

Long-Run Elasticity	Seasonally Adjusted	Stochastic Process
Long-Run Multiplier	Serial Correlation	Strictly Exogenous
Long-Run Propensity (LRP)	Short-Run Elasticity	Time Series Process
Seasonal Dummy Variables	Spurious Regression Problem	Time Trend
Seasonality	Static Model	

## Problems

1. Decide if you agree or disagree with each of the following statements and give a brief explanation of your decision:
  - (i) Like cross-sectional observations, we can assume that most time series observations are independently distributed.
  - (ii) The OLS estimator in a time series regression is unbiased under the first three Gauss-Markov assumptions.
  - (iii) A trending variable cannot be used as the dependent variable in multiple regression analysis.
  - (iv) Seasonality is not an issue when using annual time series observations.

2. Suppose that, for a province or district, the crime rate,  $crime_t$ , is a two-year distributed lag of the clear-up rate (percentage of crimes resulting in a conviction):

$$crime_t = \alpha_0 + \delta_0 clearup_t + \delta_1 clearup_{t-1} + \delta_2 clearup_{t-2} + u_t,$$

where  $u_t$  is uncorrelated with  $clearup_t$ ,  $clearup_{t-1}$ ,  $clearup_{t-2}$ , and all other past values of the arrest rate. Suppose that, through expenditures on law enforcement, the clear-up rate can be made to react to last year's crime rate:

$$clearup_t = \gamma_0 + \gamma_1 crime_{t-1} + v_t.$$

- (i) Explain, in behavioral terms, what  $\gamma_1 > 0$  means.
  - (ii) If  $v_t$  is uncorrelated with all past values of  $clearup_t$  and  $u_t$ , argue that  $clearup_t$  and  $u_{t-1}$  must be correlated. (*Hint*: Lag the first equation one period and substitute for  $crime_{t-1}$  in the second equation.)
  - (iii) Which Gauss-Markov assumption does  $\text{Corr}(clearup_t, u_{t-1}) \neq 0$  violate?
3. Suppose  $y_t$  follows a second order FDL model:

$$y_t = \alpha_0 + \delta_0 z_t + \delta_1 z_{t-1} + \delta_2 z_{t-2} + u_t.$$

Let  $z^*$  denote the *equilibrium value* of  $z_t$  and let  $y^*$  be the equilibrium value of  $y_t$ , such that

$$y^* = \alpha_0 + \delta_0 z^* + \delta_1 z^* + \delta_2 z^*.$$

Show that the change in  $y^*$ , due to a change in  $z^*$ , equals the long-run propensity times the change in  $z^*$ :

$$\Delta y^* = LRP \cdot \Delta z^*.$$

This gives an alternative way of interpreting the LRP.

**PART 2** Regression Analysis with Time Series Data

4. When the three event indicators *befile6*, *affile6*, and *afdec6* are dropped from equation (10.22), we obtain  $R^2 = .281$  and  $\bar{R}^2 = .264$ . Are the event indicators jointly significant at the 10% level?
5. Suppose you have quarterly data on new housing starts, interest rates, and real per capita income. Specify a model for housing starts that accounts for possible trends and seasonality in the variables.
6. In Example 10.4, we saw that our estimates of the individual lag coefficients in a distributed lag model were very imprecise. One way to alleviate the multicollinearity problem is to assume that the  $\delta_j$  follow a relatively simple pattern. For concreteness, consider a model with four lags:

$$y_t = \alpha_0 + \delta_0 z_t + \delta_1 z_{t-1} + \delta_2 z_{t-2} + \delta_3 z_{t-3} + \delta_4 z_{t-4} + u_t.$$

Now, let us assume that the  $\delta_j$  follow a quadratic in the lag,  $j$ :

$$\delta_j = \gamma_0 + \gamma_1 j + \gamma_2 j^2,$$

for parameters  $\gamma_0$ ,  $\gamma_1$ , and  $\gamma_2$ . This is an example of a *polynomial distributed lag (PDL) model*.

- (i) Plug the formula for each  $\delta_j$  into the distributed lag model and write the model in terms of the parameters  $\gamma_h$ , for  $h = 0, 1, 2$ .
  - (ii) Explain the regression you would run to estimate the  $\gamma_h$ .
  - (iii) The polynomial distributed lag model is a restricted version of the general model. How many restrictions are imposed? How would you test these? (*Hint*: Think  $F$  test.)
7. In Example 10.4, we wrote the model that explicitly contains the long-run propensity,  $\theta_0$ , as

$$gfr_t = \alpha_0 + \theta_0 pe_t + \delta_1(pe_{t-1} - pe_t) + \delta_2(pe_{t-2} - pe_t) + u_t,$$

where we omit the other explanatory variables for simplicity. As always with multiple regression analysis,  $\theta_0$  should have a *ceteris paribus* interpretation. Namely, if  $pe_t$  increases by one (dollar) holding  $(pe_{t-1} - pe_t)$  and  $(pe_{t-2} - pe_t)$  fixed,  $gfr_t$  should change by  $\theta_0$ .

- (i) If  $(pe_{t-1} - pe_t)$  and  $(pe_{t-2} - pe_t)$  are held fixed but  $pe_t$  is increasing, what must be true about changes in  $pe_{t-1}$  and  $pe_{t-2}$ ?
- (ii) How does your answer in part (i) help you to interpret  $\theta_0$  in the above equation as the LRP?

## Computer Exercises

- 10.1 In October 1979, the Federal Reserve changed its policy of targeting the money supply and instead began to focus directly on short-term interest rates. Using the data in INTDEF.RAW, define a dummy variable equal to 1 for years after 1979. Include this dummy in equation (10.15) to see if there is a shift in the interest rate equation after 1979. What do you conclude?
- 10.2 Use the data in BARIUM.RAW for this exercise.
  - (i) Add a linear time trend to equation (10.22). Are any variables, other than the trend, statistically significant?
  - (ii) In the equation estimated in part (i), test for joint significance of all variables except the time trend. What do you conclude?