

## Assignment 6 Guideline Solution

The following VARs models:

$$Y_t = A_0 + A_1 Y_{t-1} + \epsilon_t$$

where:  $Y_t = \begin{pmatrix} rspot_t \\ rfuture_t \end{pmatrix}$ ,  $A_0 = \begin{pmatrix} a_{10} \\ a_{20} \end{pmatrix}$ ,  $A_1 = \begin{pmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{pmatrix}$ ,  $\epsilon_t = \begin{pmatrix} e_{1t} \\ e_{2t} \end{pmatrix}$

From the data set assign04.dta:

### Requirements:

1. Estimate VARs models using spot return (*rspot*) and future return (*rfuture*) as endogenous variables and determine the most appropriated lags models using SBIC.

```
. varsoc rspot rfuture
```

| Selection-order criteria  |         |         |    |       |          | Number of obs |           | =         | 7679 |
|---------------------------|---------|---------|----|-------|----------|---------------|-----------|-----------|------|
| Sample: 6 - 7684          |         |         |    |       |          |               |           |           |      |
| lag                       | LL      | LR      | df | p     | FPE      | AIC           | HQIC      | SBIC      |      |
| 0                         | 76705.7 |         |    |       | 7.2e-12  | -19.9775      | -19.9769  | -19.9757  |      |
| 1                         | 76876.4 | 341.45  | 4  | 0.000 | 6.9e-12  | -20.0209      | -20.0191  | -20.0155  |      |
| 2                         | 76966.2 | 179.52  | 4  | 0.000 | 6.8e-12  | -20.0433      | -20.0402  | -20.0342  |      |
| 3                         | 76999.2 | 66.06   | 4  | 0.000 | 6.7e-12  | -20.0508      | -20.0465  | -20.0382* |      |
| 4                         | 77015.7 | 32.907* | 4  | 0.000 | 6.7e-12* | -20.0541*     | -20.0485* | -20.0378  |      |
| Endogenous: rspot rfuture |         |         |    |       |          |               |           |           |      |
| Exogenous: _cons          |         |         |    |       |          |               |           |           |      |

- According to SBIC, the most appropriated lag order is 3.

2. Perform stability test and Granger exogeneity test.

```
. var rspot rfuture, lag(1/3)
```

Vector autoregression

|                |            |            |   |           |
|----------------|------------|------------|---|-----------|
| Sample:        | 5 - 7684   | No. of obs | = | 7680      |
| Log likelihood | = 77010.15 | AIC        | = | -20.05108 |
| FPE            | = 6.71e-12 | HQIC       | = | -20.04674 |
| Det(Sigma_ml)  | = 6.69e-12 | SBIC       | = | -20.03842 |

| Equation | Parms | RMSE    | R-sq   | chi2     | P>chi2 |
|----------|-------|---------|--------|----------|--------|
| rspot    | 7     | .001779 | 0.0122 | 95.07421 | 0.0000 |
| rfuture  | 7     | .002044 | 0.0181 | 141.3296 | 0.0000 |

|         | Coef.     | Std. Err. | z     | P> z  | [95% Conf. Interval] |           |
|---------|-----------|-----------|-------|-------|----------------------|-----------|
| rspot   |           |           |       |       |                      |           |
| rspot   |           |           |       |       |                      |           |
| L1.     | -.0323987 | .0159661  | -2.03 | 0.042 | -.0636918            | -.0011057 |
| L2.     | -.1099664 | .0160841  | -6.84 | 0.000 | -.1414905            | -.0784422 |
| L3.     | -.0418984 | .0159205  | -2.63 | 0.008 | -.0731019            | -.0106949 |
| rfuture |           |           |       |       |                      |           |
| L1.     | .0933035  | .0138966  | 6.71  | 0.000 | .0660668             | .1205403  |
| L2.     | .0688434  | .0141336  | 4.87  | 0.000 | .0411421             | .0965447  |

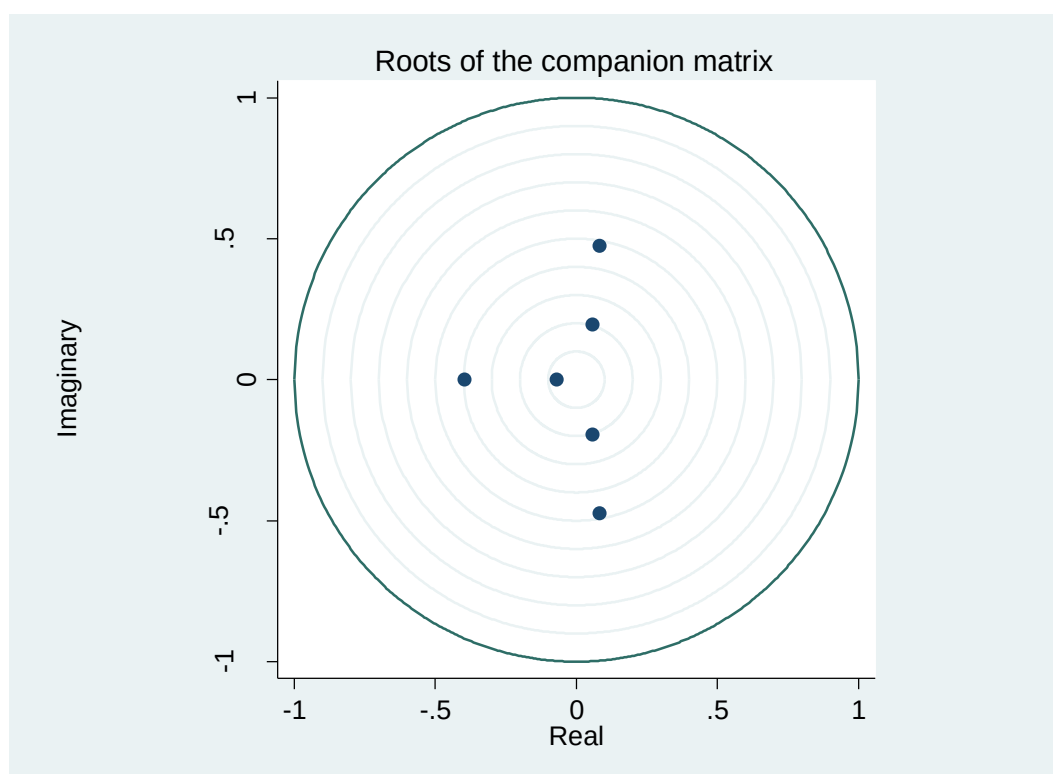
|         |           |          |       |       |           |           |
|---------|-----------|----------|-------|-------|-----------|-----------|
| L3.     | .0317131  | .0139194 | 2.28  | 0.023 | .0044315  | .0589946  |
| _cons   | .0000231  | .0000203 | 1.14  | 0.256 | -.0000167 | .0000629  |
| <hr/>   |           |          |       |       |           |           |
| rfuture |           |          |       |       |           |           |
| rspot   |           |          |       |       |           |           |
| L1.     | .2004382  | .0183405 | 10.93 | 0.000 | .1644915  | .2363849  |
| L2.     | .0600679  | .018476  | 3.25  | 0.001 | .0238557  | .0962801  |
| L3.     | .0609707  | .018288  | 3.33  | 0.001 | .0251268  | .0968146  |
| rfuture |           |          |       |       |           |           |
| L1.     | -.1528221 | .0159632 | -9.57 | 0.000 | -.1841093 | -.1215349 |
| L2.     | -.0926647 | .0162354 | -5.71 | 0.000 | -.1244855 | -.0608439 |
| L3.     | -.0524571 | .0159894 | -3.28 | 0.001 | -.0837958 | -.0211184 |
| _cons   | .0000262  | .0000233 | 1.12  | 0.262 | -.0000195 | .0000719  |

. varstable, graph

Eigenvalue stability condition

| Eigenvalue           |  | Modulus |
|----------------------|--|---------|
| .0829301 + .4737693i |  | .480973 |
| .0829301 - .4737693i |  | .480973 |
| -.3959128            |  | .395913 |
| .0571976 + .1954789i |  | .203675 |
| .0571976 - .1954789i |  | .203675 |
| -.06956342           |  | .069563 |

All the eigenvalues lie inside the unit circle.  
VAR satisfies stability condition.



```
. vargranger
```

Granger causality wald tests

| Equation | Excluded | chi2   | df | Prob > chi2 |
|----------|----------|--------|----|-------------|
| rspot    | rfuture  | 58.069 | 3  | 0.000       |
| rspot    | ALL      | 58.069 | 3  | 0.000       |
| rfuture  | rspot    | 125.3  | 3  | 0.000       |
| rfuture  | ALL      | 125.3  | 3  | 0.000       |

- According to stability test, the system is stable since all the eigenvalues lie inside the unit circle.
- According to Granger exogeneity, both rspot and rfuture are all endogenous variables since all the tests are significant.

3. Perform Impulse response analysis and determine which variable has more impact.

```
. irf create order1, o(rspot rfuture) step(10) set(irf01)
(file irf01.irf created)
(file irf01.irf now active)
(file irf01.irf updated)
```

```
. irf table oirf, impulse(rspot rfuture) response(rspot rfuture)
```

Results from order1

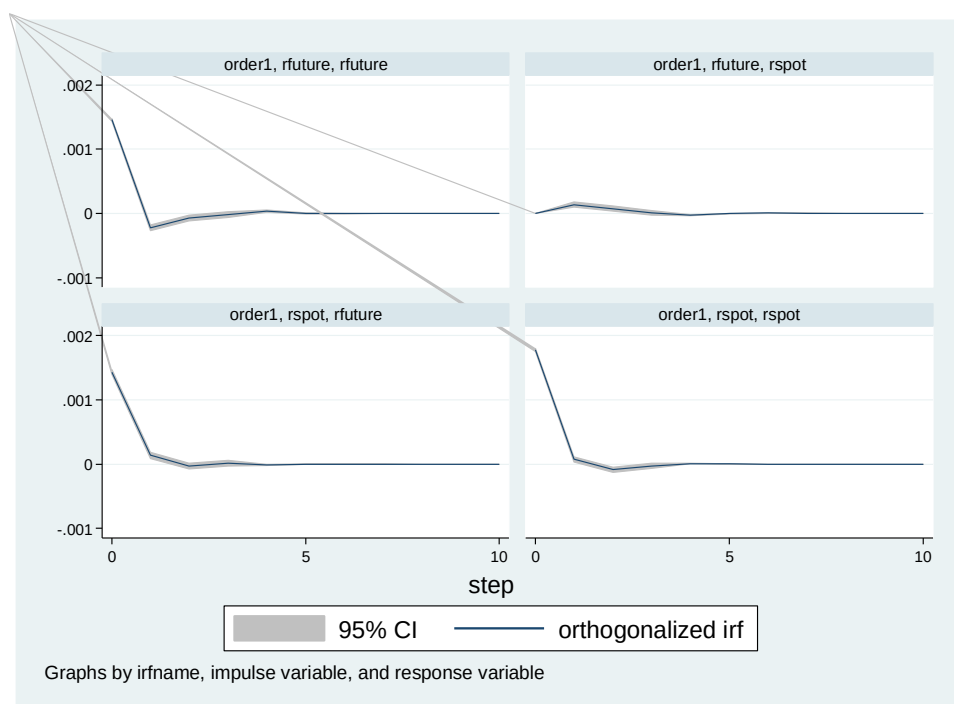
| step | (1)<br>oirf | (1)<br>Lower | (1)<br>Upper | (2)<br>oirf | (2)<br>Lower | (2)<br>Upper | (3)<br>oirf | (3)<br>Lower | (3)<br>Upper |
|------|-------------|--------------|--------------|-------------|--------------|--------------|-------------|--------------|--------------|
| 0    | .001778     | .00175       | .001806      | .001434     | .001395      | .001474      | 0           | 0            | 0            |
| 1    | .000076     | .000036      | .000116      | .000137     | .000091      | .000183      | .000136     | .000096      | .000175      |
| 2    | -.000086    | -.000126     | -.000047     | -.000032    | -.000078     | .000014      | .000075     | .000036      | .000114      |
| 3    | -.000028    | -.000068     | .000012      | .000013     | -.000033     | .000058      | 6.6e-06     | -.000032     | .000045      |
| 4    | .000011     | 3.5e-06      | .000018      | -.000012    | -.00002      | -4.5e-06     | -.000028    | -.00004      | -.000016     |
| 5    | 5.1e-06     | 3.5e-07      | 9.8e-06      | -2.5e-06    | -7.0e-06     | 2.1e-06      | -3.4e-06    | -.00001      | 3.3e-06      |
| 6    | -8.3e-07    | -2.8e-06     | 1.1e-06      | 8.0e-07     | -1.0e-06     | 2.6e-06      | 4.7e-06     | 2.1e-06      | 7.3e-06      |
| 7    | -1.5e-06    | -2.7e-06     | -2.5e-07     | 1.5e-06     | 1.3e-07      | 2.9e-06      | 2.1e-06     | -3.3e-07     | 4.6e-06      |
| 8    | 4.6e-08     | -4.1e-07     | 5.0e-07      | -2.1e-07    | -5.6e-07     | 1.3e-07      | -9.4e-07    | -1.5e-06     | -3.4e-07     |
| 9    | 3.1e-07     | 6.8e-08      | 5.4e-07      | -2.8e-07    | -5.2e-07     | -3.8e-08     | -5.7e-07    | -1.1e-06     | -4.2e-08     |
| 10   | 5.4e-08     | -1.0e-07     | 2.1e-07      | -4.3e-08    | -1.9e-07     | 1.0e-07      | 9.1e-08     | -1.3e-07     | 3.1e-07      |

| step | (4)<br>oirf | (4)<br>Lower | (4)<br>Upper |
|------|-------------|--------------|--------------|
| 0    | .001454     | .001431      | .001477      |
| 1    | -.000222    | -.000268     | -.000177     |
| 2    | -.000074    | -.000119     | -.000028     |
| 3    | -.000021    | -.000066     | .000024      |
| 4    | .000036     | .00002       | .000052      |
| 5    | -3.4e-07    | -6.6e-06     | 5.9e-06      |
| 6    | -4.1e-06    | -6.9e-06     | -1.4e-06     |
| 7    | -2.2e-06    | -4.9e-06     | 5.1e-07      |
| 8    | 1.2e-06     | 5.8e-07      | 1.9e-06      |
| 9    | 4.6e-07     | -5.3e-08     | 9.7e-07      |
| 10   | -1.1e-07    | -3.1e-07     | 8.6e-08      |

95% lower and upper bounds reported

- (1) irfname = order1, impulse = rspot, and response = rspot
- (2) irfname = order1, impulse = rspot, and response = rfuture
- (3) irfname = order1, impulse = rfuture, and response = rspot
- (4) irfname = order1, impulse = rfuture, and response = rfuture

```
. irf graph oirf, impulse(rspot rfuture) response(rspot rfuture)
```



```
. irf table coirf, impulse(rspot rfuture) response(rspot rfuture)
```

Results from order1

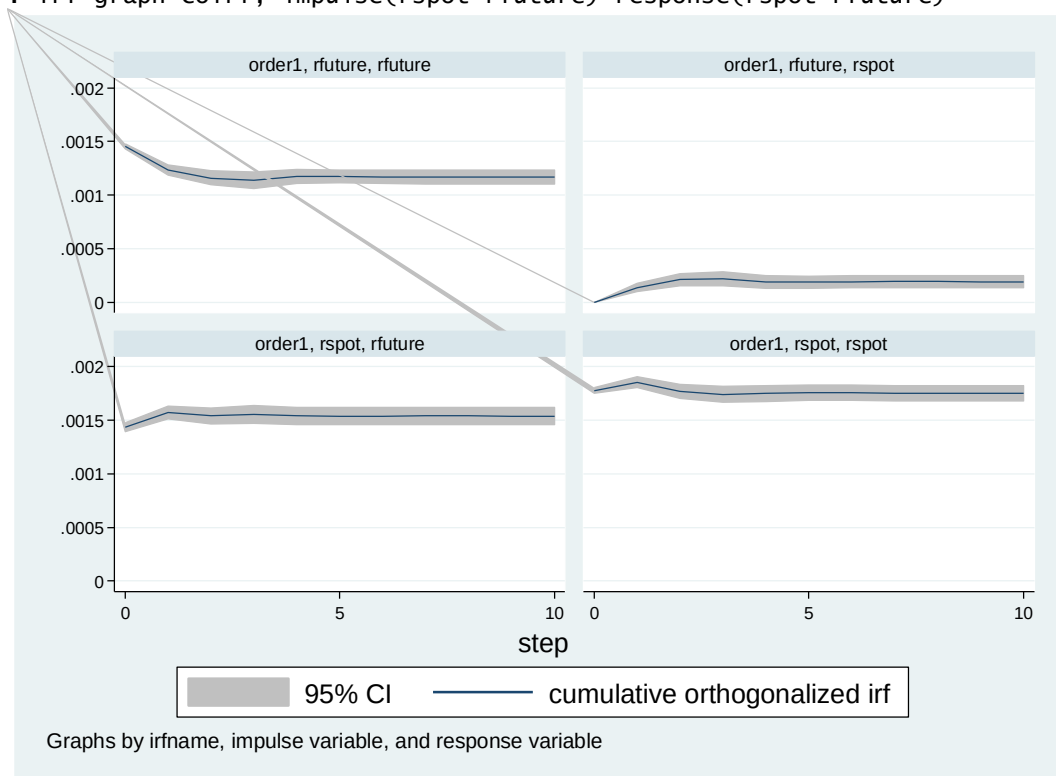
| step | (1)<br>coirf | (1)<br>Lower | (1)<br>Upper | (2)<br>coirf | (2)<br>Lower | (2)<br>Upper | (3)<br>coirf | (3)<br>Lower | (3)<br>Upper |
|------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|
| 0    | .001778      | .00175       | .001806      | .001434      | .001395      | .001474      | 0            | 0            | 0            |
| 1    | .001855      | .001805      | .001904      | .001572      | .001513      | .00163       | .000136      | .000096      | .000175      |
| 2    | .001768      | .001704      | .001832      | .00154       | .001467      | .001613      | .000211      | .000154      | .000268      |
| 3    | .00174       | .001665      | .001815      | .001552      | .001468      | .001637      | .000217      | .00015       | .000285      |
| 4    | .00175       | .001676      | .001825      | .00154       | .001457      | .001623      | .000189      | .000132      | .000247      |
| 5    | .001756      | .001684      | .001827      | .001538      | .001457      | .001618      | .000186      | .000132      | .00024       |
| 6    | .001755      | .001683      | .001826      | .001538      | .001458      | .001619      | .00019       | .000135      | .000245      |
| 7    | .001753      | .001681      | .001825      | .00154       | .001459      | .001621      | .000192      | .000136      | .000249      |
| 8    | .001753      | .001681      | .001825      | .00154       | .001459      | .001621      | .000192      | .000135      | .000248      |
| 9    | .001754      | .001682      | .001826      | .001539      | .001459      | .00162       | .000191      | .000135      | .000247      |
| 10   | .001754      | .001682      | .001826      | .001539      | .001459      | .00162       | .000191      | .000135      | .000247      |

| step | (4)<br>coirf | (4)<br>Lower | (4)<br>Upper |
|------|--------------|--------------|--------------|
| 0    | .001454      | .001431      | .001477      |
| 1    | .001232      | .001183      | .001282      |
| 2    | .001159      | .001093      | .001224      |
| 3    | .001137      | .001061      | .001214      |
| 4    | .001173      | .001109      | .001238      |
| 5    | .001173      | .001111      | .001235      |
| 6    | .001169      | .001105      | .001232      |
| 7    | .001166      | .001102      | .001231      |
| 8    | .001168      | .001104      | .001232      |
| 9    | .001168      | .001104      | .001232      |
| 10   | .001168      | .001104      | .001232      |

95% lower and upper bounds reported

- (1) irfname = order1, impulse = rspot, and response = rspot
- (2) irfname = order1, impulse = rspot, and response = rfuture
- (3) irfname = order1, impulse = rfuture, and response = rspot
- (4) irfname = order1, impulse = rfuture, and response = rfuture

```
. irf graph coirf, impulse(rspot rfuture) response(rspot rfuture)
```



- According to IRF analysis, rspot has more impact on rfuture.

4. Perform Forecast error variance decomposition and determine variable that has more impact on each endogenous variable.

```
. irf table fevd, impulse(rspot rfuture) response(rspot rfuture)
```

| Results from order1 |             |              |              |             |              |              |             |              |              |
|---------------------|-------------|--------------|--------------|-------------|--------------|--------------|-------------|--------------|--------------|
| step                | (1)<br>fevd | (1)<br>Lower | (1)<br>Upper | (2)<br>fevd | (2)<br>Lower | (2)<br>Upper | (3)<br>fevd | (3)<br>Lower | (3)<br>Upper |
| 0                   | 0           | 0            | 0            | 0           | 0            | 0            | 0           | 0            | 0            |
| 1                   | 1           | 1            | 1            | .493053     | .47713       | .508975      | 0           | 0            | 0            |
| 2                   | .994221     | .990856      | .997585      | .48956      | .473586      | .505534      | .005779     | .002415      | .009144      |
| 3                   | .992487     | .988616      | .996357      | .489057     | .473061      | .505053      | .007513     | .003643      | .011384      |
| 4                   | .992475     | .988611      | .996339      | .489024     | .47303       | .505018      | .007525     | .003661      | .011389      |
| 5                   | .992228     | .988242      | .996214      | .488895     | .472897      | .504893      | .007772     | .003786      | .011758      |
| 6                   | .992224     | .988237      | .996212      | .488895     | .472897      | .504893      | .007776     | .003788      | .011763      |
| 7                   | .992218     | .988226      | .996209      | .488894     | .472895      | .504892      | .007782     | .003791      | .011774      |
| 8                   | .992216     | .988224      | .996208      | .488893     | .472895      | .504891      | .007784     | .003792      | .011776      |
| 9                   | .992216     | .988224      | .996208      | .488893     | .472895      | .504891      | .007784     | .003792      | .011776      |
| 10                  | .992216     | .988223      | .996208      | .488893     | .472895      | .504891      | .007784     | .003792      | .011777      |

| step | (4)<br>fevd | (4)<br>Lower | (4)<br>Upper |
|------|-------------|--------------|--------------|
| 0    | 0           | 0            | 0            |
| 1    | .506947     | .491025      | .52287       |
| 2    | .51044      | .494466      | .526414      |
| 3    | .510943     | .494947      | .526939      |
| 4    | .510976     | .494982      | .52697       |
| 5    | .511105     | .495107      | .527103      |
| 6    | .511105     | .495107      | .527103      |
| 7    | .511106     | .495108      | .527105      |
| 8    | .511107     | .495109      | .527105      |
| 9    | .511107     | .495109      | .527105      |
| 10   | .511107     | .495109      | .527105      |

95% lower and upper bounds reported

(1) irfname = order1, impulse = rspot, and response = rspot

(2) irfname = order1, impulse = rspot, and response = rfuture

- (3) irfname = order1, impulse = rfuture, and response = rspot
- (4) irfname = order1, impulse = rfuture, and response = rfuture

- ***According to Forecast error variance decomposition, rspot has more impact on rfuture.***