

# EE441

## Public Goods (1)

## Characteristics of <sup>PURE</sup>Public Goods

- **Nonrivalry**: The characteristic that if one person “consumes” a good, another person’s pleasure is not diminished, nor is another person prevented from consuming it.

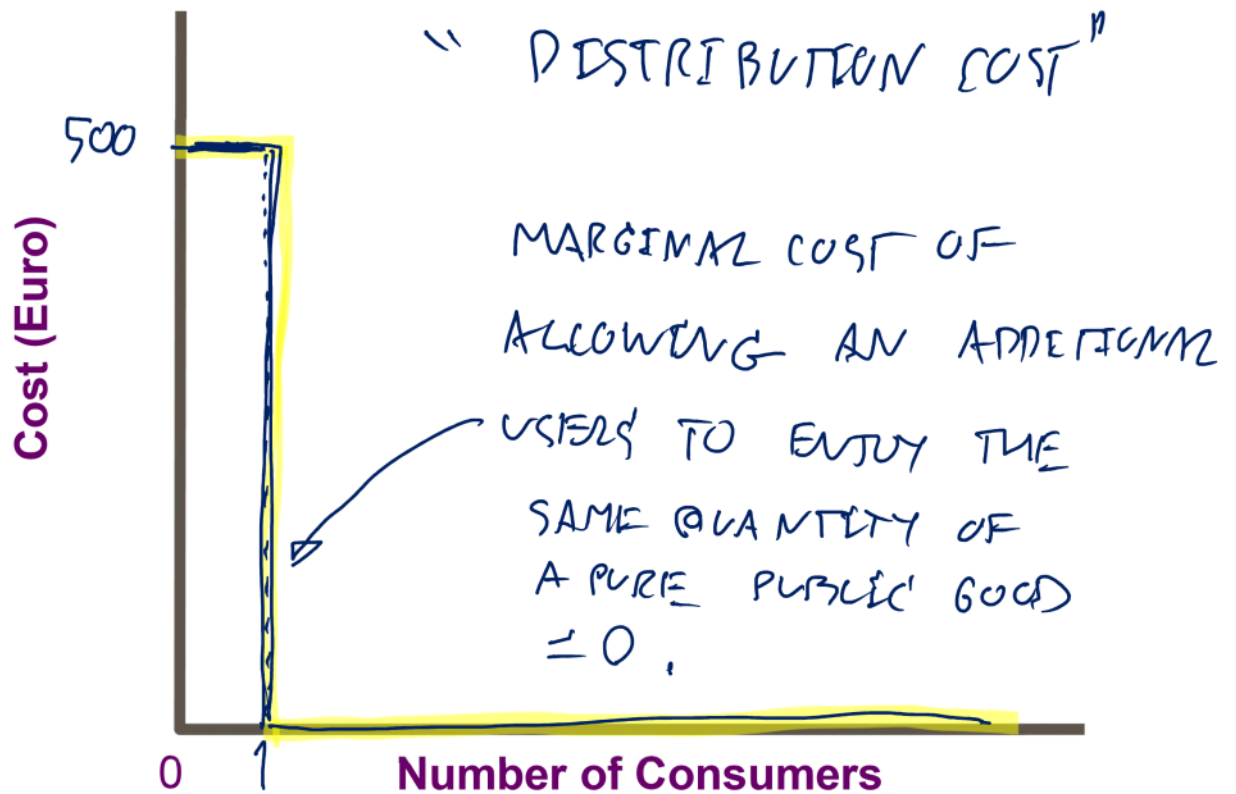
## Characteristics of Public Goods

- **Nonexclusion:** The inability of a seller to prevent people from consuming a good if they do not pay for it.

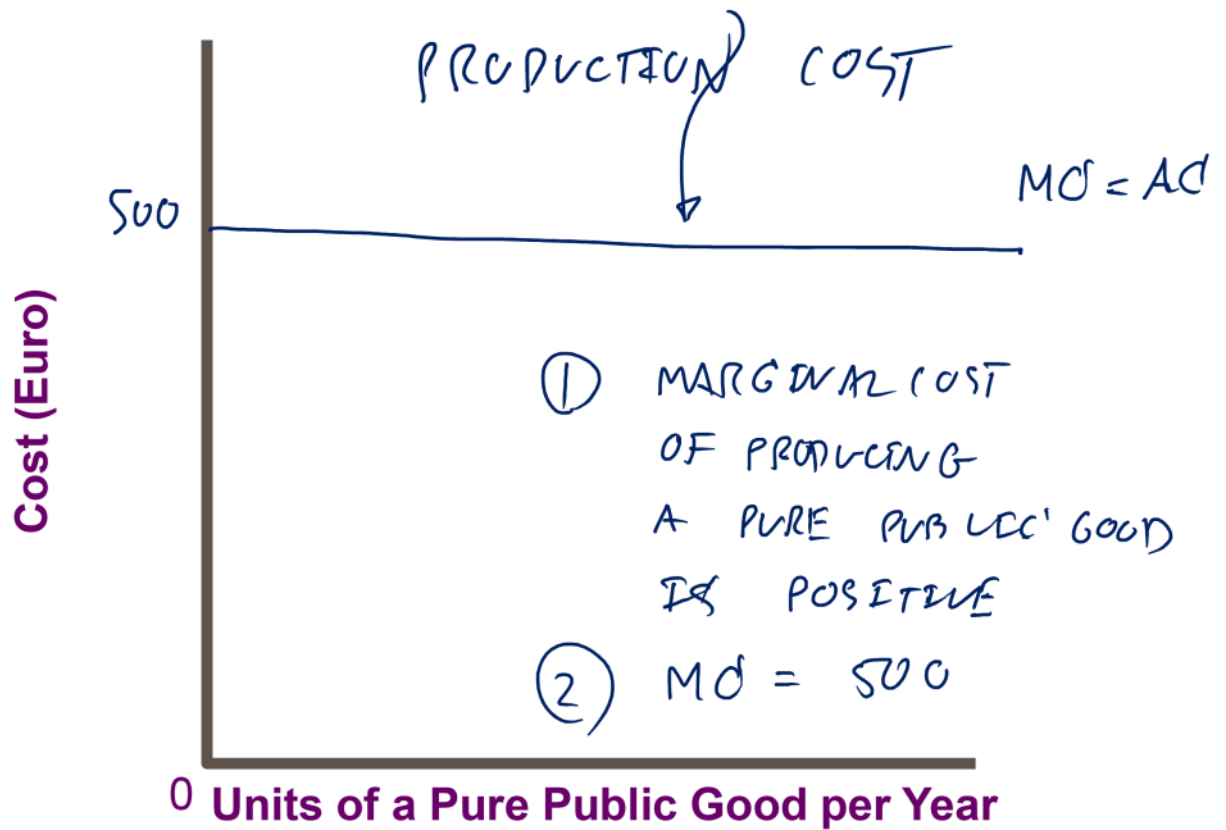
## Pure Public Goods and Pure Private Goods

- **Pure Public Good:** No ability to exclude and no rivalry for benefits.
- **Pure Private Good:** Clear ability to exclude and rivalry for benefits.

**Figure 4.1 Marginal Costs of Consuming and Producing a Pure Public Good**



**Figure 4.1 Marginal Costs of Consuming and Producing a Pure Public Good**



## Price Excludable Public Goods

- **Price-excludable public good:** there are external benefits when produced or consumed but exclusion is easy.

Examples:  
RIVALNESS : NO  
EXCLUDABLE : YES

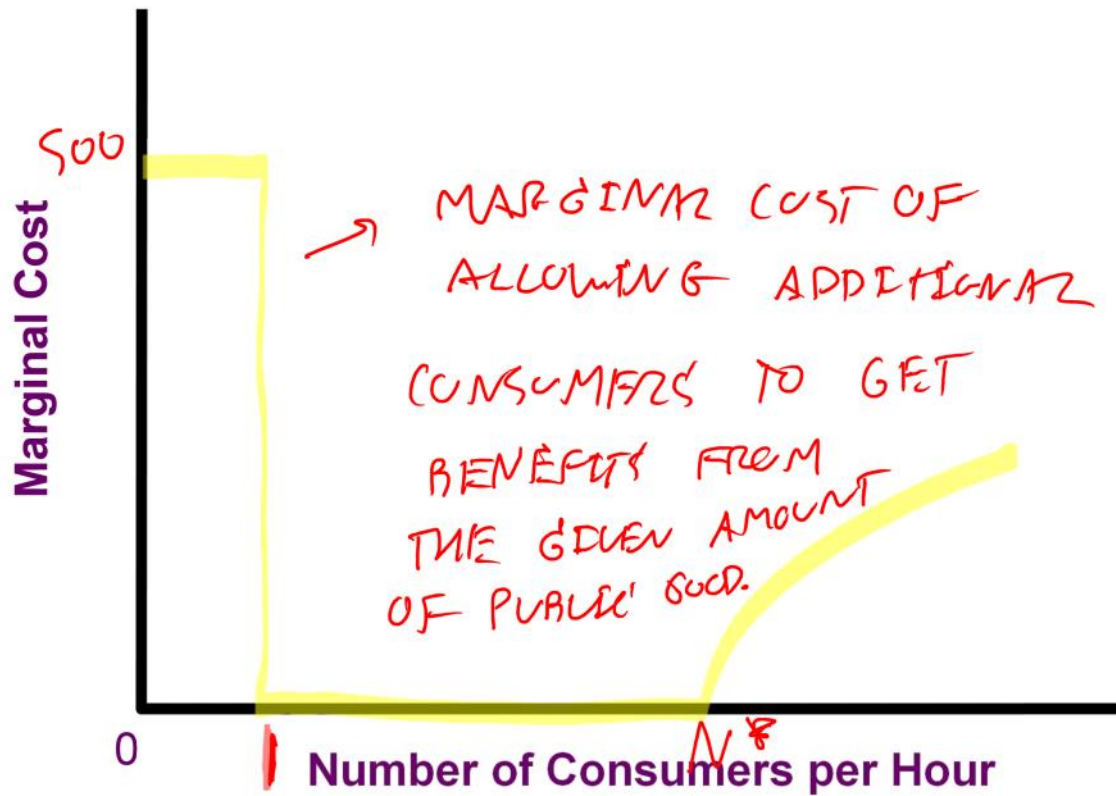
## Congestible Public Goods

- There are public goods where, after a point, the enjoyment received by the consumer is diminished by crowding or congestion. These are called **Congestible Public Goods**.

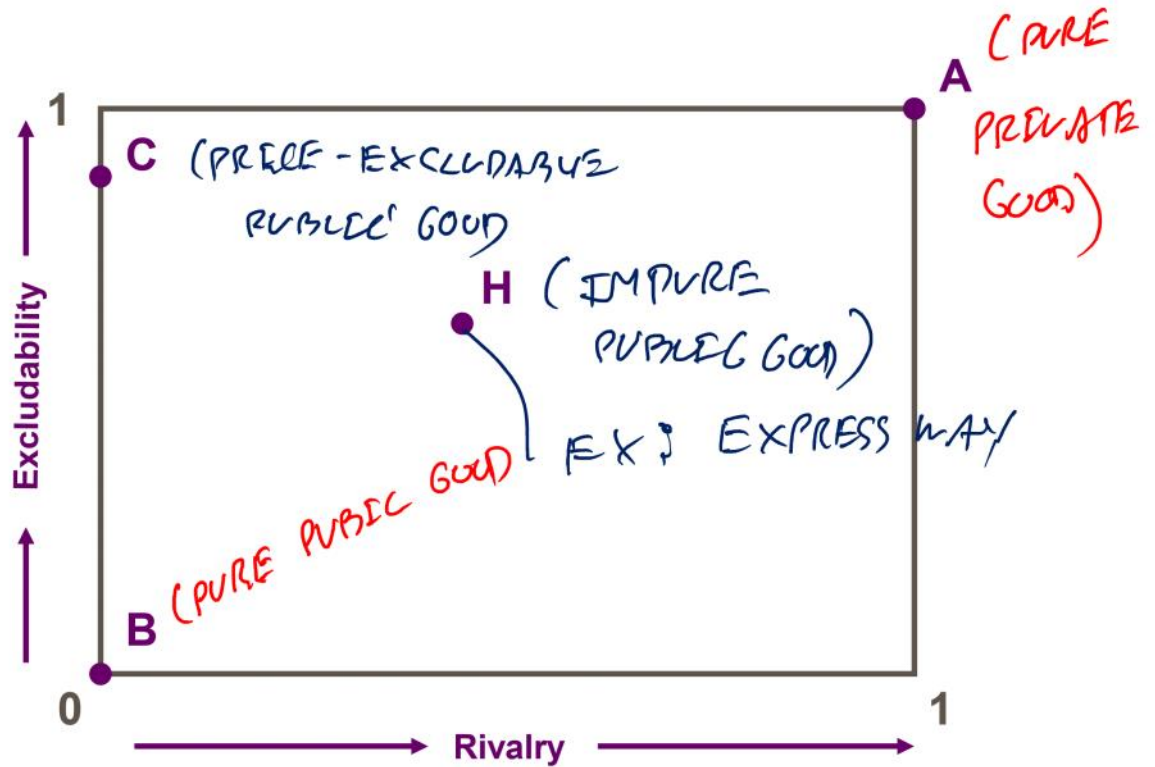
Examples:

PUBLIC PARKS  
FREE RENTS



**Figure 4.2 A Congestible Public Good**

## Classifying Goods According to the Degree of Rivalry and Excludability of Benefits from Their Use



## A TAXONOMY OF GOODS

|          | EXCLUDABLE                                        | NONEXCLUDABLE              |
|----------|---------------------------------------------------|----------------------------|
| RIVAL    | PURE PRIVATE<br>GOOD                              | CONGESTIBLE<br>PUBLIC GOOD |
| NONRIVAL | PRECE-<br>EXCLUDABLE<br>PUBLIC GOOD,<br>CLUB GOOD | PURE PUBLIC<br>GOOD        |

## SOME REMARKS ABOUT PUBLIC GOODS

- ① EVEN THOUGH EVERYONE CONSUME THE SAME QUANTITY, BUT IT IS NOT NECESSARY THAT EVERYONE WILL "VALUE" IT EQUALLY.
- ② CLASSIFICATION AS A PUBLIC GOOD IS NOT AN ABSOLUTE: IT DEPENDS ON MARKET CONDITIONS & STATE OF TECHNOLOGY.  
EX: LIGHTHOUSE PAST  
PRESENT

③ "PUBLIC GOOD" MIGHT BE PRODUCED  
EITHER BY PRIVATE OR BY  
PUBLIC SECTORS

EX: CHU WAT PARK, FLY OVER BRIDGE

④ "PRIVATE GOOD" MIGHT BE PRODUCED  
EITHER BY PRIVATE OR PUBLIC  
SECTORS

EX:

PUBLIC HOSPITALS

PUBLIC SCHOOLS

PUBLIC UNIVERSITIES

MRT

⑤ SOMETHING THAT ARE NOT  
CONVENTIONALLY THOUGHT AS  
COMMODITIES HAVE PUBLIC  
GOOD CHARACTERISTICS

EX) HONESTY, JUSTICE

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PURE PUBLIC GOODS

PURE PRIVATE GOODS

- RIVAL-EXCLUDABLE PUBLIC GOODS
  - CONGESTIBLE PUBLIC GOODS
- } "IMPURE" PUBLIC GOODS

## Efficient Provision of Private Goods

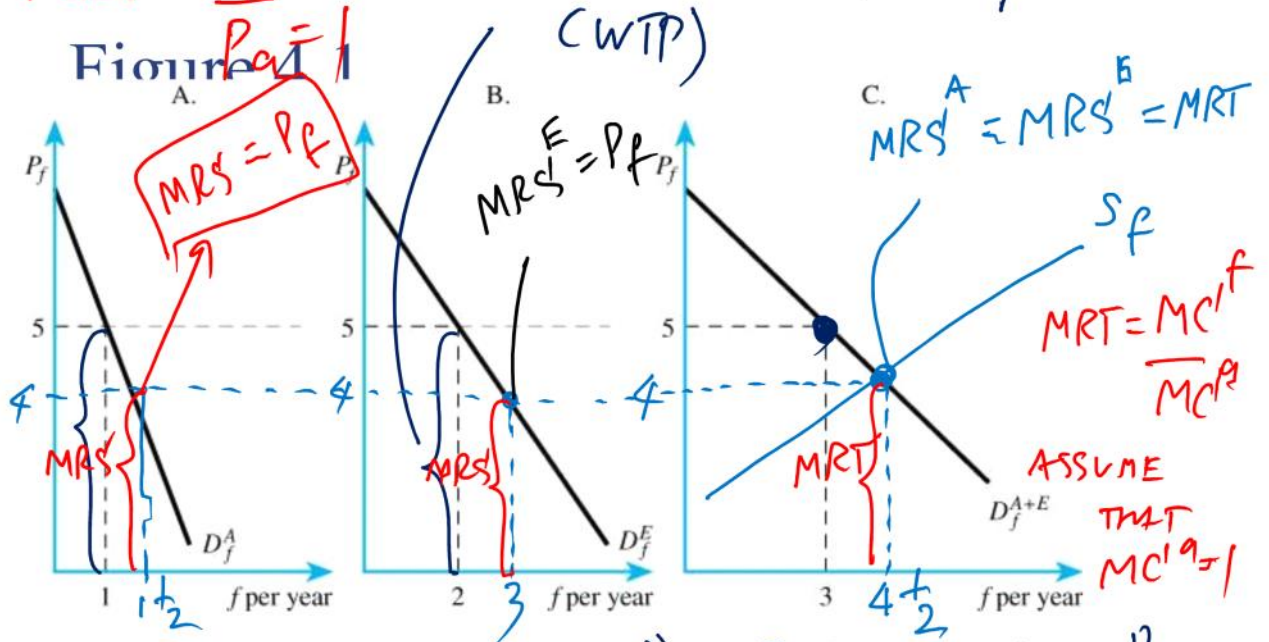
- Derivation of aggregate demand
- Each person's demand curve represents the willingness-to-pay for an additional unit of a good
- Private good: holding  $P$  constant, add together individual quantities to get  $Q$
- Horizontal summation

2 goods: fig leaves ( $f$ ) & apple ( $a$ )

$$MRS = \frac{P_f}{P_a}$$

WILLINGNESS TO PAY  
(WTP)

Figure 1



CONSUMERS CAN CONSUME "DIFFERENT AMOUNT"  
AT THE SAME PRICE



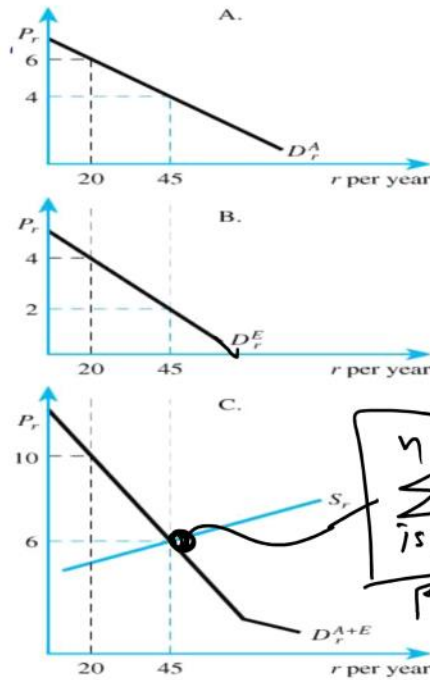
## Equilibrium in Private Goods Market

- Equilibrium where supply curve intersects aggregate demand curve
- Everyone pays the same price,  $P$
- Individuals consume different quantities,  $Q$
- Pareto efficient ;  $MRS^A = MRS^B = MRT$

## Efficient Provision of Public Goods

- Consider a fireworks display as a public good – it is nonrival and nonexcludable.
- Bigger displays give higher benefit.
- Public good: holding  $Q$  constant, add together individual willingness-to-pay to get  $P$ .
- Vertical summation.

Figure



$R \approx$  ROCKET  
DISPLAY

AT THE MOMENT,  
BOTH CURRENT  
CONSUME 19 UNITS  
OF  $R$ .

$$\sum_{i=1}^n MB_i = MC$$

FROM VERTICAL  
SUMMATION

## Efficiency in Public Goods Market

- Everyone consumes the same quantity,  $Q$ .
- Individual's marginal benefit varies.
- Efficiency requires that the *sum* of individual marginal benefits equals the marginal cost.

## Numerical Example

- Consider 2 individuals, Adam and Eve, who have the following inverse demand curves and face a marginal cost curve below.

$$P_A = 100 - \frac{1}{2} Q_A$$

$$P_E = 200 - Q_E$$

$$MC = \frac{2}{3} Q$$

## Numerical Example, Private Good

- If the good was a **private good**, then the aggregate demand curve is:

$$Q = Q_A + Q_E = (200 - 2P_A) + (200 - P_E)$$

With a **private good**, everyone pays the same price.

$$P = P_A = P_E$$

THE REFERENCE,  $\boxed{Q = 400 - 3P}$  22

$$P = \frac{400 - Q}{3}$$

$$= \frac{400}{3} - \frac{Q}{3}$$

$$P_A = 100 - \frac{1}{2} Q_A \Rightarrow Q_A = 200 - 2P_A$$

$$P_E = 200 - Q_E \Rightarrow Q_E = 200 - P_E$$

$$MC = \frac{2}{3} Q$$

$$Q_A = 200 - 2(88.8888) = 22.2222$$

$$Q_E = 200 - 88.8888 = 111.1111$$

$$Q = Q_A + Q_E = 133.3333$$

## Numerical Example, Private Good

- In a competitive market,  $P=MC$

$$P = MC \Rightarrow \frac{400}{3} - \frac{Q}{3} = \frac{2}{3} Q$$

$$Q = \frac{400}{3} \approx 133.$$

Approximately 133 units of the **private good** are provided at a price of 89.

Adam consumes around 22 units, and Eve consumes around 11 units.

$$Q = 400 - 3P.$$

$$133 = 400 - 3P$$

$$P = \frac{400 - 133}{3}$$

$$P = 89$$

$$P_A = 100 - \frac{1}{2} Q_A$$

$$P_E = 200 - Q_E$$

## Numerical Example, Public Good

- Suppose instead that the good is a **public good**.  
The aggregate demand curve is:

BY VERTICAL SUMMATION:  $P = P_A + P_E = \left(100 - \frac{1}{2}Q_A\right) + (200 - Q_E)$

With a **public good**, everyone consumes the same quantity.

$$Q = Q_A = Q_E$$

THEREFORE,  $P = \left(100 - \frac{1}{2}Q\right) + (200 - Q) = 300 - \frac{3}{2}Q$ .



## Numerical Example, Public Good

- Efficient provision would require:  $P=MC$

$$P = MC' \Rightarrow 300 - \frac{3}{2}Q = \frac{2}{3}Q$$

$$\frac{2}{3}Q + \frac{3}{2}Q = 300$$

$$\frac{4Q + 9Q}{6} = 300$$

Efficient provision would imply that Adam & Eve consume 138.46 units of the public good.

Private market may not arrive at this allocation, however.

$$\frac{13Q}{6} = 300$$

$$Q = 138.4615$$

UNITS / TIME PERIOD

25

$$P = ?$$

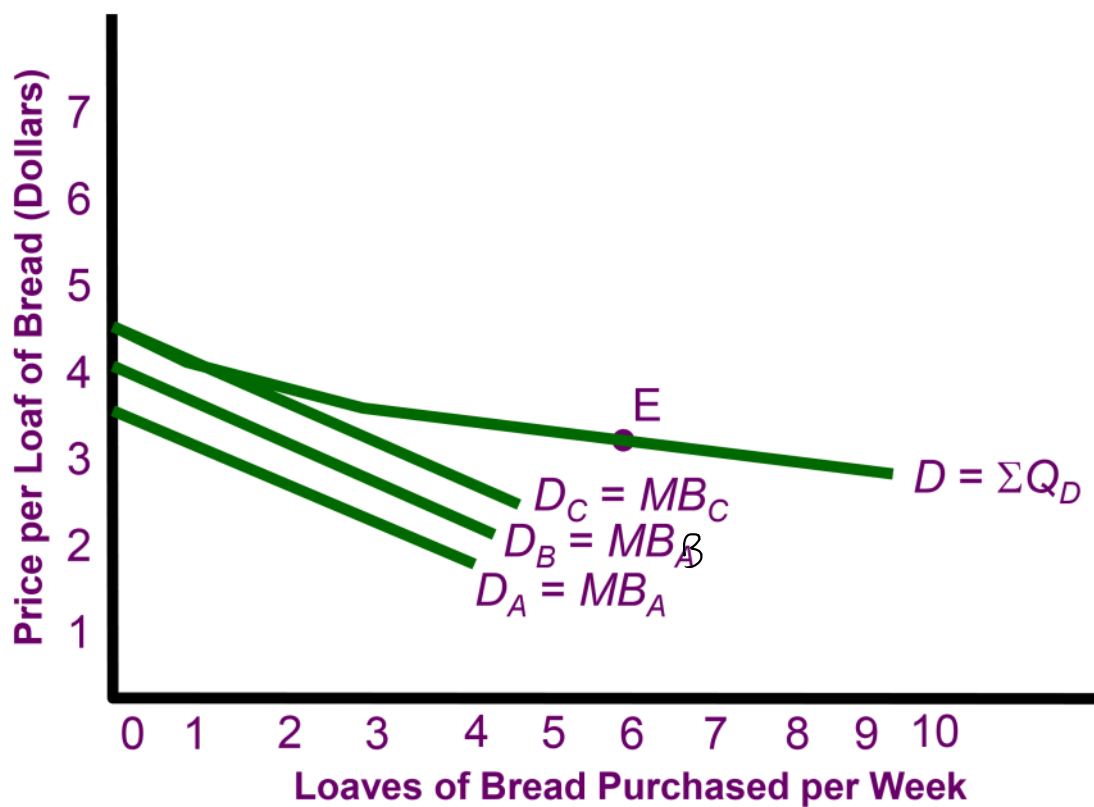
$$P = 300 - \frac{3}{2}Q$$

$$= 300 - \frac{3}{2}(138.4615)$$

$$= 300 - 207.6938$$

$$= 92.30625$$

## Another example on Demand For a Private Good



### Another Numerical Example on demand for a Pure Public Good

|             | Number of Security Guards per Week |       |       |       |
|-------------|------------------------------------|-------|-------|-------|
|             | 1                                  | 2     | 3     | 4     |
| $MB_A$      | \$300                              | \$250 | \$200 | \$150 |
| $MB_B$      | \$250                              | \$200 | \$150 | \$100 |
| $MB_C$      | \$200                              | \$150 | \$100 | \$50  |
| $\Sigma MB$ | \$750                              | \$600 | \$450 | \$300 |

MARGINAL  
SOCIAL

BENEFITS OF A PURE PUBLIC GOOD AT A GIVEN AMOUNT ( $\Sigma MB$ )

$$\Sigma MB = \sum_{i=1}^3 MB_i$$

- UNIT COST FOR  
A SECURITY GUARD = 450\$ / GUARD  
SO  $MC = AC = 450$

$Q=1: 750$  vs.  $450 \rightarrow$  EXCESS =  $750 - 450 = 300$

FOR  $Q=2$ : A WILL PAY  $250 \cdot 2 = 500$   
B " "  $200 \cdot 2 = 400$  VS  $450 \cdot 2 = 900$   
C " "  $150 \cdot 2 = 300$   
1200

FOR  $Q=3$ : A WILL PAY  $200 \cdot 3 = 600$   
" "  $150 \cdot 3 = 450$  VS  $450 \cdot 3 = 1350$   
" "  $100 \cdot 3 = 300$   
1350

LINDAHL PRICE: EQUILIBRIUM  
(TAX PRICE) CONTRIBUTIONS "PER UNIT" OF THE PUBLIC GOOD

- NO ONE WILL HIRE ANY SECURITY GUARD IF HE OR SHE HAS TO MAKE AN INDIVIDUAL PAYMENT.  
EX: EVEN MR A., HAS  $MB$  OF 1<sup>ST</sup> UNIT <  $MC$ .  
(300) (450)
- IT IS SOCIALLY **INEFFICIENT** IF NO SECURITY GUARD IS HIRED.  
OBSERVE THAT AT  $Q=1$ ,  $\Sigma MB > MC$   
(750) (450)

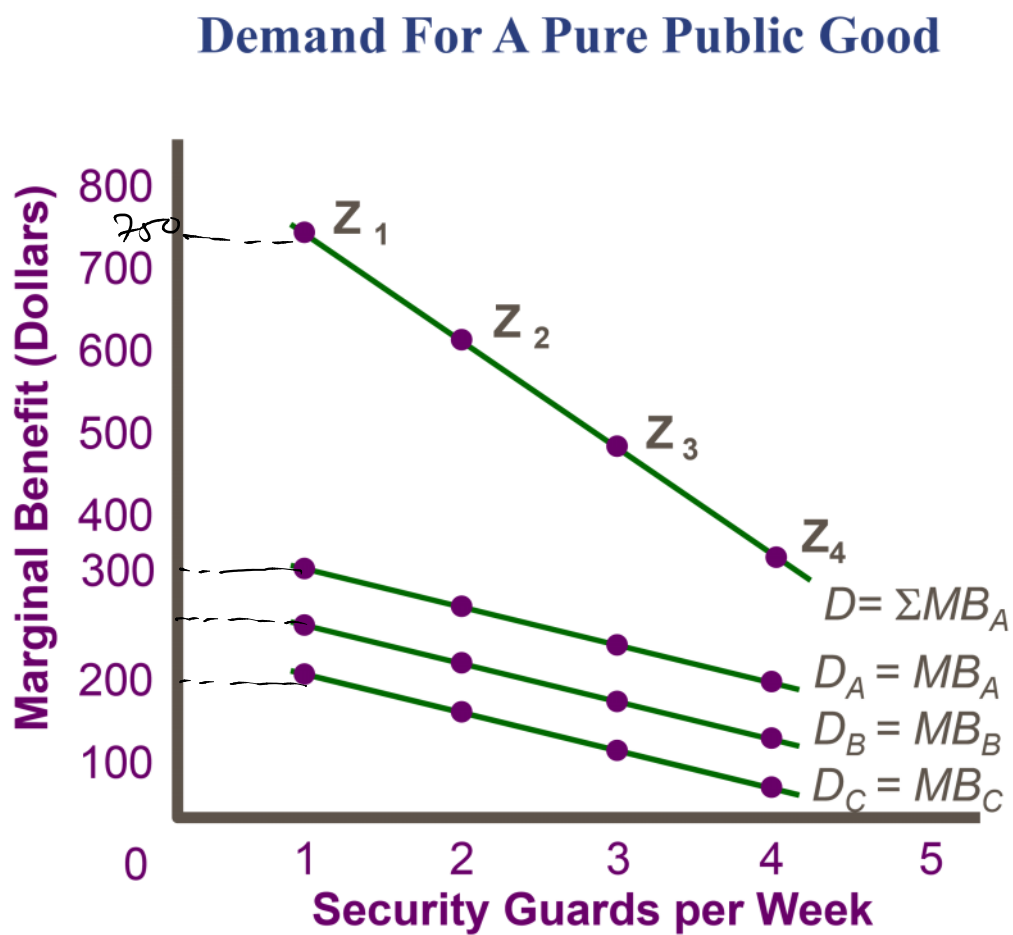
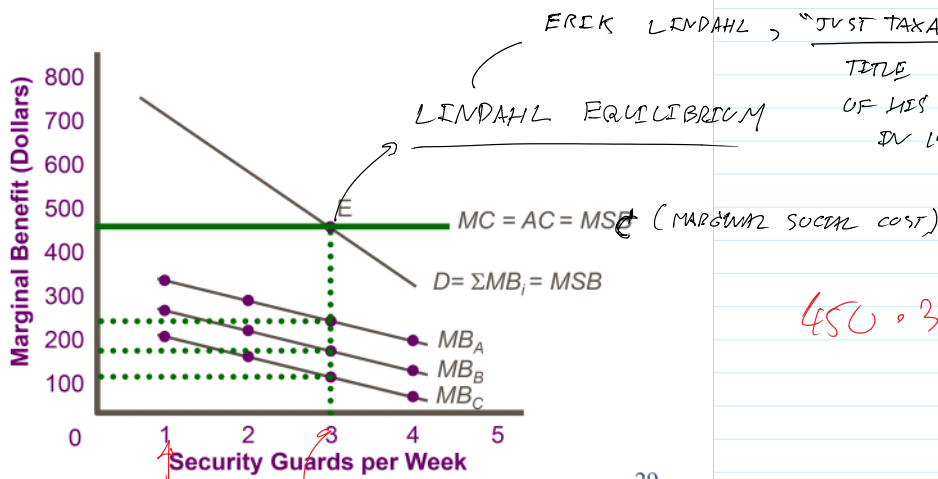


Figure 4.6 Efficient Output for a Pure Public Good



2 ISSUES

① TRUTHFUL REVELATION OF PREFERENCES

② # OF MEMBERS IN THE COMMUNITY (OR SOCIETY)

$450 \cdot 3 = 1350$  ✓

FACT #3

AN OPTIMAL QUANTITY OF A PUBLIC GOOD = 3 WARDEN

$\sum_{i=1}^3 MB_i = MSC$  AT EFFICIENT AMOUNT OF PUBLIC GOOD

WHEN  $Q < 3$ ,  $\sum MB > MSC$ . THEN MORE OF SECURITY GUARD SHOULD BE HIRED.

WHEN  $Q > 3$ ,  $\sum MB < MSC$ . THEN NO FURTHER AMOUNT SHOULD BE HIRED.

$MSB = MB_i + \sum_{j=1}^{n-1} MB_j$

MARGINAL BENEFIT RECEIVING BY ANY ONE IN THE COMMUNITY

MARGINAL BENEFIT RECEIVING BY

REMAINING MEMBERS OF THE COMMUNITY

REFLECTS

NATURES OF PUBLIC

GOOD: NONRIVAL IN CONSUMPTION + NONEXCLUDABLE IN CONSUMPTION

## Efficient Output of a Pure Public Good

- The socially optimal level of the public good requires that we set the Marginal Social Benefit of that good equal to its Marginal Social Cost.  $MSB = MSC$

- $MSB = MB_i + \sum_{j=1}^{n-1} MB_j = MSC$

## Mathematically: Lindahl Pricing

Recall from Figure 4.5 that the marginal social benefit for a pure public good is the sum of the individual marginal benefits.

That is:  $MSB = \sum MB.$

Efficient output is therefore:

$$MSB = \sum MB = MSC.$$

## Lindahl Equilibrium

- The amount each person contributes,  $t_i$ , depends on individual desires for the public good.
- The sum of the contributions equals the total cost of the public good.
  - $\sum t_i Q^* = MC(Q^*) = AC(Q^*)$
  - $\sum t_i = MC = AC$
- All individuals agree to pay their shares.



## Freeriding

- **Freeriding** occurs when people are not honest in stating their Marginal Benefit, because if they understate it, they can get a slightly reduced level of the public good while paying nothing for it.

## Freeriding is easier with

- **Anonymity:** If everyone knows who contributes, there can be powerful social stigmas applied to shirkers.
- **Large numbers of people:**