

$$\ln S_t = \beta_{10} + \beta_{11} \ln P_{Dt} + \beta_{12} \ln P_{X2t} + \beta_{13} \ln P_{X3t} + \beta_{14} \ln P_{X4t} + \varepsilon_{1t} \quad \text{I}$$

$$\ln D_t = \beta_{20} + \beta_{21} \ln P_{Dt} + \beta_{22} \ln GDP_t + \varepsilon_{2t} \quad \text{II}$$

Endogenous variables in this system include S_t , D_t , and P_{Dt}

Exogenous variables in this system include P_{X2t} , P_{X3t} , P_{X4t} , and GDP_t

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Assume demand = supply or $\ln S_t = \ln D_t \quad \text{III}$

$$\beta_{10} + \beta_{11} \ln P_{Dt} + \beta_{12} \ln P_{X2t} + \beta_{13} \ln P_{X3t} + \beta_{14} \ln P_{X4t} = \beta_{20} + \beta_{21} \ln P_{Dt} + \beta_{22} \ln GDP_t$$

$$\beta_{11} \ln P_{Dt} - \beta_{21} \ln P_{Dt} = -\beta_{10} + \beta_{20} - \beta_{12} \ln P_{X2t} - \beta_{13} \ln P_{X3t} - \beta_{14} \ln P_{X4t} + \beta_{22} \ln GDP_t + \varepsilon_{2t} - \varepsilon_{1t}$$

$$(\beta_{11} - \beta_{21}) \ln P_{Dt} = \beta_{20} - \beta_{10} + \beta_{22} \ln GDP_t - \beta_{12} \ln P_{X2t} - \beta_{13} \ln P_{X3t} - \beta_{14} \ln P_{X4t} + \varepsilon_{2t} - \varepsilon_{1t}$$

$$\ln P_{Dt} = \frac{\beta_{20} - \beta_{10}}{\beta_{11} - \beta_{21}} + \frac{\beta_{22}}{\beta_{11} - \beta_{21}} \ln GDP_t - \frac{\beta_{12}}{\beta_{11} - \beta_{21}} \ln P_{X2t} - \frac{\beta_{13}}{\beta_{11} - \beta_{21}} \ln P_{X3t} - \frac{\beta_{14}}{\beta_{11} - \beta_{21}} \ln P_{X4t} + \frac{\varepsilon_{2t} - \varepsilon_{1t}}{\beta_{11} - \beta_{21}} \quad \text{IV}$$

Put value IV into II

$$\ln D_t = \beta_{20} + \frac{\beta_{21} (\beta_{20} - \beta_{10})}{\beta_{11} - \beta_{21}} + \frac{\beta_{21} \beta_{22} \ln GDP_t}{\beta_{11} - \beta_{21}} - \frac{\beta_{21} \beta_{12} \ln P_{X2t}}{\beta_{11} - \beta_{21}} - \frac{\beta_{21} \beta_{13} \ln P_{X3t}}{\beta_{11} - \beta_{21}} - \frac{\beta_{21} \beta_{14} \ln P_{X4t}}{\beta_{11} - \beta_{21}} + \frac{\beta_{21} (\varepsilon_{2t} - \varepsilon_{1t})}{\beta_{11} - \beta_{21}} + \beta_{22} \ln GDP_t + \varepsilon_{2t}$$

$$= \beta_{20} + \frac{\beta_{21} (\beta_{20} - \beta_{10})}{\beta_{11} - \beta_{21}} + \frac{\beta_{21} \beta_{22} \ln GDP_t}{\beta_{11} - \beta_{21}} - \frac{\beta_{21} \beta_{12} \ln P_{X2t}}{\beta_{11} - \beta_{21}} - \frac{\beta_{21} \beta_{13} \ln P_{X3t}}{\beta_{11} - \beta_{21}} - \frac{\beta_{21} \beta_{14} \ln P_{X4t}}{\beta_{11} - \beta_{21}} + \frac{\beta_{21} (\varepsilon_{2t} - \varepsilon_{1t})}{\beta_{11} - \beta_{21}} + \varepsilon_{2t} \quad \text{V}$$

use π_{ij}

$$\pi_{20} = \beta_{20} + \frac{\beta_{21} (\beta_{20} - \beta_{10})}{\beta_{11} - \beta_{21}}, \quad \pi_{21} = \frac{\beta_{21} \beta_{22}}{\beta_{11} - \beta_{21}}, \quad \pi_{22} = -\frac{\beta_{21} \beta_{12}}{\beta_{11} - \beta_{21}}, \quad \pi_{23} = -\frac{\beta_{21} \beta_{13}}{\beta_{11} - \beta_{21}}, \quad \pi_{24} = -\frac{\beta_{21} \beta_{14}}{\beta_{11} - \beta_{21}}$$

$$w_{2t} = \frac{\beta_{21} (\varepsilon_{2t} - \varepsilon_{1t})}{\beta_{11} - \beta_{21}} + \varepsilon_{2t}$$

Put value IV into I

$$\ln S_t = \beta_{10} + \frac{\beta_{11} (\beta_{20} - \beta_{10})}{\beta_{11} - \beta_{21}} + \frac{\beta_{11} \beta_{22} \ln GDP_t}{\beta_{11} - \beta_{21}} - \frac{\beta_{11} \beta_{12} \ln P_{X2t}}{\beta_{11} - \beta_{21}} - \frac{\beta_{11} \beta_{13} \ln P_{X3t}}{\beta_{11} - \beta_{21}} - \frac{\beta_{11} \beta_{14} \ln P_{X4t}}{\beta_{11} - \beta_{21}} + \beta_{12} \ln P_{X2t} + \beta_{13} \ln P_{X3t} + \beta_{14} \ln P_{X4t} + \frac{\beta_{11} (\varepsilon_{2t} - \varepsilon_{1t})}{\beta_{11} - \beta_{21}} + \varepsilon_{1t}$$

$$= \beta_{10} + \frac{\beta_{11} (\beta_{20} - \beta_{10})}{\beta_{11} - \beta_{21}} + \frac{\beta_{11} \beta_{22} \ln GDP_t}{\beta_{11} - \beta_{21}} - \frac{\beta_{11} \beta_{12} \ln P_{X2t}}{\beta_{11} - \beta_{21}} - \frac{\beta_{21} \beta_{13} \ln P_{X3t}}{\beta_{11} - \beta_{21}} - \frac{\beta_{21} \beta_{14} \ln P_{X4t}}{\beta_{11} - \beta_{21}} + \frac{\beta_{11} (\varepsilon_{2t} - \varepsilon_{1t})}{\beta_{11} - \beta_{21}} + \varepsilon_{1t} \quad \text{VI}$$

$$\pi_{10} = \beta_{10} + \frac{\beta_{11} (\beta_{20} - \beta_{10})}{\beta_{11} - \beta_{21}}, \quad \pi_{11} = \frac{\beta_{11} \beta_{22}}{\beta_{11} - \beta_{21}}, \quad \pi_{12} = -\frac{\beta_{11} \beta_{12}}{\beta_{11} - \beta_{21}}, \quad \pi_{13} = -\frac{\beta_{21} \beta_{13}}{\beta_{11} - \beta_{21}}, \quad \pi_{14} = -\frac{\beta_{21} \beta_{14}}{\beta_{11} - \beta_{21}}, \quad w_{1t} = \frac{\beta_{11} (\varepsilon_{2t} - \varepsilon_{1t})}{\beta_{11} - \beta_{21}} + \varepsilon_{1t}$$

From IV

$$\pi_{30} = \frac{\beta_{20} - \beta_{10}}{\beta_{11} - \beta_{21}}, \quad \pi_{31} = \frac{\beta_{22}}{\beta_{11} - \beta_{21}}, \quad \pi_{32} = -\frac{\beta_{12}}{\beta_{11} - \beta_{21}}, \quad \pi_{33} = -\frac{\beta_{13}}{\beta_{11} - \beta_{21}}, \quad \pi_{34} = -\frac{\beta_{14}}{\beta_{11} - \beta_{21}}, \quad w_{3t} = \frac{\varepsilon_{2t} - \varepsilon_{1t}}{\beta_{11} - \beta_{21}}$$

Therefore, reduced forms are

$$\ln s_t = \pi_{10} + \pi_{11} \ln GDP_t + \pi_{12} \ln P_{x2t} + \pi_{13} \ln P_{x3t} + \pi_{14} \ln P_{x4t} + w_t$$

$$\ln d_t = \pi_{20} + \pi_{21} \ln GDP_t + \pi_{22} \ln P_{x2t} + \pi_{23} \ln P_{x3t} + \pi_{24} \ln P_{x4t} + w_{2t}$$

$$\ln p_{0t} = \pi_{30} + \pi_{31} \ln GDP_t + \pi_{32} \ln P_{x2t} + \pi_{33} \ln P_{x3t} + \pi_{34} \ln P_{x4t} + w_{3t}$$

2.

```
. g lnst=ln(st)
```

```
. g lndt=ln(dt)
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```
. g pd=pm+t
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```
. g lnpx2=ln(px2)
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```
. g lnpx3=ln(px3)
```

```
. g lnpx4=ln(px4)
```

```
. g lngdp=ln(gdp)
```

```
. g lngdp=ln(gdp)
```

```
. reg lnst lnpx2 lnpx3 lnpx4 lngdp
```

Source	SS	df	MS	Number of obs	=	22
Model	4.64569724	4	1.16142431	F(4, 17)	=	37.32
Residual	.529104674	17	.031123804	Prob > F	=	0.0000
				R-squared	=	0.8978
				Adj R-squared	=	0.8737
Total	5.17480192	21	.246419139	Root MSE	=	.17642

lnst	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]
lnpx2	-.4503744	.1515961	-2.97	0.009	-.7702142 -.1305347
lnpx3	-.9242052	.2783356	-3.32	0.004	-1.511442 -.3369685
lnpx4	-.3883793	.4222332	-0.92	0.371	-1.279214 .5024549
lngdp	.3438812	.1913463	1.80	0.090	-.0598242 .7475865
_cons	24.65741	5.309757	4.64	0.000	13.4548 35.86002

```
. predict lnsthat , xb
```

```
. reg lndt lnpx2 lnpx3 lnpx4 lngdp
```

Source	SS	df	MS	Number of obs	=	22
Model	3.4026552	4	.850663799	F(4, 17)	=	26.43
Residual	.54721789	17	.032189288	Prob > F	=	0.0000
				R-squared	=	0.8615
				Adj R-squared	=	0.8289
Total	3.94987309	21	.188089195	Root MSE	=	.17941

lndt	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]
lnpx2	-.4887365	.1541691	-3.17	0.006	-.8140049 -.1634682
lnpx3	-.7243134	.2830597	-2.56	0.020	-1.321517 -.1271097
lnpx4	-.577921	.4293997	-1.35	0.196	-1.483875 .3280333
lngdp	.1265855	.194594	0.65	0.524	-.2839719 .5371429
_cons	27.18614	5.399879	5.03	0.000	15.79339 38.57889

```
. predict lndthat , xb
```

```
. reg lnpx2 lnpx3 lnpx4 lngdp
```

Source	SS	df	MS	Number of obs	=	22
Model	.17707359	4	.044268398	F(4, 17)	=	6.76
Residual	.111247189	17	.006543952	Prob > F	=	0.0019
				R-squared	=	0.6142
				Adj R-squared	=	0.5234
Total	.288320779	21	.013729561	Root MSE	=	.08089

lnpx2	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]
lnpx2	.1318015	.0695123	1.90	0.075	-.0148567 .2784596
lnpx3	.0939842	.127627	0.74	0.472	-.1752851 .3632535
lnpx4	.4939641	.1936093	2.55	0.021	.0854842 .9024439
lngdp	.1632779	.0877392	1.86	0.080	-.0218357 .3483914
_cons	2.87652	2.434717	1.18	0.254	-2.260283 8.013322

```
. predict lndthat , xb
```

. reg lnpg lnpx2 lnpx3 lnpx4 lngdp

Source	SS	df	MS	Number of obs	=	22
Model	.17707359	4	.044268398	F(4, 17)	=	6.76
Residual	.111247189	17	.006543952	Prob > F	=	0.0019
				R-squared	=	0.6142
				Adj R-squared	=	0.5234
Total	.288320779	21	.013729561	Root MSE	=	.08089

lnpg	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]	
lnpx2	.1318015	.0695123	1.90	0.075	-.0148567	.2784596
lnpx3	.0939842	.127627	0.74	0.472	-.1752851	.3632535
lnpx4	.4939641	.1936093	2.55	0.021	.0854842	.9024439
lngdp	.1632779	.0877392	1.86	0.080	-.0218357	.3483914
_cons	2.87652	2.434717	1.18	0.254	-2.260283	8.013322

. predict lnpgdhat , xb

3. . reg lnst lnpgdhat lnpx2 lnpx3 lnpx4

Source	SS	df	MS	Number of obs	=	22
Model	4.64569773	4	1.16142443	F(4, 17)	=	37.32
Residual	.529104183	17	.031123775	Prob > F	=	0.0000
				R-squared	=	0.8978
				Adj R-squared	=	0.8737
Total	5.17480192	21	.246419139	Root MSE	=	.17642

lnst	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]	
lnpgdhat	2.106112	1.171903	1.80	0.090	-.3663879	4.578612
lnpx2	-.727963	.1840856	-3.95	0.001	-1.11635	-.3395762
lnpx3	-1.122146	.2824139	-3.97	0.001	-1.717988	-.5263052
lnpx4	-1.428722	.4751381	-3.01	0.008	-2.431176	-.4262679
_cons	18.59912	8.546622	2.18	0.044	.5673274	36.63092

. reg lndt lnpgdhat lngdp

Source	SS	df	MS	Number of obs	=	22
Model	3.26129847	2	1.63064924	F(2, 19)	=	44.99
Residual	.688574614	19	.036240769	Prob > F	=	0.0000
				R-squared	=	0.8257
				Adj R-squared	=	0.8073
Total	3.94987309	21	.188089195	Root MSE	=	.19037

lndt	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]	
lnpgdhat	-2.574157	.5697943	-4.52	0.000	-3.76675	-1.381563
lngdp	.5212927	.1344816	3.88	0.001	.2398194	.802766
_cons	35.93498	7.189835	5.00	0.000	20.88648	50.98347

4. . reg3 (lnst lnpg lnpx2 lnpx3 lnpx4) (lndt lnpg lngdp) , ols inst(lnpx2 lnpx3 lnpx4 lngdp)

Multivariate regression

Equation	Obs	Parms	RMSE	"R-sq"	F-Stat	P
lnst	22	4	.1652258	0.9103	43.14	0.0000
lndt	22	2	.1391259	0.9069	92.53	0.0000

	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]	
lnst						
lnpg	-1.111835	.4515147	-2.46	0.019	-2.027549	-.1961207
lnpx2	-.4189546	.1431634	-2.93	0.006	-.7093034	-.1286059
lnpx3	-.9424196	.2585266	-3.65	0.001	-1.466736	-.4181034
lnpx4	-.521346	.3441643	-1.51	0.139	-1.219344	.1766516
_cons	41.4946	3.661911	11.33	0.000	34.0679	48.9213
lndt						
lnpg	-2.181329	.2946999	-7.40	0.000	-2.779008	-1.58365
lngdp	.5776586	.0887536	6.51	0.000	.397658	.7576593
_cons	31.03578	3.761201	8.25	0.000	23.40771	38.66385

. reg3 (lnst lnpd lnpx2 lnpx3 lnpx4) (lndt lnpd lngdp) , 2sls inst(lnpx2 lnpx3 lnpx4 lngdp)

Two-stage least-squares regression

Equation	Obs	Parms	RMSE	"R-sq"	F-Stat	P
lnst	22	4	.329951	0.6424	10.67	0.0000
lndt	22	2	.1454858	0.8982	77.04	0.0000

	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]	
lnst						
lnpd	2.10611	2.191774	0.96	0.343	-2.339013	6.551233
lnpx2	-.7279628	.3442892	-2.11	0.041	-1.426214	-.0297119
lnpx3	-1.122146	.528189	-2.12	0.041	-2.193363	-.0509293
lnpx4	-1.428722	.8886357	-1.61	0.117	-3.230959	.3735147
_cons	18.59914	15.98447	1.16	0.252	-13.81886	51.01715
lndt						
lnpd	-2.574157	.4354519	-5.91	0.000	-3.457295	-1.69102
lngdp	.5212921	.1027745	5.07	0.000	.3128558	.7297283
_cons	35.93499	5.494663	6.54	0.000	24.7913	47.07868

Endogenous variables: lnst lnpd lndt

Exogenous variables: lnpx2 lnpx3 lnpx4 lngdp

. reg3 (lnst lnpd lnpx2 lnpx3 lnpx4) (lndt lnpd lngdp) , 3sls inst(lnpx2 lnpx3 lnpx4 lngdp)

Three-stage least-squares regression

Equation	Obs	Parms	RMSE	"R-sq"	chi2	P
lnst	22	4	.2963642	0.6266	57.47	0.0000
lndt	22	2	.135203	0.8982	178.41	0.0000

	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
lnst						
lnpd	2.171576	1.926095	1.13	0.260	-1.603501	5.946652
lnpx2	-.7990055	.2985983	-2.68	0.007	-1.384247	-.2137635
lnpx3	-1.329743	.4560002	-2.92	0.004	-2.223487	-.4359989
lnpx4	-1.171403	.775654	-1.51	0.131	-2.691657	.348851
_cons	17.84948	14.04122	1.27	0.204	-9.670808	45.36976
lndt						
lnpd	-2.574157	.4046743	-6.36	0.000	-3.367304	-1.78101
lngdp	.5212921	.0955104	5.46	0.000	.3340951	.708489
_cons	35.93499	5.106302	7.04	0.000	25.92682	45.94316

Endogenous variables: lnst lnpd lndt

Exogenous variables: lnpx2 lnpx3 lnpx4 lngdp

. reg3 (lnst lnpd lnpx2 lnpx3 lnpx4) (lndt lnpd lngdp) , 3sls ireg3 inst(lnpx2 lnpx3 lnpx4 lngdp)

Iteration 1: tolerance = .1059484
Iteration 2: tolerance = .04569793
Iteration 3: tolerance = .01846611
Iteration 4: tolerance = .00725496
Iteration 5: tolerance = .00281814
Iteration 6: tolerance = .00108981
Iteration 7: tolerance = .00042072
Iteration 8: tolerance = .00016231
Iteration 9: tolerance = .0000626
Iteration 10: tolerance = .00002414
Iteration 11: tolerance = 9.310e-06
Iteration 12: tolerance = 3.590e-06
Iteration 13: tolerance = 1.384e-06
Iteration 14: tolerance = 5.339e-07

Three-stage least-squares regression, iterated

Equation	Obs	Parms	RMSE	"R-sq"	chi2	P
lnst	22	4	.3022006	0.6117	54.83	0.0000
lndt	22	2	.135203	0.8982	178.41	0.0000

	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
lnst						
lnpd	2.212666	2.005956	1.10	0.270	-1.718936	6.144268
lnpx2	-.8435967	.3049354	-2.77	0.006	-1.441259	-.2459342
lnpx3	-1.460044	.4623671	-3.16	0.002	-2.366267	-.5538216
lnpx4	-1.009892	.7998393	-1.26	0.207	-2.577548	.557764
_cons	17.37893	14.61488	1.19	0.234	-11.26571	46.02357
lndt						
lnpd	-2.574157	.4046743	-6.36	0.000	-3.367304	-1.78101
lngdp	.5212921	.0955104	5.46	0.000	.3340951	.708489
_cons	35.93499	5.106302	7.04	0.000	25.92682	45.94316

Endogenous variables: lnst lnpd lndt

Exogenous variables: lnpx2 lnpx3 lnpx4 lngdp

According to all approaches applied above, the most appropriated model is 2SLS. The reason is model of 2SLS does have consistency while being able to answer the bias of endogeneity. On the other hand, the model of OLS is still lack behind in terms of consistency and does contain endogeneity bias. Compared to models of 3SLS and I3SLS, 2SLS has the highest performance. What makes 3SLS become disadvantaged is there is risk of inconsistency from specification error despite being more asymptotically efficient. Therefore, the most appropriated model is 2SLS.

5. β_{21} represents elasticity of domestic demand over domestic price
 β_{2e} represents elasticity of domestic demand over GDP or domestic economy