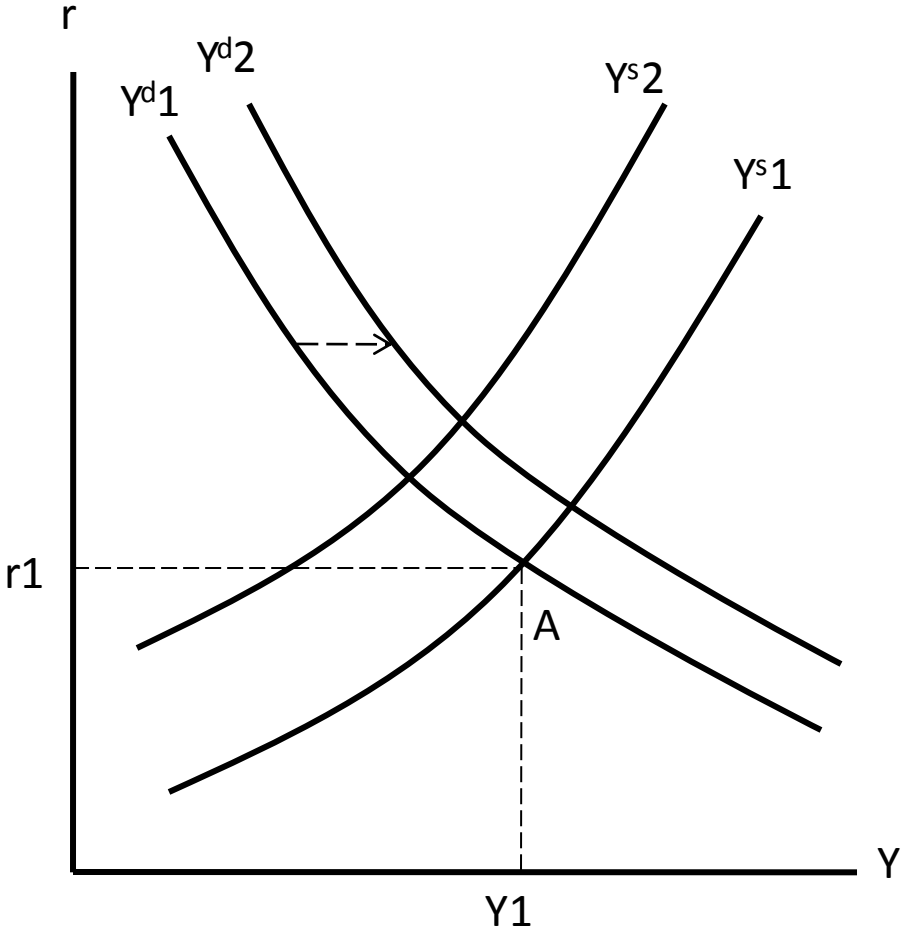
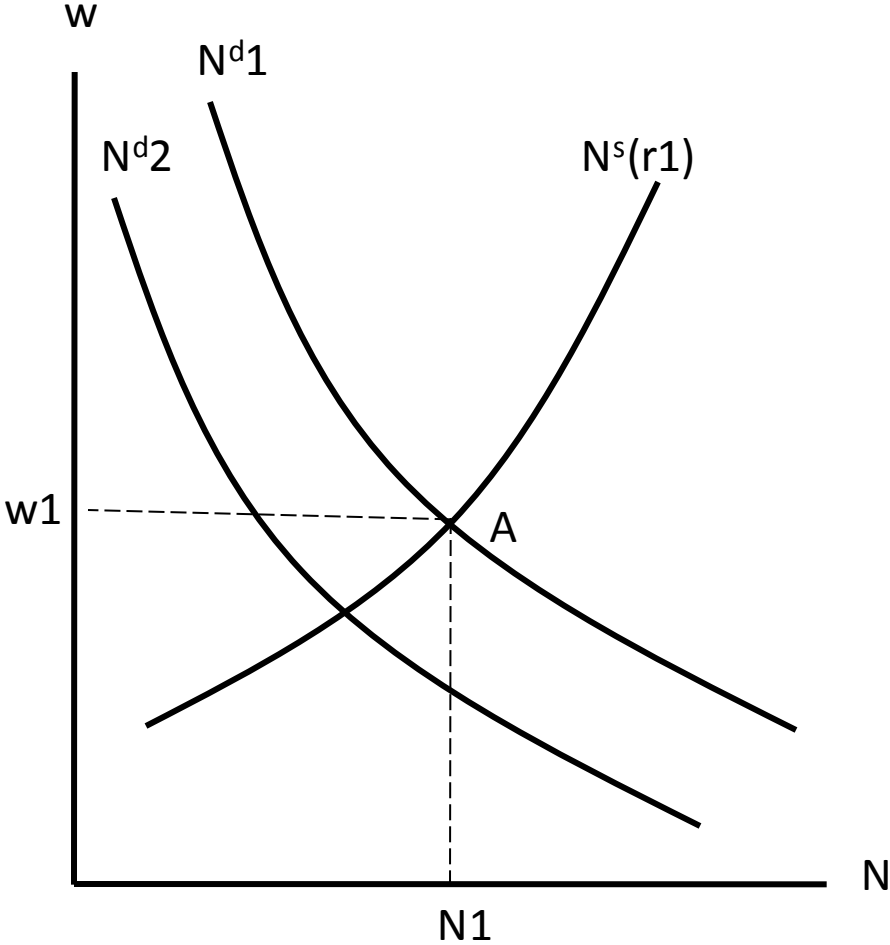


- **Effect on  $Y^d$ :**
  - A smaller current  $K$  means a smaller future  $K'$ .
  - Future  $MP'_K$  rises; investment increases, given  $r$ .
  - The optimal investment curve ( $I^d$ ) shifts right.
  - The output demand curve ( $Y^d$ ) shifts right.
- **The real interest rate** must rise.
- **Step 2:** the higher real interest rate reduces leisure (increases labor supply), current consumption and investment.

# Step 1 Higher $MP'_K$ and rising $I^d$

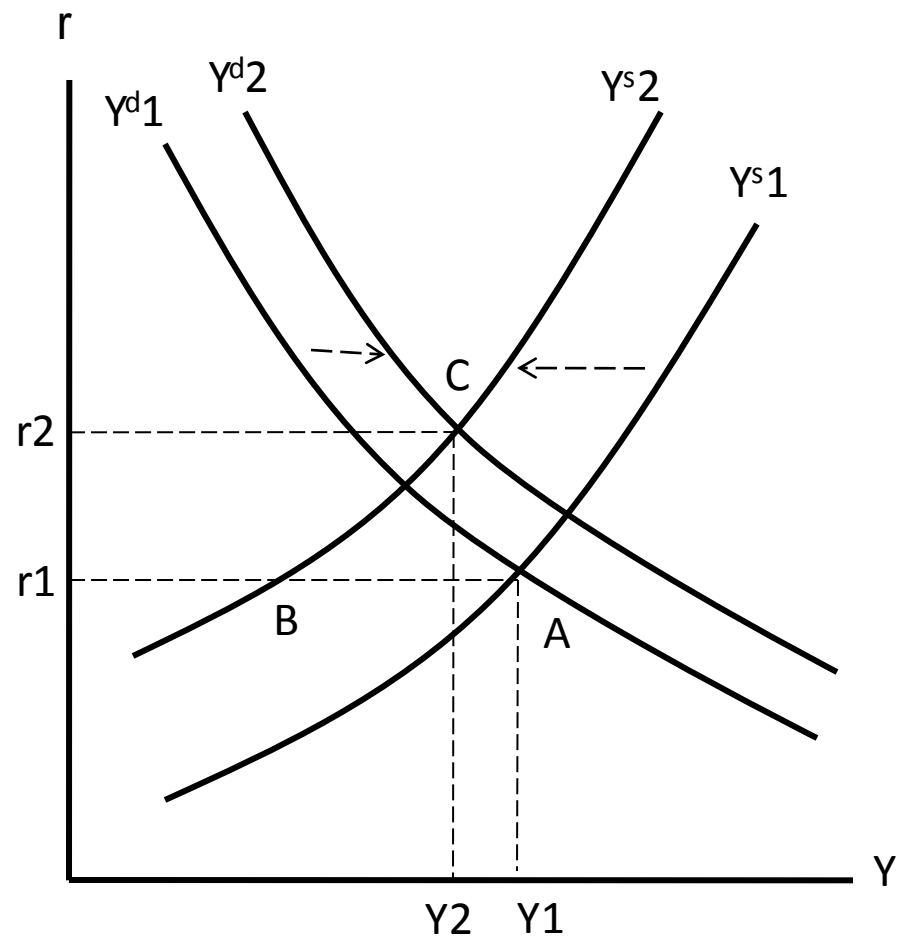
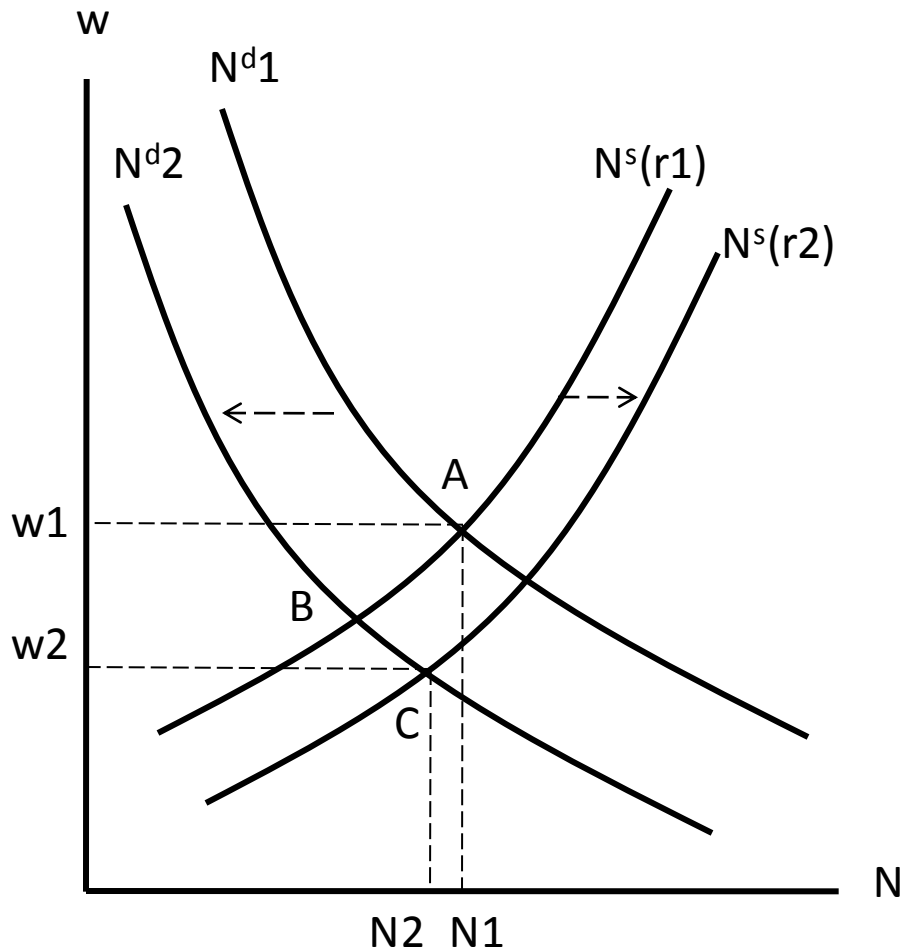


# Step 1 A rising $I^d$ shifts $Y^d$ right.



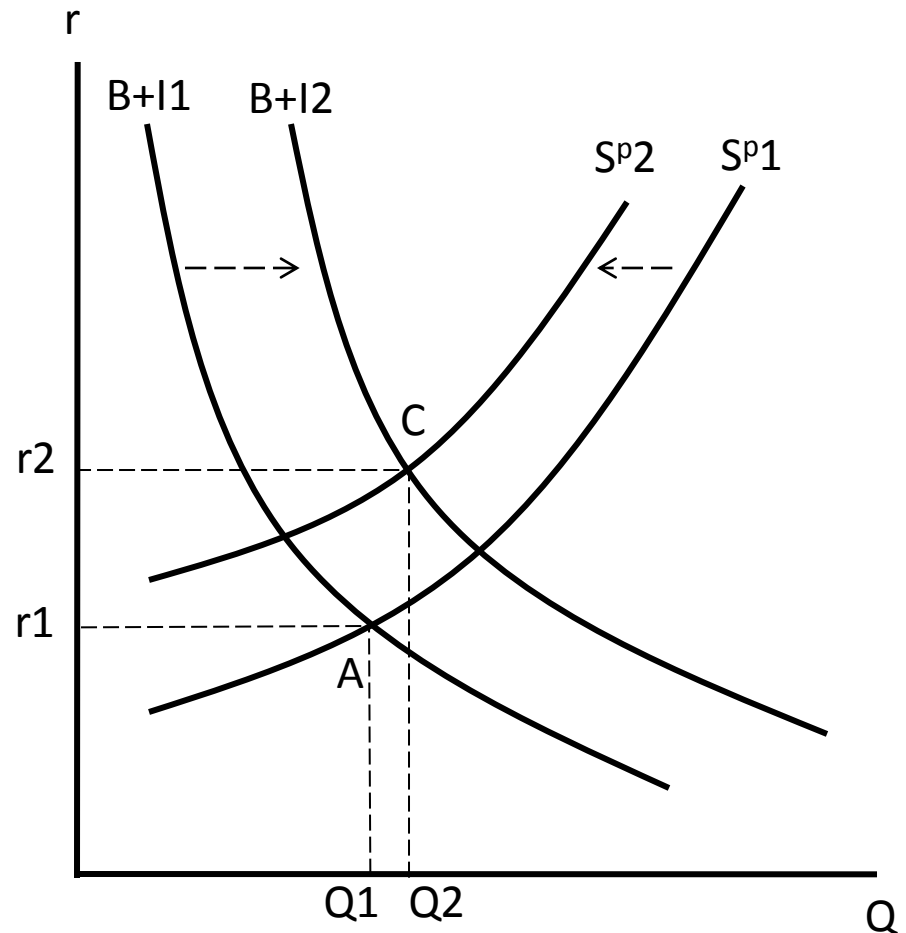
- Leisure decreases and labor supply increases.
  - The labor supply curve shifts to the right.
  - The real wage drops further.
  - A movement on the  $Y^s$  curve.
- Investment increases to make up for the decline in the capital stock:
  - The higher real interest rate depresses investment, but higher  $MP'_K$  raise it.
  - If investment finally decreases, current  $K$  will be falling indefinitely --- impossible.

# Step 2 A decrease in current K: rising $r$



# The credit market

- C drops less than Y ( $\Delta Y > C\Delta$ ).
- Consumption smoothing;  $S^p$  decreases.
- $I^d$  increases.
- The real interest rate increases.



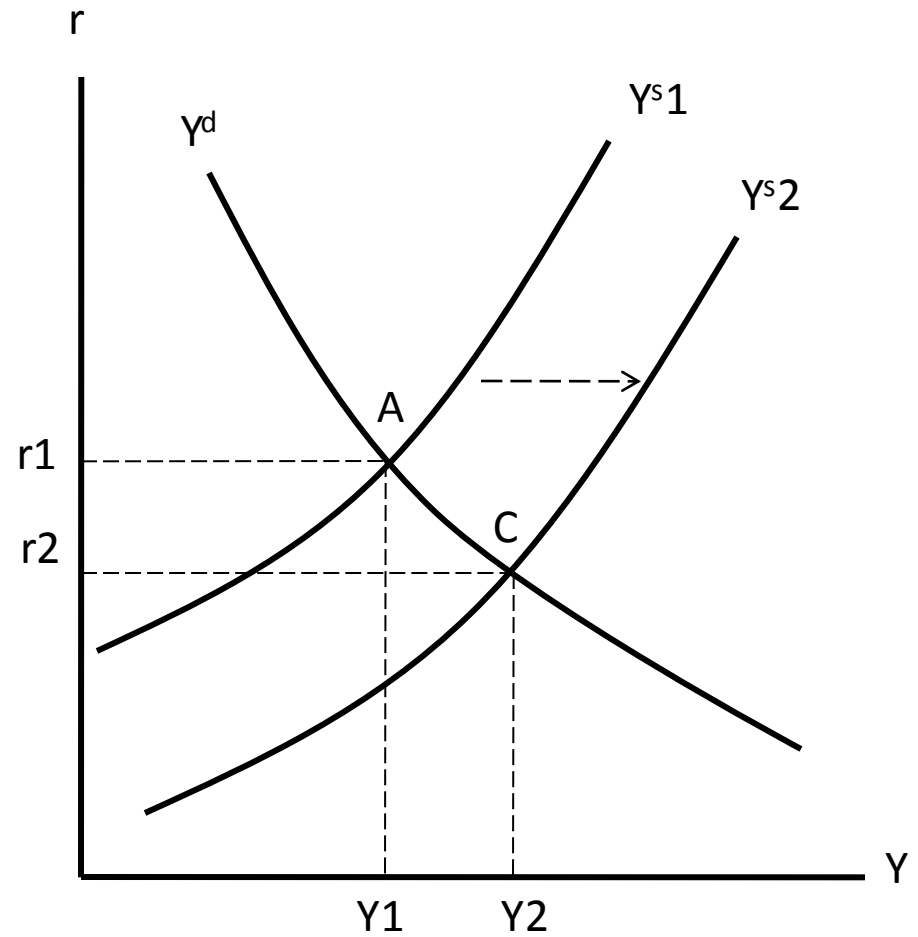
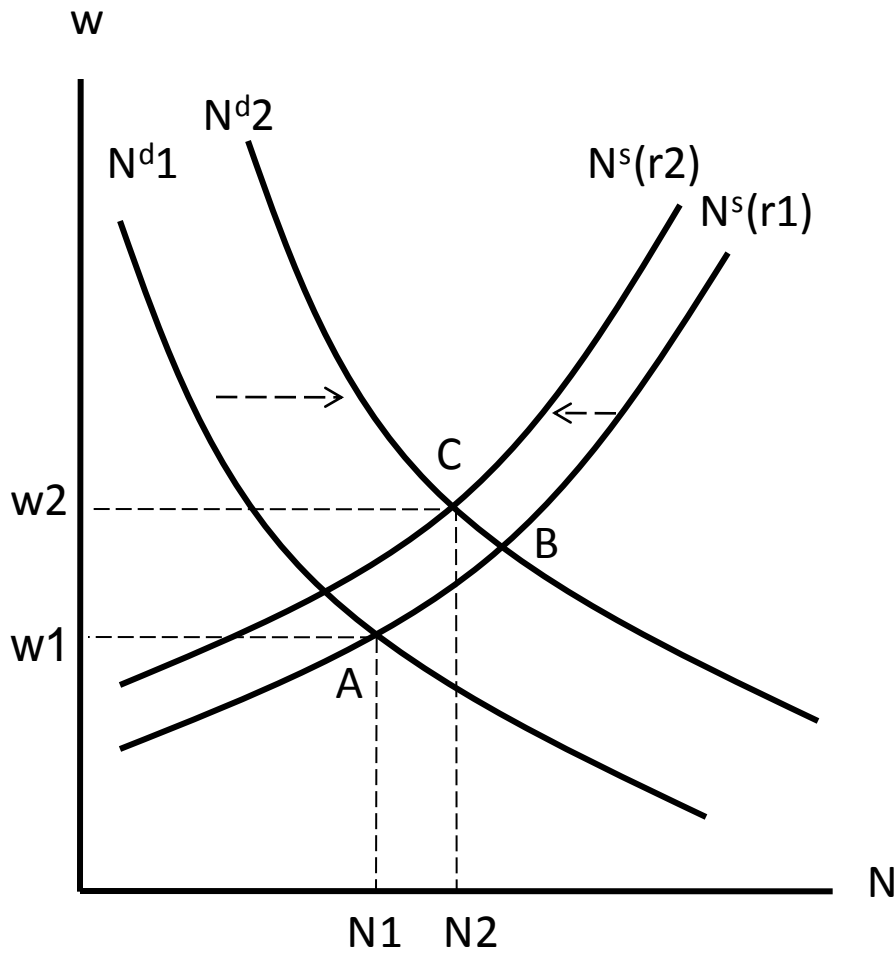
# Overall effect of a drop in K

- A decrease in current K raises the real interest rate but may increase or reduce output.
  - Current consumption and leisure decrease.
  - Investment increases.
  - The real wage decreases.
  - Employment and output may increase or decrease.
- Destruction of K tends to reduce output and employment.

# A temporary increase in $z$

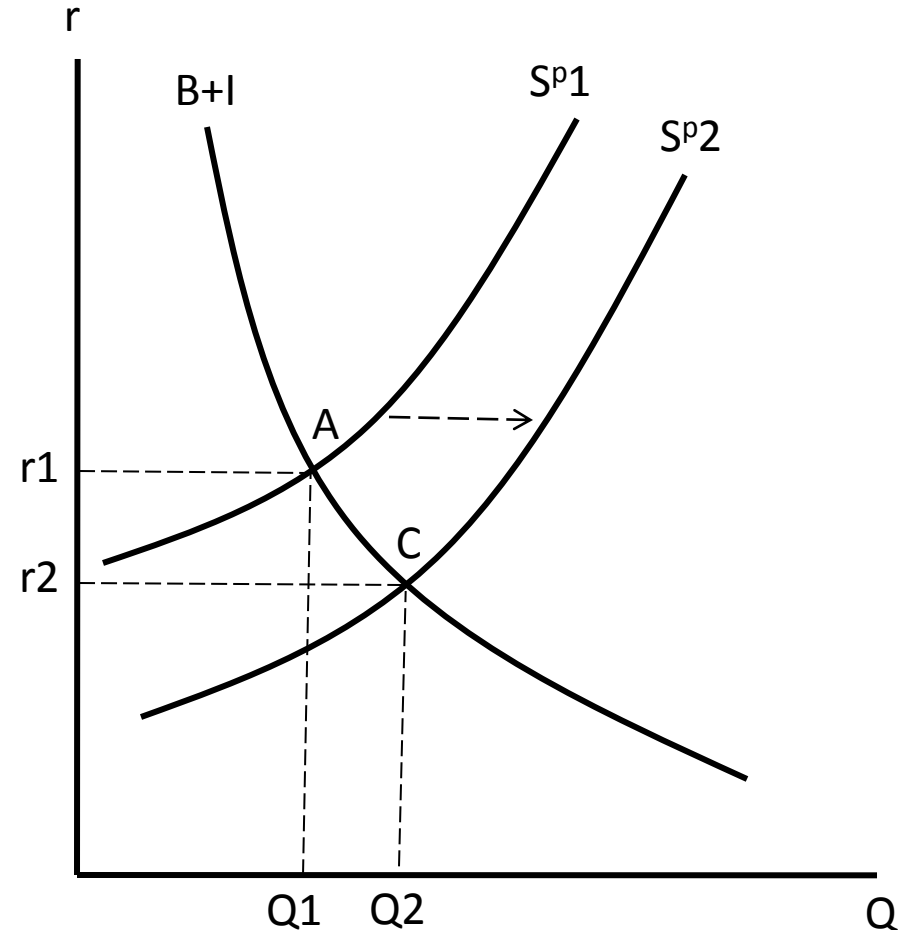
- **Step 1:** An increase in current total factor productivity ( $z$ ) raises  $MP_N$ .
  - Labor demand and **output supply shift right.**
  - The real interest rate decreases.
- **Step 2:** the lower real interest rate raises current consumption, investment and leisure.
  - Labor supply decreases; the labor supply curve shifts left.
  - Employment, output and the real wage increase.

# An increase in $z$



# The credit market

- Consumption increases less than income (consumption smoothing).
- Private savings increase.
- The real interest rate decreases.



# Overall effect of $\Delta z$

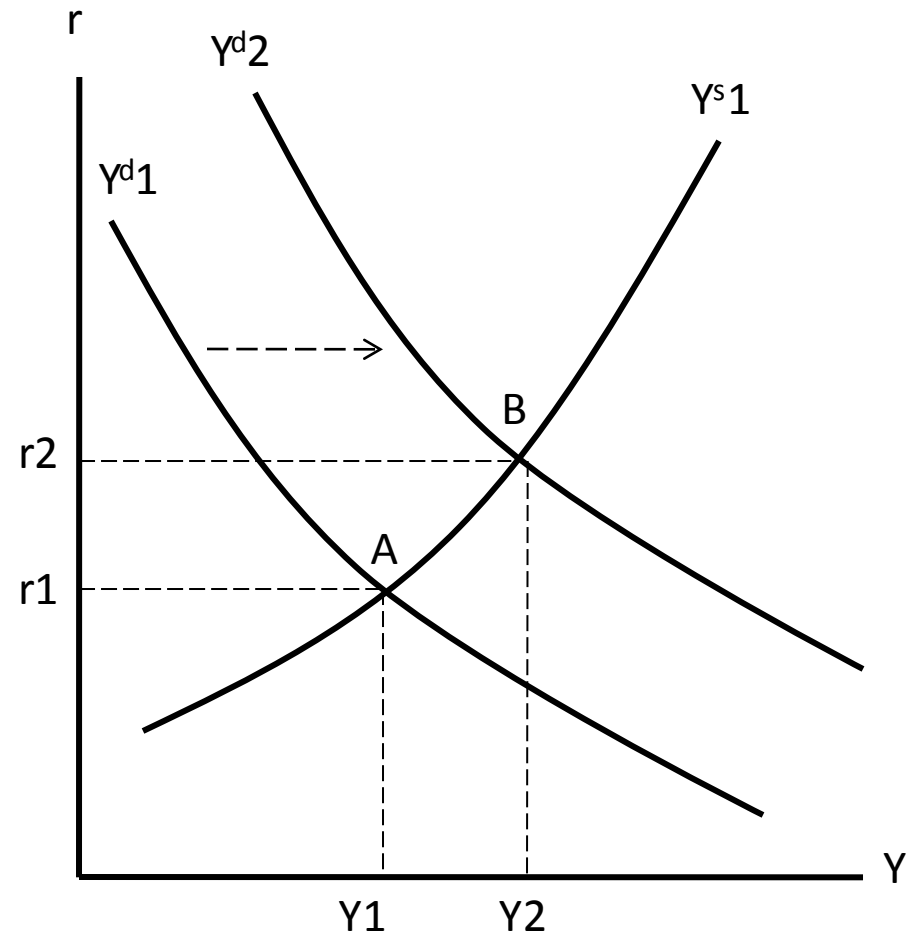
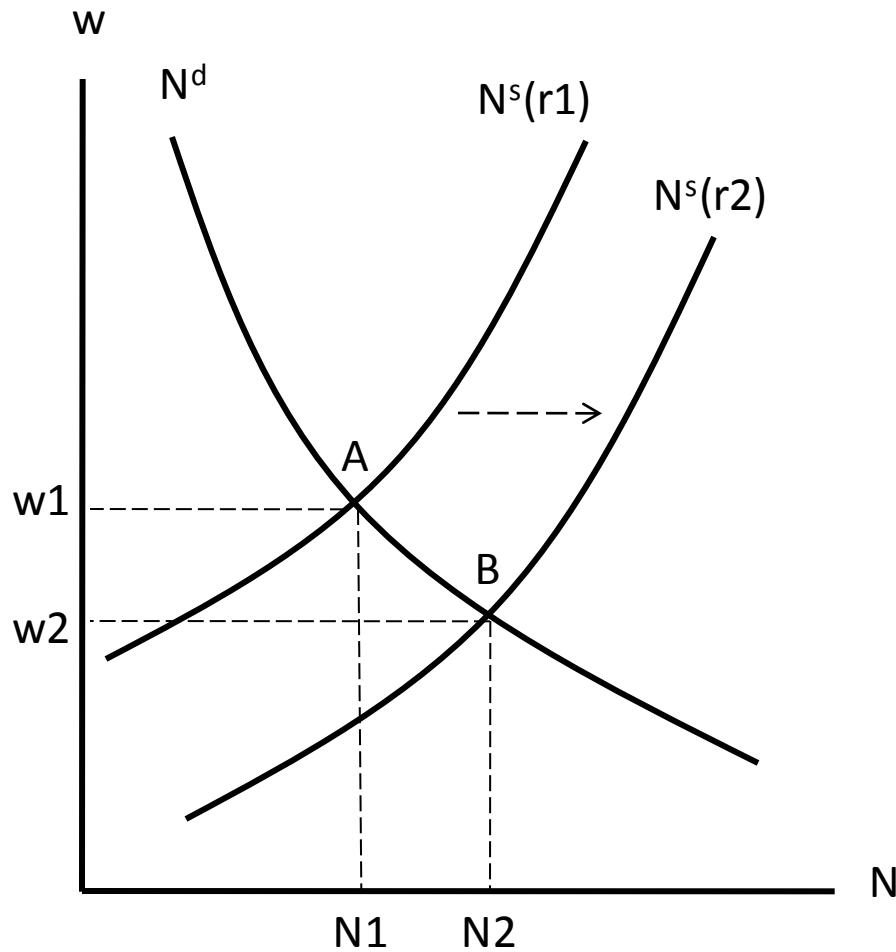
- An increase in the current  $z$  reduces the real interest rate but increases output.
  - Employment and output increase.
  - The real wage increases.
  - This is partly offset by the increase in leisure (with lower  $r$  and higher current income).
  - Investment increases (with lower  $r$ ).
  - Current consumption increases with lower  $r$  and larger  $Y$ .

# An increase in future $z'$

- **Step 1:** Future  $z'$  is expected to rise; future  $MP'_K$  increases.
- Investment ( $I^d$ ) increases; higher future income raises current consumption.
- Output demand shifts right (increases).
  - The real interest rate increases.
- **Step 2:** the higher  $r$  reduces consumption, investment and leisure.

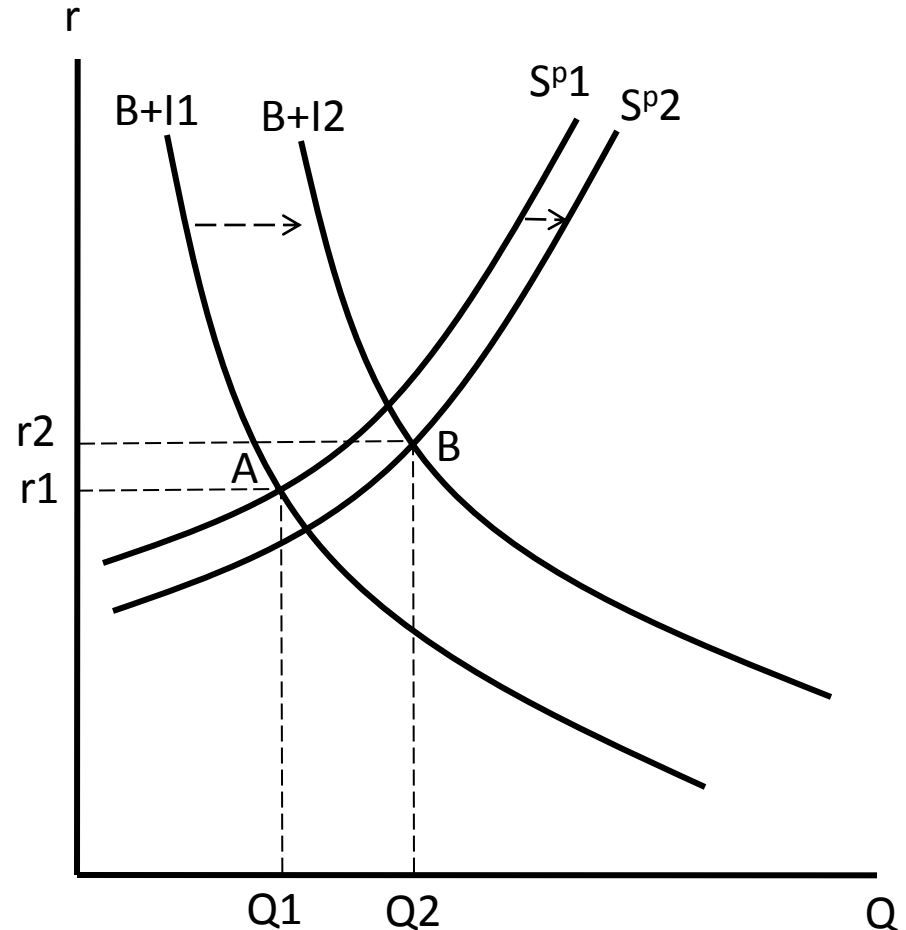
- The labor supply curve shifts right; the real wage drops.
- Employment and output increase.
- Higher current consumption from higher income partially drops from the higher real interest rate.
- The higher investment from higher  $MP'_K$  is partially offset by the higher real interest rate.
  - Investment increases as the effect of  $MP'_K$  is stronger .

# An expected increase in $z'$



# The credit market

- Investment increases.
- $C$  increases less than  $Y$ ; private savings increase.
- The real interest rate increases.



# Overall effect of $\Delta z'$

- Investment increases with higher expected  $MP'_K$ , partly offset by the higher  $r$ .
- Both real interest rate and output increase.
- Current consumption rises from higher current and future income but falls due to the higher real interest rate.
- Employment increases with falling real wage.