

Chapter 12 Consumption: Equilibrium

Consumer's Problem The consumer wants to maximize satisfaction (utility) by deciding what and how much to consume under a limitation of income

Budget Line

- Every point on the budget line is a bundle the consumer can afford.
- Slope of budget line

$$\text{relative price } x \text{ in terms of } y = -\frac{p_x}{p_y}$$

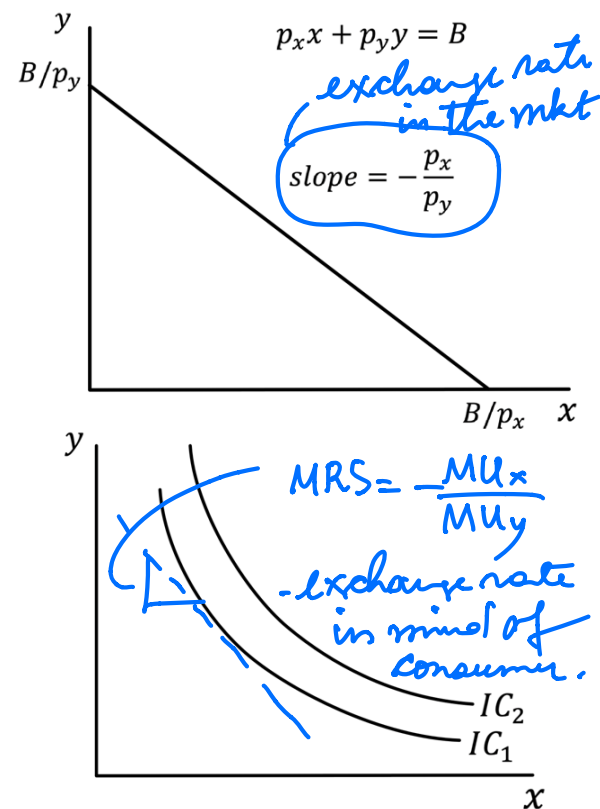
= exchange rate of x in terms of y in the market

Indifference Curve (IC)

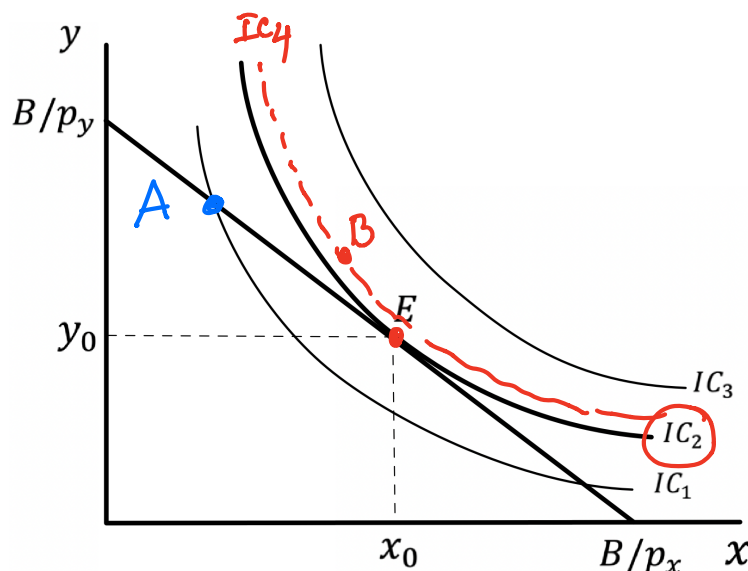
- Each IC shows all the bundles that give the same satisfaction.
- Higher IC means higher satisfaction.
- Slope of IC at (x_0, y_0) is

$$MRS = -\frac{MU_x(x_0, y_0)}{MU_y(x_0, y_0)}$$

= exchange rate of x in terms of y in the mind of consumer



Equilibrium of Consumption Problem The consumer wants to maximize satisfaction (utility) by deciding what and how much to consume under a limitation of income



The equilibrium is at point $E = (x_0, y_0)$ because

- 1) E is on the budget line— E is affordable

A is affordable but gives lower satisfaction than E because A is on a lower IC₁ (lower than IC₂)
E is on the highest IC (IC₂) affordable because if you are at B - get higher satisfaction than at E - because B is on a higher IC.
But B is not affordable because it's above the budget line.

Budget line given

2) E is on the highest IC (IC_2) the consumer can reach.

- ~~B~~ • F is on a higher IC but it is not affordable
~~A~~ • G is affordable because it is on the budget line but it is on a lower IC than IC_2 .

At the equilibrium point E, the indifference curve IC_2 is tangent to the budget line. Thus, at point E the

at E —
$$\frac{\text{Slope of } IC_2}{\text{Slope the budget line}} = \frac{-\frac{MU_x(x_0, y_0)}{MU_y(x_0, y_0)}}{-\frac{p_x}{p_y}} = \frac{p_x}{p_y}$$

Exchange rate between x and y in consumer's mind = Exchange rate between x and y in the market

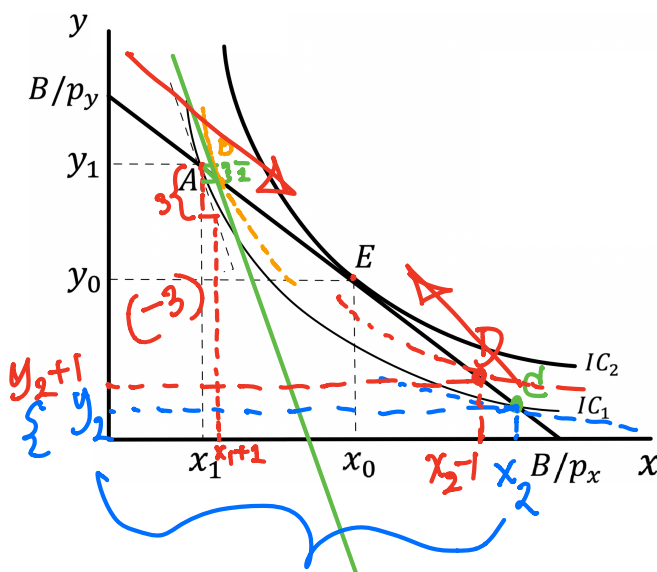
- If $\frac{MU_x(x_0, y_0)}{MU_y(x_0, y_0)} \neq \frac{p_x}{p_y}$, the consumer can attain higher satisfaction by buying more (or less) of x and less (or more) of y.

Equilibrium Conditions: Consumer has equilibrium at $E = (x_0, y_0)$ with the following conditions:

- 1) $p_x x_0 + p_y y_0 = B \Leftrightarrow E$ is affordable. 10 5
2) $\frac{MU_x(x_0, y_0)}{MU_y(x_0, y_0)} = \frac{p_x}{p_y}$, or equivalently $\frac{MU_x(x_0, y_0)}{p_x} = \frac{MU_y(x_0, y_0)}{p_y}$

- $\frac{MU_x(x_0, y_0)}{p_x} = \frac{MU_y(x_0, y_0)}{p_y}$ means that the utility from the last baht spent on x is equal to that spent on y.

Another Explanation for Equilibrium at E: The equilibrium must be at point $E = (x_0, y_0)$ because if it is anywhere else on the budget line like at point A the consumer can attain a higher utility level.

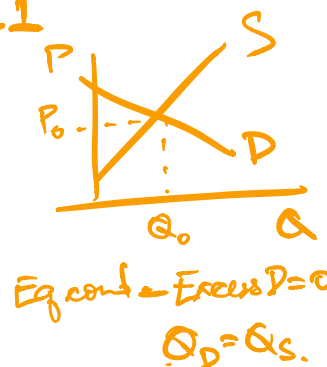


Moving from A to B.
— higher satisfaction
— But is B the best the consumer can do?
— is B the equilibrium?

No. since at B we still have $\frac{MU_x}{MU_y} > \frac{p_x}{p_y}$

$-\frac{MU_x}{MU_y} = 2$ willing to exchng 2 of y for 1 more x

$-\frac{p_x}{p_y} = -\frac{10}{10} = -1$



Eq cond = Excess D = 0.
 $Q_D = Q_S$.

- keep increasing x until
reducing y until
we reach E where
 $\frac{MU_x}{MU_y} = \frac{P_x}{P_y}$

At A, slope of IC_1 is more than the slope of the budget line (in absolute value). That is, we have at $A = (x_1, y_1)$,

$$+\frac{MU_x(x_1, y_1)}{MU_y(x_1, y_1)} > \frac{P_x}{P_y}$$

- For ease of explanation, let us assume that $\frac{MU_x(x_1, y_1)}{MU_y(x_1, y_1)} = 3$ and $\frac{P_x}{P_y} = 1$. The consumer can consume one more unit of x by sacrificing just 1 unit of y. *- in the market.*
- Since $\frac{MU_x(x_1, y_1)}{MU_y(x_1, y_1)} = 3$, in the mind of the consumer, at A he is willing to sacrifice 3 units of y for 1 unit of x to have the same satisfaction.
- By sacrificing only 1 unit of y, instead of 3 units, the consumer thus can be on a higher IC.
- The consumer can repeat this until the point of consumption reaches E, where the exchange rate between x and y in the market is now equal to exchange rate in the mind of the consumer.

$$\text{At C. } \frac{MU_x(x_2, y_2)}{MU_y(x_2, y_2)} < \frac{P_x}{P_y}$$

$$0.2 < 1$$

1 more unit of x will sacrifice 0.2 unit of y

But in the market.

1 X for 1 Y.

∴ not consume more of x.

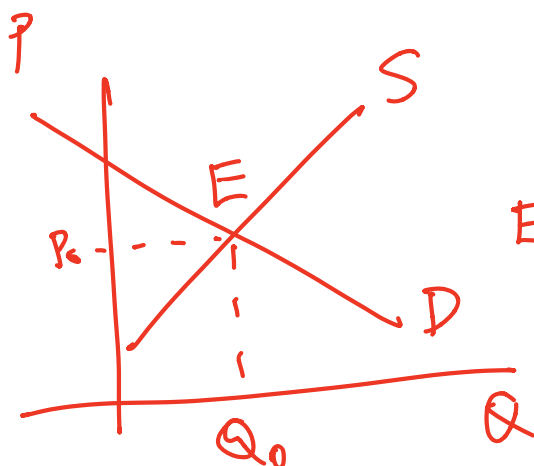
more of y in the market

$$1 \text{ more Y} \Rightarrow 1 \text{ less of X}$$

$$1 \text{ unit of X} \Rightarrow 0.2 \text{ unit of Y}$$

$$5 \text{ units of X} \Leftarrow 1 \text{ unit of Y}$$

At C. consumer is willing to have 1 more of y and sacrifice 5 units of x



Eq Condition at P_0 .

$$Q_D = Q_S$$

Excess D = 0.