

HW#2 Solution

HW Given $y = 10 + \sqrt{x}$,

- a) Find the derivative $f'(x) = \frac{1}{2\sqrt{x}}$
 b) Fill in the table

Point	X	Y	$f'(x)$
	0	10	∞
A	1	11	0.5
B	2	11.414	0.35
C	3	11.732	0.29

- c) Does the slope increase as x increases? *No, the slope decreases as x increases*
 d) Approximate the change in Y when $\Delta x = 0.2$ at $x_1 = 3$. Is the approximation under- or over-estimate?

$$\Delta y \approx f'(x) \Delta x = (0.29)(0.2) = 0.058$$

Actual change can be found from

$$f(3) = 11.732.$$

$$f(3.2) = 10 + \sqrt{3.2} = 11.788$$

$$\begin{aligned} \therefore \text{actual change } \Delta y &= f(3.2) - f(3) \\ &= 11.788 - 11.732 \\ &= 0.056 < 0.058 \end{aligned}$$

The approximation is overestimated