

$$1.a) \text{ narr } sb_i = \beta_1 + \beta_2 \text{ pcnv}_i + \beta_3 \text{ avgse}_i + \beta_4 \text{ tottime}_i + \beta_5 \text{ptime } sb_i + \beta_6 \text{ qemp } sb_i + u_i$$

$$\text{ narr } sb_i = 0.7061 - 0.1512 \text{ pcnv}_i - 0.0070 \text{ avgse}_i + 0.0121 \text{ tottime}_i - 0.0393 \text{ptime } sb_i - 0.1031 \text{ qemp } sb_i$$

step 1

$$H_0: \beta_3 = 0 \text{ - Null Hypothesis}$$

$$H_A: \beta_3 \neq 0 \text{ - Alternative hypothesis}$$

step 2

$$\alpha = 0.05$$

step 3

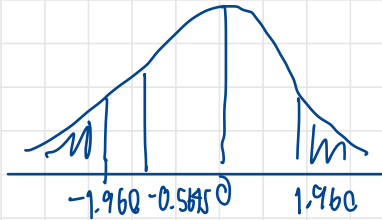
$$\beta_3 t_{\text{cal}} = \frac{\hat{\beta}_3 - \beta_3}{se_{\hat{\beta}_3}}$$

$$t_{\text{cal}} = \frac{-0.0070}{0.0124} = -0.5645$$

step 4

$$t_{\text{lower}} = -1.960$$

$$t_{\text{upper}} = 1.960$$



step 5 At confidence 95 percent, the average sentence served from prior conviction (in months) is not equal to zero,

## (1.b) Model (1.1)

step 1  $H_0: \beta_2 = \beta_3 = \beta_4 = \beta_5 = \beta_6 = 0$

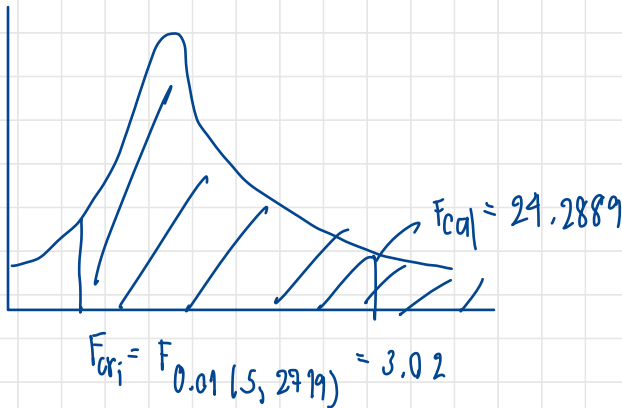
$H_A$ : otherwise

step 2  $F_{cal} = \frac{ESS/df}{RSS/df} = \frac{ESS/(k-1)}{RSS/(n-k)} = \frac{85,9632/(6-1)}{1924,3939/(2725-6)} = 24,2889$

step 3  $\alpha = 0.01$

$F_{upper, \alpha}(5, 2719) = 3.02$

step 4



$\therefore$  We can make sure that  $\beta_2, \beta_3, \beta_4, \beta_5, \beta_6$  are not simultaneously equal to zero, 99 times out of 100.

(1.b) Model (1.2)

step 1  $H_0: \beta_2 = \beta_3 = \beta_4 = \beta_5 = \beta_6 = \beta_7 = \beta_8 = \beta_9 = 0$

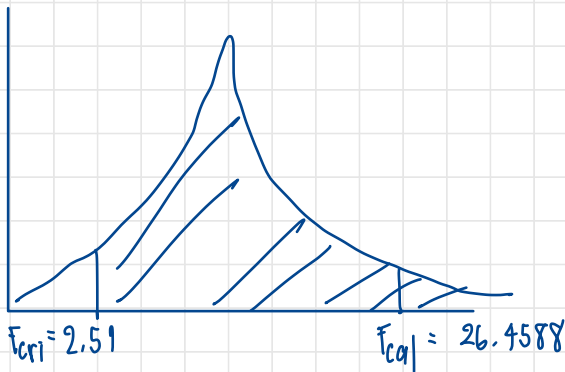
$H_A = \text{otherwise}$

step 2  $F_{\text{cal}} = \frac{R^2/(k-1)}{1-R^2/(n-k)} = \frac{0.0723/(9-1)}{1-0.0723/(2,325-9)} = 26.4588$

step 3  $\alpha = 0.01$

$F_{\text{upper}, \alpha}(8, 2316) = 2.51$

step 4



$\therefore$  We can make sure that  $\beta_2, \beta_3, \beta_4, \beta_5, \beta_6, \beta_7, \beta_8$  and  $\beta_9$  are not simultaneously equal to zero, 99 times out of 100.

1.C)

Step 1

 $H_0$ : ethnic background and legal income has no marginal contribution to the model. $H_a$ : otherwise

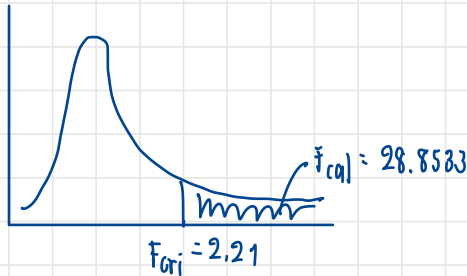
$$\text{step 2} \quad F_{\text{cal}} = \frac{\text{ESS}_{\text{new}} - \text{ESS}_{\text{old}} / (\text{number of new regressors})}{\text{RSS}_{\text{new}} / (n - k_{\text{new}})}$$

$$F_{\text{cal}} = \frac{145,3901 - 85.9532 / 3}{1864,9571 / (2725 - 9)} = 28.8533$$

$$\text{step 3} \quad \alpha = 0.05$$

$$F_{\text{upper}, \alpha} (5, 2716) = 2.21$$

step 4



$\therefore$  We can make sure that ethnic background and legal income has marginal contribution to the model, 95 times out of 100.

2.9

6304647662 - Film

Assume  $\alpha = 0.05$

Step 1  $H_0: \beta_1 = 0$

$H_A: \beta_1 \neq 0$

Step 2

$$t_{\text{cal}}(\beta_1) = \frac{\hat{\beta}_1 - \beta_1}{\text{se}\hat{\beta}_1}$$

$$t_{\text{cal}}(\beta_1) = \frac{9.1748 - 0}{0.0035} = 2621.3714$$

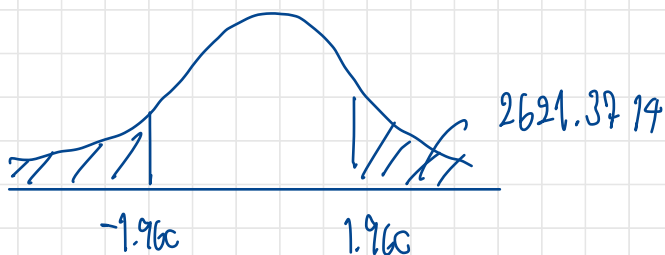
Step 3

$$t_{\text{upper}} = 1.960$$

$$n = 97,873$$

$$n - k = 97,870 \quad \alpha = 0.05$$

$$t_{\text{lower}} = -1.960$$



Step 4

From 95 of 100 times,  $\beta_1$  is reject  $H_0$  or  $\beta_1$  is not equal to 0.

2.9

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Step 1  $H_0: \beta_2 = 0$

$H_A: \beta_2 \neq 0$

Step 2

$$t_{\text{cal}}(\beta_2) = \frac{\hat{\beta}_2 - \beta_2}{\text{se}\beta_2}$$

$$t_{\text{cal}}(\beta_2) = \frac{0.587 - 0}{0.0072} = 81.5278$$

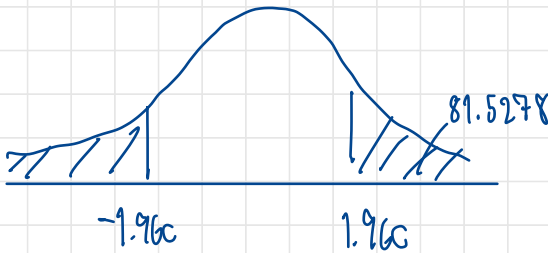
Step 3

$$t_{\text{upper}} = 1.960$$

$$n = 97,873$$

$$n-k = 97,870 \quad \alpha = 0.05$$

$$t_{\text{lower}} = -1.960$$



Step 4

From 95 of 100 times,  $\beta_2$  is reject  $H_0$  or  $\beta_2$  is not equal to 0.

29

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step1  $H_0: \beta_3 = 0$

$H_A: \beta_3 \neq 0$

step2

$$t_{cal}(\beta_3) = \frac{\hat{\beta}_3 - \beta_3}{se\beta_3}$$

$$t_{cal}(\beta_3) = \frac{-0.0336 - 0}{0.005} = -6.72$$

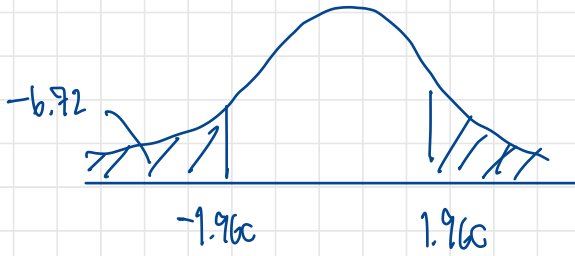
step3

$$t_{upper} = 1.960$$

$$n = 97,873$$

$$n - k = 97,870 \quad \alpha = 0.05$$

$$t_{lower} = -1.960$$



step4

From 95 of 100 times,  $\beta_3$  is reject  $H_0$  or  $\beta_3$  is not equal to 0.

2.9 step 1  $H_0: \beta_4 = 0$

$H_A: \beta_4 \neq 0$

step 2

$$t_{\text{cal}}(\beta_4) = \frac{\hat{\beta}_4 - \beta_4}{\text{se } \hat{\beta}_4}$$

$$t_{\text{cal}}(\beta_4) = \frac{0.0444 - 0}{0.0102} = 4.3529$$

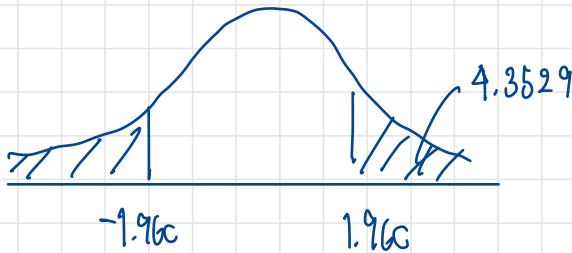
step 3

$$t_{\text{upper}} = 1.960$$

$$n = 97,873$$

$$n - k = 97,870 \quad \alpha = 0.05$$

$$t_{\text{lower}} = -1.960$$



step 4

From 95 of 100 times,  $\beta_4$  is reject  $H_0$  or  $\beta_4$  is not equal to 0.

All in all, at level significant = 0.05,  $\beta_1, \beta_2, \beta_3, \beta_4 \neq 0$

(2.b)

$$\ln \text{wage}_i = 9.1748 + 0.587 \text{ civil}_i - 0.0336 \text{ year}_i + 0.0444 \text{ civil}_i \cdot \text{year}_i + u_i$$

$$\text{wage}_i = e^{9.1748 + 0.587 \text{ civil}_i - 0.0336 \text{ year}_i + 0.0444 \text{ civil}_i \cdot \text{year}_i + u_i}$$

$$\begin{aligned} \text{percentage of civil servant stage and state employee wage without pandemic} &= (e^{\beta_2} - 1) \times 100 \\ &= (e^{0.587} - 1) \times 100 \\ &= 79.8585 \% \end{aligned}$$

It can be said that civil servant stage and state employee gain wage more than others by 79.8585%.

(2.c)

$$\begin{aligned} \text{percentage of wage due to pandemic} &= (e^{\beta_3} - 1) \times 100 \\ &= (e^{-0.0336} - 1) \times 100 \\ &= -3.3042 \% \end{aligned}$$

It can be seen that in 2020 with pandemic year overall wage drop by 3.3042%.

2.d

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$$\widehat{\ln \text{ wage}_i} = \beta_1 + \beta_2 \text{civil}_i + \beta_3 \text{year} + \beta_4 \text{civil}_i \cdot \text{year}_i + u_i$$

$$\widehat{\text{wage}_i} = e^{\beta_1 + \beta_2 \text{civil}_i + \beta_3 \text{year} + \beta_4 \text{civil}_i \cdot \text{year}_i + u_i}$$

$$\widehat{\ln \text{ wage}_i} = 9.1748 + 0.587 \text{civil}_i - 0.0336 \text{year}_i + 0.0444 \text{civil}_i \cdot \text{year}_i + u_i$$

$$\widehat{\text{wage}_i} = e^{9.1748 + 0.587 \text{civil}_i - 0.0336 \text{year}_i + 0.0444 \text{civil}_i \cdot \text{year}_i + u_i}$$

$$E[\widehat{\text{wage}_i} \mid \text{civil}_i = 0, \text{year} = 1, \text{civil} \cdot \text{year} = 0] = e^{9.1748 - 0.0336} = 9,331.9568$$

$$E[\widehat{\text{wage}_i} \mid \text{civil}_i = 0, \text{year} = 0, \text{civil} \cdot \text{year} = 0] = e^{9.1748} = 9,650.8377$$

$$E[\widehat{\text{wage}_i} \mid \text{civil}_i = 1, \text{year} = 1, \text{civil} \cdot \text{year} = 1] = e^{9.1748 + 0.587 - 0.0336 + 0.0444} = 17,546.3284$$

$$E[\widehat{\text{wage}_i} \mid \text{civil}_i = 1, \text{year} = 0, \text{civil} \cdot \text{year} = 0] = e^{9.1748 + 0.587} = 17,367.8477$$

It can be concluded that the civil servant (control group) is better-off during 2020 by 188.480702 or 1.0859% of their wage. While the others are worse-off by 318.8909 or -3.3042 of the wage.

This makes economic sense because civil servants' wage is fixed and did not decrease during pandemic but the others group had an effect from pandemic because of government policy such as lock-down, social distancing, and time limitation to roll.

3.9 In Klein's rule of thumb suggests that multicollinearity is troublesome if the  $R^2$  is greater than  $R^2$  from another model that we regress  $Y$  on these  $X_j$  and other  $X$ .  
 Moreover, VIF should not exceed 10, while TOL should be closer to 1 rather than 0.

$$\alpha = 0.05$$

step 1  $H_0: \beta_1 = 0$

$$H_A: \beta_1 \neq 0$$

step 2

$$t_{\text{calc}}(\beta_1) = \frac{\hat{\beta}_1 - \beta_1}{\text{se}\beta_1} = \frac{-34.1349 - 0}{15.6763} = -2.1775$$

step 3

$$\alpha = 0.05$$

$$\text{df } n - k = 30 - 4 = 26$$

$$t_{\text{upper}} = 2.056$$

$$t_{\text{lower}} = -2.056$$

step 4



From 95 out of 100 times,  $\beta_1$  is reject  $H_0$  or not equal to 0.

3.9) Step 1  $H_0: \beta_2 = 0$

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$H_A: \beta_2 \neq 0$

Step 2

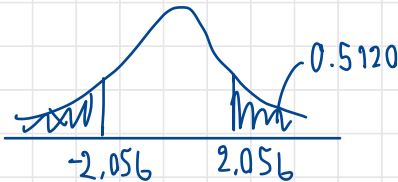
$$t_{\text{cal}}(\beta_2) = \frac{\hat{\beta}_2 - \beta_2}{\text{se}\beta_2} = \frac{1.5386 - 0}{3.005} = 0.5120$$

Step 3

$\alpha = 0.05$   
 $df \ n-k = 30-4 = 26$

$t_{\text{upper}} = 2.056$   
 $t_{\text{lower}} = -2.056$

Step 4



From 95 out of 100 times,  $\beta_2$  is reject  $H_0$  or not equal to 0.

Step 1

$H_0: \beta_3 = 0$

$H_A: \beta_3 \neq 0$

Step 2

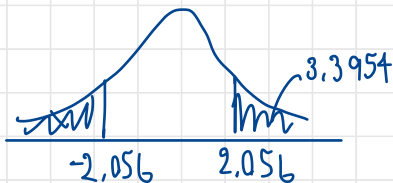
$$t_{\text{cal}}(\beta_3) = \frac{\hat{\beta}_3 - \beta_3}{\text{se}\beta_3} = \frac{3.9152 - 0}{1.1531} = 3.3954$$

Step 3

$\alpha = 0.05$   
 $df \ n-k = 30-4 = 26$

$t_{\text{upper}} = 2.056$   
 $t_{\text{lower}} = -2.056$

Step 4



From 95 out of 100 times,  $\beta_3$  is reject  $H_0$  or not equal to 0.

3.c) Step 1  $H_0: \beta_4 = 0$

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$H_A: \beta_4 \neq 0$

Step 2

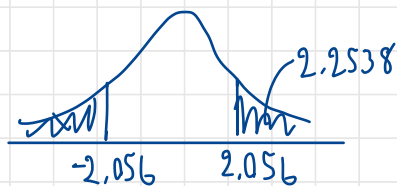
$$t_{\text{cal}}(\beta_4) = \frac{\hat{\beta}_4 - \beta_4}{\text{se}\hat{\beta}_4} = \frac{18.8023 - 0}{8.3426} = 2.2538$$

Step 3

$\alpha = 0.05$   
 $\text{df } n - k = 30 - 4 = 26$

$t_{\text{upper}} = 2.056$   
 $t_{\text{lower}} = -2.056$

Step 4



From 95 out of 100 times,  $\beta_4$  is reject  $H_0$  or not equal to 0.

All in all It is clear that there are no multicollinearity in this model because  $R^2 = 0.6552$  and all of the parameters are different from zero.

3.b) BLUE (Best Linear Unbiased Estimator) is the estimators that show the best variance or the lowest variance as possible. They are unbiased because when there are more samples, probability limit of the estimators tend toward true parameters. BLUE cannot use in multicollinearity. In multicollinearity causes misleading conclusion of hypothesis test.

$$(4.a) \quad \text{Inf}_t = \beta_1 + \beta_2 \text{unem}_t + u_t$$

$$\text{Inf}_t = 1.0108 + 0.5055 \text{unem}_t + u_t$$

$\beta_1$  is the intercept which equal to 1.0108. It implies that when Unemployment rate is 0, the inflation rate is 1.0108 % on average

$\beta_2$  is the slope which is 0.5055. It means when unemployment increase by 1%, the inflation rate will increase by 0.5055% on average.

(4.b) White's test

step 1:  $H_0 = (\text{Homoskedasticity})$   
 $H_a = (\text{Unrestricted heteroskedasticity})$

step 2  $\hat{R}_{123}^2 = 0.0633$

step 3  $LM_{cal} = n \cdot R_{123}^2 = 59 \times 0.0633 = 3.7347$

The critical value  $(\chi_{k-1}^2) = \chi_7^2 \quad \alpha = 0.05 = 8.841426$

step 4 We reject the null hypothesis  $LM_{cal} > \chi_{k-1}^2$ .  
 at significant level = 0.05, heteroscedasticity is present on this model.

(4.c) The OLS estimators still retain than BLUE because from (4.b) this model is heteroscedasticity. Therefore, BLUE property is not violated