



$$TR = P \times Q = 10Q - Q^2$$

$$\text{Slope of } TR = \frac{\Delta TR}{\Delta Q} = MR$$

Thus, revenue max condition is $MR = 0$

Example 2.1: A monopolist firm faces the market demand given by $P = 10 - Q$. Consider the following questions if the cost function $C(Q) = 4Q$.

- What is the revenue-maximizing level of output?

revenue function $TR(Q) = P(Q) \times Q$

$$\text{slope} = \frac{dTR}{dQ} = 10 - 2Q$$

maximum occurs when $\frac{dTR}{dQ} = 0$

$$10 - 2Q = 0$$

$$Q = 5$$

At $Q = 5$, TR is max
 $TR = 25$

$$TR = (10 - Q) \times Q = 10Q - Q^2$$

$$0 = 10 - 2Q$$

$$-10 = -2Q$$

$$5 = Q$$

50 - 25 = 25 ✓

- What is the break-even output?

profit is 0

$$\pi = 0 \rightarrow TR = TC$$

$$0 = TR - TC$$

$$0 = [(10 - Q) \times Q] - [4Q]$$

$$0 = 10Q - Q^2 - 4Q$$

$$0 = 6Q - Q^2$$

$$0 = Q(6 - Q)$$

$$Q = 0, 6$$

at $Q = 0, 6$ is break-even output.

- What is the profit-maximizing level of output?

① $MR = MC$

$$\frac{\Delta TR}{\Delta Q} = \frac{\Delta TC}{\Delta Q}$$

$$4 = 10 - 2Q$$

$$6 = 2Q$$

$$3 = Q$$

② $\pi = TR - TC$

$$\pi = 10Q - Q^2 - 4Q$$

$$\pi = 6Q - Q^2$$

$$\frac{d\pi}{dQ} = 6 - 2Q$$

$$0 = 6 - 2Q$$

$$3 = Q$$

$\frac{d\pi}{dQ} = 0 \rightarrow Q^*$