

SECOND EDITION

Stephen A. Ross
Randolph W. Westerfield
Bradford D. Jordan
Joseph Lim
Ruth Tan

FUNDAMENTALS

OF *Corporate*
FINANCE



ASIA GLOBAL EDITION



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CHAPTER 5

INTRODUCTION TO VALUATION: TIME VALUE OF MONEY (CALCULATOR)

KEY CONCEPTS AND SKILLS

- Be able to compute the future value of an investment made today
- Be able to compute the present value of cash to be received at some future date
- Be able to compute the return on an investment
- Be able to compute the number of periods that equates a present value and a future value given an interest rate
- Be able to use a financial calculator and a spreadsheet to solve time value of money problems

CHAPTER OUTLINE

- Future Value and Compounding
- Present Value and Discounting
- More about Present and Future Values

BASIC DEFINITIONS

- Present Value – earlier money on a time line
- Future Value – later money on a time line
- Interest rate – “exchange rate” between earlier money and later money
 - Discount rate
 - Cost of capital
 - Opportunity cost of capital
 - Required return

FUTURE VALUES – EXAMPLE 1

- Suppose you invest \$1,000 for one year at 5% per year. What is the future value in one year?
 - Interest = $1,000(.05) = 50$
 - Value in one year = principal + interest = $1,000 + 50 = 1,050$
 - Future Value (FV) = $1,000(1 + .05) = 1,050$
- Suppose you leave the money in for another year. How much will you have two years from now?
 - FV = $1,000(1.05)(1.05) = 1,000(1.05)^2 = 1,102.50$

FUTURE VALUES: GENERAL FORMULA

- $FV = PV(1 + r)^t$
 - FV = future value
 - PV = present value
 - r = period interest rate, expressed as a decimal
 - t = number of periods
- Future value interest factor = $(1 + r)^t$

EFFECTS OF COMPOUNDING

- Simple interest vs. Compound interest
- Consider the previous example
 - FV with simple interest = $1,000 + 50 + 50 = 1,100$
 - FV with compound interest = $1,102.50$
 - The extra 2.50 comes from the interest of $.05(50) = 2.50$ earned on the first interest payment

CALCULATOR KEYS

- Texas Instruments BA-II Plus
 - FV = future value
 - PV = present value
 - I/Y = period interest rate
 - P/Y must equal 1 for the I/Y to be the period rate
 - Interest is entered as a percent, not a decimal
 - N = number of periods
 - Remember to clear the registers (CLR TVM) after each problem
 - Other calculators are similar in format

FUTURE VALUES – EXAMPLE 2

- Suppose you invest the \$1,000 from the previous example for 5 years. How much would you have?
 - 5 N; 5 I/Y; 1,000 PV
 - CPT FV = -1,276.28
- The effect of compounding is small for a small number of periods, but increases as the number of periods increases. (Simple interest would have a future value of \$1,250, for a difference of \$26.28.)

FUTURE VALUES – EXAMPLE 3

- Suppose you had a relative deposit \$10 at 5.5% interest 200 years ago. How much would the investment be worth today?
 - 200 N; 5.5 I/Y; 10 PV
 - CPT FV = -447,189.84
- What is the effect of compounding?
 - Simple interest = $10 + 200(10)(.055) = 120.00$
 - Compounding added \$447,069.84 to the value of the investment

FUTURE VALUE AS A GENERAL GROWTH FORMULA

- Suppose your company expects to increase unit sales of widgets by 15% per year for the next 5 years. If you sell 3 million widgets in the current year, how many widgets do you expect to sell in the fifth year?
 - 5 N; 15 I/Y; 3,000,000 PV
 - CPT FV = -6,034,072 units
(remember the sign convention)

QUICK QUIZ - PART I

- What is the difference between simple interest and compound interest?
- Suppose you have \$500 to invest and you believe that you can earn 8% per year over the next 15 years.
 - How much would you have at the end of 15 years using compound interest?
 - How much would you have using simple interest?

PRESENT VALUES

- How much do I have to invest today to have some amount in the future?
 - $FV = PV(1 + r)^t$
 - Rearrange to solve for $PV = FV / (1 + r)^t$
- When we talk about discounting, we mean finding the present value of some future amount.
- When we talk about the “value” of something, we are talking about the present value unless we specifically indicate that we want the future value.

PRESENT VALUE - ONE PERIOD EXAMPLE

- Suppose you need \$10,000 in one year for the down payment on a new car. If you can earn 7% annually, how much do you need to invest today?
- $PV = 10,000 / (1.07)^1 = 9,345.79$
- Calculator
 - 1 N
 - 7 I/Y
 - 10,000 FV
 - CPT PV = -9,345.79

PRESENT VALUES – EXAMPLE 2

- You want to begin saving for your daughter's college education and you estimate that she will need \$150,000 in 17 years. If you feel confident that you can earn 8% per year, how much do you need to invest today?
 - $N = 17; I/Y = 8; FV = 150,000$
 - CPT PV = -40,540.34 (remember the sign convention)

PRESENT VALUES – EXAMPLE 3

- Your parents set up a trust fund for you 10 years ago that is now worth \$19,671.51. If the fund earned 7% per year, how much did your parents invest?
 - $N = 10; I/Y = 7; FV = 19,671.51$
 - $\text{CPT PV} = -10,000$

PRESENT VALUE – IMPORTANT RELATIONSHIP I

- For a given interest rate – the longer the time period, the lower the present value
 - What is the present value of \$500 to be received in 5 years? 10 years? The discount rate is 10%
 - 5 years: $N = 5$; $I/Y = 10$; $FV = 500$
CPT PV = -310.46
 - 10 years: $N = 10$; $I/Y = 10$; $FV = 500$
CPT PV = -192.77

PRESENT VALUE - IMPORTANT RELATIONSHIP II

- For a given time period – the higher the interest rate, the smaller the present value
 - What is the present value of \$500 received in 5 years if the interest rate is 10%? 15%?
 - Rate = 10%; $N = 5$; $I/Y = 10$; $FV = 500$
CPT PV = -310.46
 - Rate = 15%; $N = 5$; $I/Y = 15$; $FV = 500$
CPT PV = -248.59

QUICK QUIZ - PART II

- What is the relationship between present value and future value?
- Suppose you need \$15,000 in 3 years. If you can earn 6% annually, how much do you need to invest today?
- If you could invest the money at 8%, would you have to invest more or less than at 6%? How much?

THE BASIC PV EQUATION - REFRESHER

- $PV = FV / (1 + r)^t$
- There are four parts to this equation
 - PV, FV, r and t
 - If we know any three, we can solve for the fourth
- If you are using a financial calculator, be sure to remember the sign convention or you will receive an error (or a nonsense answer) when solving for r or t

DISCOUNT RATE

- Often we will want to know what the implied interest rate is on an investment
- Rearrange the basic PV equation and solve for r
 - $FV = PV(1 + r)^t$
 - $r = (FV / PV)^{1/t} - 1$
- If you are using formulas, you will want to make use of both the y^x and the $1/x$ keys

DISCOUNT RATE - EXAMPLE 1

- You are looking at an investment that will pay \$1,200 in 5 years if you invest \$1,000 today. What is the implied rate of interest?
 - $r = (1,200 / 1,000)^{1/5} - 1 = .03714 = 3.714\%$
 - Calculator – the sign convention matters!!!
 - $N = 5$
 - $PV = -1,000$ (you pay 1,000 today)
 - $FV = 1,200$ (you receive 1,200 in 5 years)
 - $CPT I/Y = 3.714\%$

DISCOUNT RATE - EXAMPLE 2

- Suppose you are offered an investment that will allow you to double your money in 6 years. You have \$10,000 to invest. What is the implied rate of interest?
 - $N = 6$
 - $PV = -10,000$
 - $FV = 20,000$
 - $\text{CPT } I/Y = 12.25\%$

DISCOUNT RATE - EXAMPLE 3

- Suppose you have a 1-year old son and you want to provide \$75,000 in 17 years towards his college education.
 - You currently have \$5,000 to invest.
 - What interest rate must you earn to have the \$75,000 when you need it?
- $N = 17; PV = -5,000; FV = 75,000$
- $CPT I/Y = 17.27\%$

QUICK QUIZ – PART III

- What are some situations in which you might want to know the implied interest rate?
- You are offered the following investments:
 - You can invest \$500 today and receive \$600 in 5 years. The investment is considered low risk.
 - You can invest the \$500 in a bank account paying 4%.
 - What is the implied interest rate for the first choice and which investment should you choose?

FINDING THE NUMBER OF PERIODS

- Start with the basic equation and solve for t (remember your logs)
 - $FV = PV(1 + r)^t$
 - $t = \ln(FV / PV) / \ln(1 + r)$
- You can use the financial keys on the calculator as well; just remember the sign convention.

NUMBER OF PERIODS - EXAMPLE 1

- You want to purchase a new car, and you are willing to pay \$20,000.
 - If you can invest at 10% per year and you currently have \$15,000, how long will it be before you have enough money to pay cash for the car?
 - $I/Y = 10$; $PV = -15,000$; $FV = 20,000$
 - $CPT N = 3.02$ years

NUMBER OF PERIODS – EXAMPLE 2

- Suppose you want to buy a new house.
 - You currently have \$15,000, and you figure you need to have a 10% down payment plus an additional 5% of the loan amount for closing costs.
 - Assume the type of house you want will cost about \$150,000 and you can earn 7.5% per year.
 - How long will it be before you have enough money for the down payment and closing costs?

NUMBER OF PERIODS – EXAMPLE 2

CONTINUED

- How much do you need to have in the future?
 - Down payment = $.1(150,000) = 15,000$
 - Closing costs = $.05(150,000 - 15,000) = 6,750$
 - Total needed = $15,000 + 6,750 = 21,750$
- Compute the number of periods
- Using a financial calculator:
 - $PV = -15,000$; $FV = 21,750$; $I/Y = 7.5$
 - $CPT N = 5.14$ years
- Using the formula:
 - $t = \ln(21,750 / 15,000) / \ln(1.075) = 5.14$ years

QUICK QUIZ – PART IV

- When might you want to compute the number of periods?
- Suppose you want to buy some new furniture for your family room.
 - You currently have \$500, and the furniture you want costs \$600.
 - If you can earn 6%, how long will you have to wait if you don't add any additional money?

SPREADSHEET EXAMPLE

- Use the following formulas for TVM calculations
 - $FV(\text{rate}, \text{nper}, \text{pmt}, \text{pv})$
 - $PV(\text{rate}, \text{nper}, \text{pmt}, \text{fv})$
 - $RATE(\text{nper}, \text{pmt}, \text{pv}, \text{fv})$
 - $NPER(\text{rate}, \text{pmt}, \text{pv}, \text{fv})$
- The formula icon is very useful when you can't remember the exact formula
- Click on the Excel icon to open a spreadsheet containing four different examples.



WORK THE WEB EXAMPLE

- Many financial calculators are available online
- -
- Go to Investopedia's web site
<http://www.investopedia.com/calculator/>
and work the following example:
 - You need \$50,000 in 10 years. If you can earn 6% interest, how much do you need to invest today?
 - You should get \$27,919.74



TABLE 5.4

I. Symbols:

PV = Present value, what future cash flows are worth today

FV_t = Future value, what cash flows are worth in the future

r = Interest rate, rate of return, or discount rate per period—typically, but not always, one year

t = Number of periods—typically, but not always, the number of years

C = Cash amount

II. Future Value of C Invested at r Percent for t Periods:

$$FV_t = C \times (1 + r)^t$$

The term $(1 + r)^t$ is called the *future value factor*.

III. Present Value of C to Be Received in t Periods at r Percent per Period:

$$PV = C / (1 + r)^t$$

The term $1 / (1 + r)^t$ is called the *present value factor*.

IV. The Basic Present Value Equation Giving the Relationship between Present and Future Value:

$$PV = FV_t / (1 + r)^t$$

COMPREHENSIVE PROBLEM

- You have \$10,000 to invest for five years.
- How much additional interest will you earn if the investment provides a 5% annual return, when compared to a 4.5% annual return?
- How long will it take your \$10,000 to double in value if it earns 5% annually?
- What annual rate has been earned if \$1,000 grows into \$4,000 in 20 years?

CHAPTER 5 - CALCULATOR

END OF CHAPTER