

HOMEWORK 3 paper, pencil

1. Which of the following can cause the usual OLS  $t$  statistics to be invalid (that is, not to have  $t$  distributions under  $H_0$ )?

- i. Heteroskedasticity.
- ii. A sample correlation coefficient of .95 between two independent variables that are in the model.
- iii. Omitting an important explanatory variable.

2. Consider an equation to explain salaries of CEOs in terms of annual firm sales, return on equity ( $roe$ , in percentage form), and return on the firm's stock ( $ros$ , in percentage form):

$$\log(\text{salary}) = \beta_0 + \beta_1 \log(\text{sales}) + \beta_2 roe + \beta_3 ros + u.$$

- i. In terms of the model parameters, state the null hypothesis that, after controlling for  $sales$  and  $roe$ ,  $ros$  has no effect on CEO salary. State the alternative that better stock market performance increases a CEO's salary.

$$H_0 : \beta_3 = 0$$

$$H_a : \beta_3 \neq 0$$

ii. Using the data in CEOSAL1, the following equation was obtained by OLS:

$$\widehat{\log(\text{salary})} = 4.32 + .280 \log(\text{sales}) + .0174 roe + .00024 ros$$

$$(.32) \quad (.035) \quad (.0041) \quad (.00054)$$

$$n = 209, R^2 = .283.$$

By what **percentage** is  $salary$  predicted to increase if  $ros$  increases by 50 points? Does  $ros$  have a practically large effect on  $salary$ ?

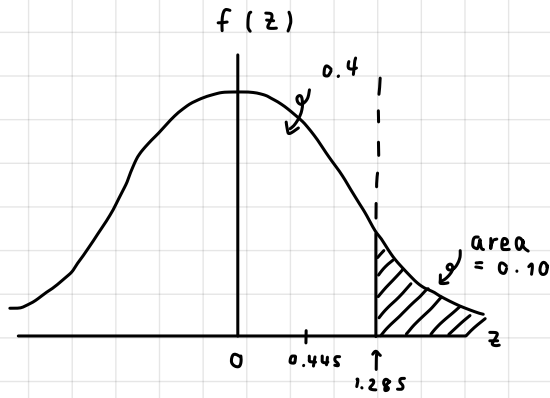
If  $ros$  increases by 50 points, it increases the salary only  $\approx 16\%$ . So, 50 points increase in  $ros$  doesn't have a large effect on salary

iii. Test the null hypothesis that  $ros$  has no effect on  $salary$  against the alternative that  $ros$  has a positive effect. Carry out the test at the 10% significance level.

$$\alpha = 10\% = 0.10$$

$$H_0 : \beta_3 \leq 0$$

$$H_a : \beta_3 > 0$$



$$d.f = n - k - 1 = 209 - 3 - 1 > 30 \quad \text{use } z\text{-score}$$

let's test with 10% significant level

$$z = \frac{\hat{\beta}_3 - \beta_3}{s.e. \hat{\beta}_3} = \frac{0.00024 - 0}{0.00054} = 0.445$$

$$0.445 < 1.285$$

Because 0.445 doesn't fall in the rejection region, we reject  $H_0$ .  
So, *ros* has negative impact.

iv. Would you include *ros* in a final model explaining CEO compensation in terms of firm performance? Explain.

$\beta$  is significant?

## Computer

C8. The data set 401KSUBS contains information on net financial wealth (*nettfa*), age of the survey respondent (*age*), annual family income (*inc*), family size (*fsize*), and participation in certain pension plans for people in the United States. The wealth and income variables are both recorded in thousands of dollars. For this question, use only the data for single-person households (so *fsize* = 1).

i. How many single-person households are there in the data set?

$$n = 2017$$

ii. Use OLS to estimate the model

$$nettfa = \beta_0 + \beta_1 inc + \beta_2 age + u,$$

and report the results using the usual format. Be sure to use only the single-person households in the sample. Interpret the slope coefficients.

Are there any surprises in the slope estimates?

interpret equation  $\beta_1 = 0.7993167$

. regress nettfa inc age if fsize == 1

Source	SS	df	MS	Number of obs	=	2,017
Model	544916.989	2	272458.495	F(2, 2014)	=	136.46
Residual	4021048.06	2,014	1996.54819	Prob > F	=	0.0000
				R-squared	=	0.1193
				Adj R-squared	=	0.1185
Total	4565965.05	2,016	2264.86361	Root MSE	=	44.683

nettfa	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]
inc	.7993167	.0597307	13.38	0.000	.6821762 .9164572
age	.8426563	.0920169	9.16	0.000	.6621982 1.023115
_cons	-43.03981	4.080393	-10.55	0.000	-51.04204 -35.03758

iii. Does the intercept from the regression in part (ii) have an interesting meaning? Explain.  $\beta_0 = -43.03981$

iv. Find the  $p$ -value for the test  $H_0: \beta_2 = 1$  against  $H_1: \beta_2 < 1$ . Do you reject  $H_0$  at the 1% significance level? ทำแบบ moodle

v. If you do a simple regression of nettfa on inc, is the estimated coefficient on inc much different from the estimate in part (ii)? Why or why not?

$$inc = \beta_0 + \beta_1 nettfa + u \quad : \text{compare coefficient}$$

. regress inc nettfa if fsize == 1

Source	SS	df	MS	Number of obs	=	2,017
Model	46335.1731	1	46335.1731	F(1, 2015)	=	181.60
Residual	514127.962	2,015	255.150354	Prob > F	=	0.0000
Total	560463.135	2,016	278.007508	R-squared	=	0.0827
				Adj R-squared	=	0.0822
				Root MSE	=	15.973

	inc	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]
nettfa		.100737	.0074754	13.48	0.000	.0860768 .1153973
_cons		28.07666	.3699027	75.90	0.000	27.35123 28.80209

$\beta_0 = 28.07666$   
 $\beta_1 = 0.100737$

} comparing to the normal equation, the intercept is positive and increases but the slope decreases from the initial ones. However, the number of observation is still the same

C6. ไม่ต้องรู้ Use the data in WAGE2 for this exercise.

i. Consider the standard wage equation

$$\log(wage) = \beta_0 + \beta_1 educ + \beta_2 exper + \beta_3 tenure + u.$$

Print Preview

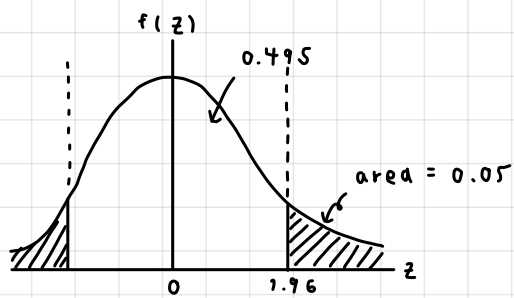
State the null hypothesis that another year of general workforce experience has the same effect on  $\log(wage)$  as another year of tenure with the current employer.

$$H_0: \beta_2 = \beta_3, \quad \beta_2 - \beta_3 = 0$$

$$H_a: \beta_2 \neq \beta_3, \quad \beta_2 - \beta_3 \neq 0$$

ii. Test the null hypothesis in part (i) against a two-sided alternative, at the 5% significance level, by constructing a 95% confidence interval. What do you conclude?

## z-tailed test



$$z = \frac{(\hat{\beta}_2 - \hat{\beta}_3) - 0}{\text{s.e.}(\hat{\beta}_2 - \hat{\beta}_3)}$$

$$\text{let } \theta = \hat{\beta}_2 - \hat{\beta}_3$$
$$\text{then } H_0: \theta = 0$$
$$H_a: \theta \neq 0$$

$$z = \frac{\hat{\theta}_2 - 1}{\text{s.e.}(\hat{\theta}_2)}$$

$$\text{Now, } \hat{\beta}_1 = \hat{\theta}_2 + \hat{\beta}_3$$
$$\beta_1 = \theta_2 + \beta_3$$

substitute in the main regression

$$y = \beta_0 + \beta_1 \text{educ} + (\theta_2 + \beta_3) \text{exper} + \beta_3 \text{tenure} + u$$

C1) The following model can be used to study whether campaign expenditures affect election outcomes:

$$\text{voteA} = \beta_0 + \beta_1 \log(\text{expendA}) + \beta_2 \log(\text{expendB}) + \beta_3 \text{ptystrA} + u,$$

where *voteA* is the percentage of the vote received by Candidate A, *expendA* and *expendB* are campaign expenditures by Candidates A and B, and *ptystrA* is a measure of party strength for Candidate A (the percentage of the most recent presidential vote that went to A's party).

i. What is the interpretation of  $\beta_1$  ?

slope or the measure of expenditure A corresponding with vote A.

ii. In terms of the parameters, state the null hypothesis that a 1% increase in A's expenditures is offset by a 1% increase in B's expenditures.

$$\text{slope} = 1\% = 0.01$$

iii. Estimate the given model using the data in VOTE1 and report the results in usual form. Do A's expenditures affect the outcome? What about B's expenditures? Can you use these results to test the hypothesis in part (ii)? *different variable in equation*

as A and B have different value and sign. Therefore, it generates different outcomes.