

H.W.

2 consumers

1 seller  
 $Q = P$

1) draw diagrams

2) find eq<sup>m</sup>

A :  $Q_A = 10 - P \Rightarrow P = 10 - Q$

B :  $Q_B = 10 - \frac{1}{2}P \Rightarrow P = 20 - 2Q$

$P < 10 ; Q^m = Q^A + Q^B$

$Q^m = 20 - 1.5P$

$P > 10 ; Q^m = 10 - \frac{1}{2}P$

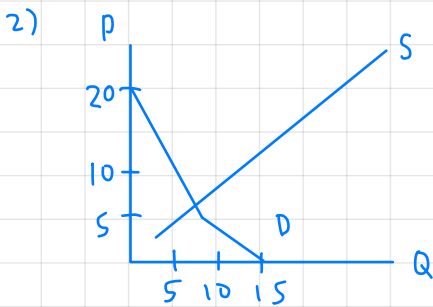
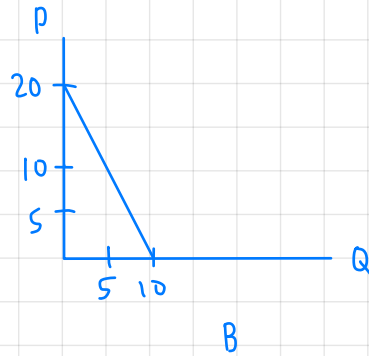
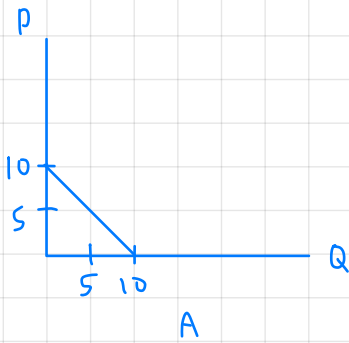
$P < 10$

$Q^D = Q^S$

$20 - 1.5P = P$

$P = 8$

1) Market Equilibrium



∴ There is 1 buyer.

$$Q_{mkt}^D \begin{cases} 10 - \frac{1}{2}P ; P > 10 \\ 20 - \frac{3}{2}P ; P \leq 10 \end{cases}$$

# H.W.

## Example 3.J: Excess burden formula under linear model & Tax-Revenue-maximizing tax rate

Due monday

Demand:  $p^d = a - bQ^d$  ;  $a \geq 0, b \leq 0$ .

Supply:  $p^s = c + dQ^s$  ;  $d \geq 0$ .

- o Solve for quantity and prices equilibrium when the unit tax is imposed. Analyze the result

Before tax

solve for  $P^*, Q^*$   
 $P^* = f(a, b, c, d)$

$Q^* = f(a, b, c, d)$

After tax

Assume tax per unit =  $t$

new  $S$ :  $p = c + dQ + t$

$P^*_{tax} = f(a, b, c, d, t)$

$Q^*_{tax} = f(a, b, c, d, t)$

Before tax

$$a - bQ = c + dQ$$

$$Q = \frac{a - c}{b + d}$$

$$P = c + d \left( \frac{a - c}{b + d} \right)$$

$$P = \frac{cb + cd - ad - cd}{b + d}$$

$$P = \frac{cb - ad}{b + d}$$

After tax

$$a - bQ = c + dQ + t$$

$$Q = \frac{a - c + t}{b + d}$$

$$P = c + d \left( \frac{a - c + t}{b + d} \right)$$

$$P = \frac{ab - ad + dt}{b + d}$$

- Derive the excess burden formula for buyers and sellers

consumers' burden

$$= (P_B - P^*) \times Q_{tax}$$

producers' burden

$$= (P^* - P_S) \times Q_{tax}$$

Tax burden on consumer per unit

$$= \left[ \left( \frac{cb - ad + dt}{b + d} \right) - \left( \frac{cb - ad}{b + d} \right) \right]$$

$$= \frac{dt}{b + d}$$

Tax burden on producer per unit

$$= t - \frac{dt}{b + d}$$

$$= \frac{bt}{b + d}$$

H.W.

- Calculate the tax rate that maximizes the tax revenue of government.

$$\text{tax revenue} = t \times Q_{\text{tax}}^{(\dots t)}$$

$$\frac{\partial \text{tax revenue}}{\partial t} = 0$$

$$\Rightarrow t^*$$

$$\text{Total Tax} = t \left( \frac{a - c + t}{b + d} \right)$$

$$= \frac{at - ct + t^2}{b + d}$$

$$\frac{d \text{total}}{dt} = 0 = \frac{a - c + 2t}{b + d}$$

$$t = \frac{c - a}{2}$$

**Example 3.K Price control and Welfare**

Consider the market for apartment rentals in Chicago. The price of rent is determined by the following system of equations.

$$\text{Demand: } p = -2q_d + 160$$

$$\text{Supply: } p = q_s + 10$$

- What is the equilibrium price and quantity in the market for apartment rentals?

$$-2q + 160 = q + 10$$

$$150 = 3Q$$

$$Q = 50$$

$$p = 60$$

- Suppose the government tries to control the rent prices through a price ceiling of \$40. Discuss the implication of this policy. Is there any deadweight loss?

$$p = 40$$

$$Q^d; 40 = -2Q + 160$$

$$Q = 80$$

$$Q^s; 40 = Q + 10$$

$$Q = 20$$

$$\text{so, excess demand} = 50$$

∴ There is DWL b/c it is not in eq<sup>m</sup>

