

Assignment 3

1.

```
. probit y x1 x2 x3 x4
```

```
Iteration 0: log likelihood = -248.43455
Iteration 1: log likelihood = -150.03919
Iteration 2: log likelihood = -147.48531
Iteration 3: log likelihood = -147.46882
Iteration 4: log likelihood = -147.46881
```

```
Probit regression                               Number of obs   =       400
                                                LR chi2(4)      =     201.93
                                                Prob > chi2     =     0.0000
Log likelihood = -147.46881                    Pseudo R2      =     0.4064
```

y	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
x1	.3590739	.0371539	9.66	0.000	.2862536	.4318941
x2	-.8525746	.144481	-5.90	0.000	-1.135752	-.569397
x3	-.5735764	.2202882	-2.60	0.009	-1.005333	-.1418195
x4	-1.248569	.226762	-5.51	0.000	-1.693014	-.8041238
_cons	1.45664	.2037279	7.15	0.000	1.057341	1.85594

```
. fitstat
```

```
Measures of Fit for probit of y
```

```
Log-Lik Intercept Only:   -248.435   Log-Lik Full Model:     -147.469
D(395):                   294.938   LR(4):                 201.931
                           Prob > LR:         0.000
McFadden's R2:           0.406   McFadden's Adj R2:     0.386
Maximum Likelihood R2:   0.396   Cragg & Uhler's R2:    0.557
McKelvey and Zavoina's R2: 0.640   Efron's R2:           0.446
Variance of y*:         2.775   Variance of error:     1.000
Count R2:                0.818   Adj Count R2:         0.416
AIC:                     0.762   AIC*n:                304.938
BIC:                    -2071.691   BIC':                 -177.966
```

. estat clas

Logistic model for y

Classified	True		Total
	D	~D	
+	251	49	300
-	24	76	100
Total	275	125	400

Classified + if predicted $\Pr(D) \geq .5$

True D defined as $y \neq 0$

Sensitivity	$\Pr(+ D)$	91.27%
Specificity	$\Pr(- \sim D)$	60.80%
Positive predictive value	$\Pr(D +)$	83.67%
Negative predictive value	$\Pr(\sim D -)$	76.00%
False + rate for true ~D	$\Pr(+ \sim D)$	39.20%
False - rate for true D	$\Pr(- D)$	8.73%
False + rate for classified +	$\Pr(\sim D +)$	16.33%
False - rate for classified -	$\Pr(D -)$	24.00%
Correctly classified		81.75%

Probit Model

Overall test: As Chi-square is equal to 201.93 (p-value=0.0000), at least one regressor is not equal to zero. Then, the model can explain dependent variable.

Individual test: Since all explanatory variable has p-value lower than 0.05, all regressors are significant and can explain dependent variable.

Pseudo R squared: for probit model, the pseudo R squared is 0.406.

Counted R squared: In terms of prediction correctness, the model can well explain the variation of the total observation by 81.75%.

```
. logit y x1 x2 x3 x4
```

```
Iteration 0:   log likelihood = -248.43455
Iteration 1:   log likelihood = -154.06753
Iteration 2:   log likelihood = -148.00091
Iteration 3:   log likelihood = -147.90887
Iteration 4:   log likelihood = -147.90869
Iteration 5:   log likelihood = -147.90869
```

```
Logistic regression           Number of obs   =       400
                              LR chi2(4)           =       201.05
                              Prob > chi2           =       0.0000
Log likelihood = -147.90869   Pseudo R2       =       0.4046
```

	y	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
	x1	.6299401	.0708979	8.89	0.000	.4909828	.7688974
	x2	-1.488248	.2597744	-5.73	0.000	-1.997396	-.9790992
	x3	-.9562902	.3882611	-2.46	0.014	-1.717268	-.1953124
	x4	-2.155321	.4055058	-5.32	0.000	-2.950097	-1.360544
	_cons	2.5165	.3714373	6.78	0.000	1.788496	3.244503

```
. fitstat
```

Measures of Fit for **logit** of **y**

```
Log-Lik Intercept Only:      -248.435      Log-Lik Full Model:      -147.909
D(395):                      295.817      LR(4):                   201.052
                              Prob > LR:           0.000
McFadden's R2:               0.405        McFadden's Adj R2:      0.385
Maximum Likelihood R2:       0.395        Cragg & Uhler's R2:     0.555
McKelvey and Zavoina's R2:   0.622        Efron's R2:             0.445
Variance of y*:              8.707        Variance of error:      3.290
Count R2:                    0.818        Adj Count R2:           0.416
AIC:                          0.765        AIC*n:                  305.817
BIC:                          -2070.811     BIC':                   -177.086
```

Logit model

Overall test: As Chi-square is equal to 201.05 (p-value=0.0000), at least one regressor is not equal to zero. Then, the model can explain dependent variable.

Individual test: Since all explanatory variable has p-value lower than 0.05, all regressors are significant and can explain dependent variable.

Pseudo R squared: for probit model, the pseudo R squared is 0.405.

Counted R squared: In terms of prediction correctness, the model can well explain the variation of the total observation by 81.8%.

2. To compare between models, pseudo r-squared is appropriated. Based on the result, Probit model is better than Logit model ($0.406 > 0.405$).

3. Overall LR-test = $2(-147.46881+248.43455) = 201.93$

`. probit y, nolog`

```

Probit regression                               Number of obs   =       400
                                                LR chi2(0)      =       0.00
                                                Prob > chi2     =           .
Log likelihood = -248.43455                    Pseudo R2       =     0.0000

```

y	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]
_cons	.4887764	.0654634	7.47	0.000	.3604706 .6170822

4. Logit model: $\hat{I} = 2.52+0.62(0.45)-1.49(0.81)-0.96(0.56)+2.16(0.12) = 1.32$

`. mfx, predict (xb)`

Marginal effects after logit

```

y = Linear prediction (log odds) (predict, xb)
= 1.32418

```

variable	dy/dx	Std. Err.	z	P> z	[95% C.I.]	X
x1	.6299401	.0709	8.89	0.000	.490983 .768897	.454973
x2	-1.488248	.25977	-5.73	0.000	-1.9974 -.979099	.809344
x3	-.9562902	.38826	-2.46	0.014	-1.71727 -.195312	.556712
x4	-2.155321	.40551	-5.32	0.000	-2.9501 -1.36054	-.119684

5.

. mfx

Marginal effects after logit
 y = Pr(y) (predict)
 = .7898763

variable	dy/dx	Std. Err.	z	P> z	[95% C.I.]	X
x1	.1045522	.01146	9.12	0.000	.082083 .127022	.454973
x2	-.247007	.04388	-5.63	0.000	-.333011 -.161003	.809344
x3	-.1587171	.06397	-2.48	0.013	-.2841 -.033334	.556712
x4	-.3577223	.06679	-5.36	0.000	-.488633 -.226812	-.119684

. mfx, at(median)

Marginal effects after logit
 y = Pr(y) (predict)
 = .84127022

variable	dy/dx	Std. Err.	z	P> z	[95% C.I.]	X
x1	.0841188	.00961	8.76	0.000	.065292 .102946	.655749
x2	-.1987326	.03349	-5.93	0.000	-.264373 -.133093	.692745
x3	-.1276979	.04944	-2.58	0.010	-.224597 -.030799	.488768
x4	-.28781	.05616	-5.12	0.000	-.397881 -.177739	-.109732

6.

. mfx, at(0.5 1 0.5 0)

Marginal effects after probit
 y = Pr(y) (predict)
 = .69034

variable	dy/dx	Std. Err.	z	P> z	[95% C.I.]	X
x1	.1266183	.01307	9.69	0.000	.101001 .152235	.5
x2	-.3006389	.05452	-5.51	0.000	-.4075 -.193778	1
x3	-.2022572	.07644	-2.65	0.008	-.352085 -.05243	.5
x4	-.4402764	.08419	-5.23	0.000	-.605293 -.27526	0

7.

. estat clas

Logistic model for y

Classified	True		Total
	D	~D	
+	251	49	300
-	24	76	100
Total	275	125	400

Classified + if predicted $\text{Pr}(D) \geq .5$

True D defined as $y \neq 0$

Sensitivity	$\text{Pr}(+ D)$	91.27%
Specificity	$\text{Pr}(- \sim D)$	60.80%
Positive predictive value	$\text{Pr}(D +)$	83.67%
Negative predictive value	$\text{Pr}(\sim D -)$	76.00%
False + rate for true ~D	$\text{Pr}(+ \sim D)$	39.20%
False - rate for true D	$\text{Pr}(- D)$	8.73%
False + rate for classified +	$\text{Pr}(\sim D +)$	16.33%
False - rate for classified -	$\text{Pr}(D -)$	24.00%
Correctly classified		81.75%

8.

```
. estat clas, cut(0.7)
```

Logistic model for y

Classified	True		Total
	D	~D	
+	217	24	241
-	58	101	159
Total	275	125	400

Classified + if predicted $\Pr(D) \geq .7$

True D defined as $y \neq 0$

Sensitivity	$\Pr(+ D)$	78.91%
Specificity	$\Pr(- \sim D)$	80.80%
Positive predictive value	$\Pr(D +)$	90.04%
Negative predictive value	$\Pr(\sim D -)$	63.52%
False + rate for true ~D	$\Pr(+ \sim D)$	19.20%
False - rate for true D	$\Pr(- D)$	21.09%
False + rate for classified +	$\Pr(\sim D +)$	9.96%
False - rate for classified -	$\Pr(D -)$	36.48%
Correctly classified		79.50%