

Example 3.G: Solve for the market equilibrium using the information in **Example 3.E** and **Example 3.F**. Justify your answer!

2 consumers

$$A: Q_A = 10 - P$$

$$B: Q_B = 10 - \frac{1}{2}P$$

1 seller

$$Q = P$$

① draw diagrams

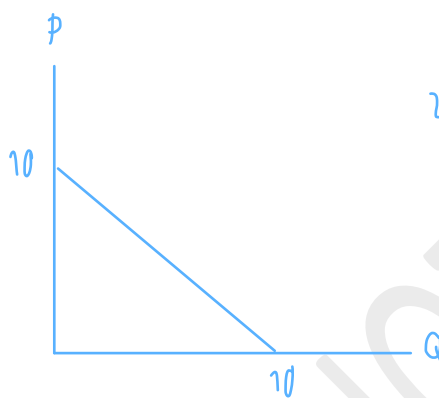
- individual demand

- market demand

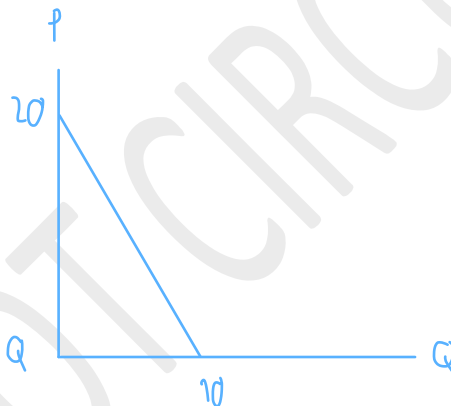
② find equilibrium

- how many buyers buy

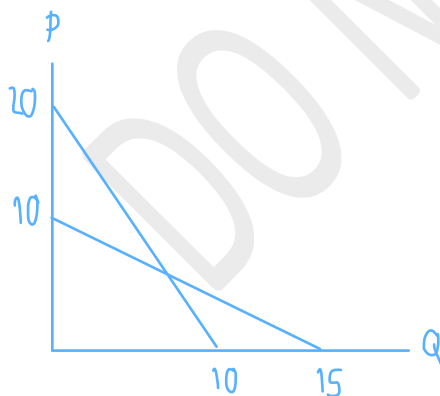
① consumer 1



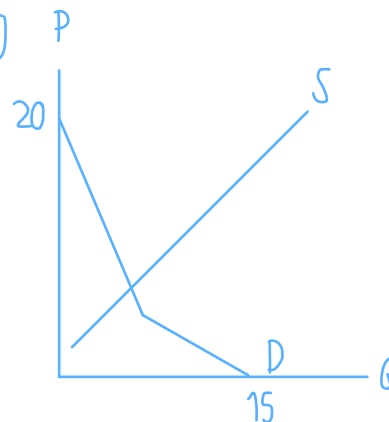
consumer 2



market



②



$$Q_{\text{market}}^D \begin{cases} 10 - \frac{1}{2}P; & P > 10 \\ 20 - \frac{3}{2}P; & P \leq 10 \end{cases}$$

there is only 1 buyer in the market.

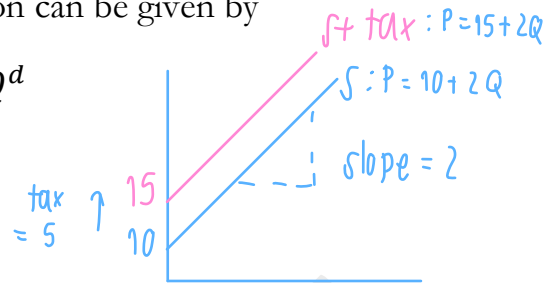
HW



Example 3.I Suppose that demand/supply equation can be given by

$$P^d = 80 - 3Q^d$$

$$P^s = 10 + 2Q^s$$



- Find the market equilibrium.

$$\begin{aligned}
 P^d &= P^s \\
 80 - 3Q &= 10 + 2Q \\
 70 &= 5Q \rightarrow Q^* = 14 \\
 P^* &= 38
 \end{aligned}$$

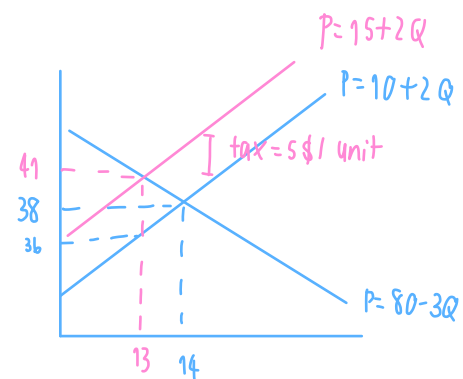
- Suppose that government imposes tax on producer equal to \$5 per unit, determine market equilibrium under taxation.

$$\text{new } S: P = 10 + 2Q + 5$$

$$P = 15 + 2Q$$

$$P^*_{\text{tax}} = 41$$

$$Q^*_{\text{tax}} = 13$$



HW

Example 3.J: Excess burden formula under linear model & Tax-Revenue-maximizing tax rate

Demand: $p^d = a - bQ^d$; $a \geq 0$, $b \leq 0$.

Supply : $p^s = c + dQ^s$; $d \geq 0$.

- Solve for quantity and prices equilibrium when the unit tax is imposed. Analyze the result

$$Q^d = \frac{a-p}{b}$$

$$Q^s = \frac{p-c+t}{d}$$

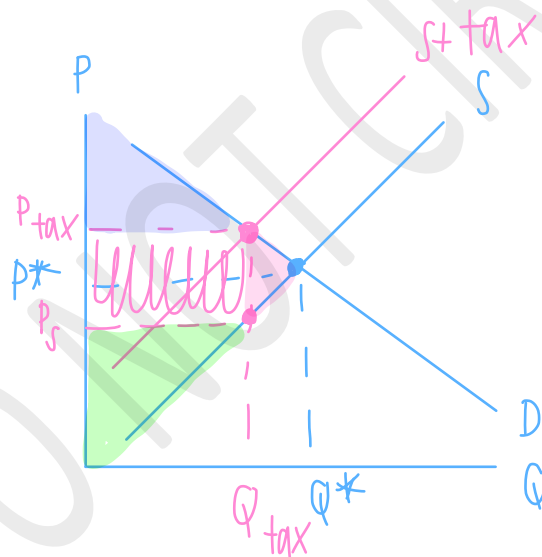
equilibrium : $p^s = p^d$

$$c + dQ^s + t = a - bQ^d$$

$$Q(d+b) = a - c + t$$

$$Q^* = \frac{a - c + t}{d + b}$$

$$p^* = c + t + d \left[\frac{a - c + t}{d + b} \right]$$

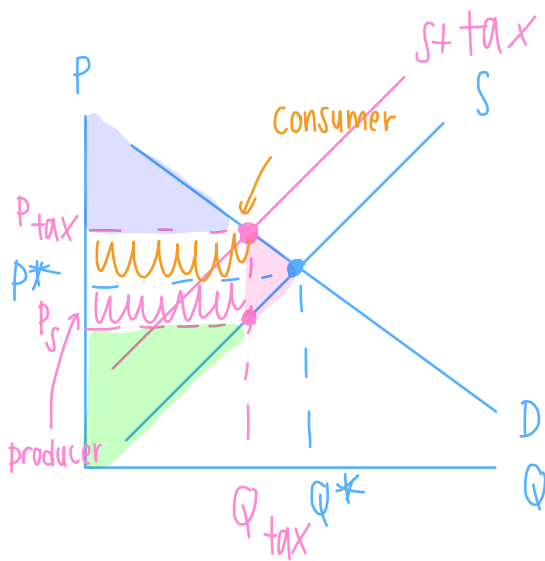


 government revenue

HW



- Derive the excess burden formula for buyers and sellers



extra cost of consumers
 $(P_{tax} - P^*) \times Q_{tax}$

extra cost of producers
 $(P_s - P^*) \times Q_{tax}$

- Calculate the tax rate that maximizes the tax revenue of government.

$$\begin{aligned}\frac{d \text{ tax revenue}}{dt} &= \left[\frac{a-c+t}{d+b} \right] \times t \\ &= at - ct - t^2 + d^{-1}t + b^{-1}t \\ 0 &= a - c - 2t - d^{-1} - b^{-1} \\ 2t &= a - c - d^{-1} - b^{-1} \\ t &= \frac{a - c - d^{-1} - b^{-1}}{2}\end{aligned}$$

Example 3.K Price control and Welfare

Consider the market for apartment rentals in Chicago. The price of rent is determined by the following system of equations.

$$\text{Demand: } p = -2q_d + 160$$

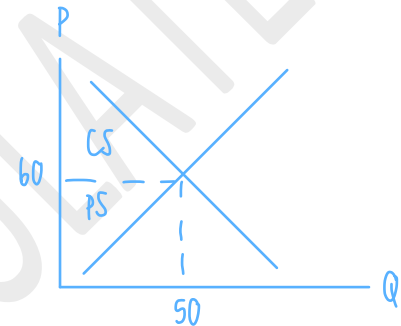
$$\text{Supply: } p = q_s + 10$$

- What is the equilibrium price and quantity in the market for apartment rentals?

equilibrium: $p^s = p^d$
 $q^s + 10 = -2q^d + 160$
 $3Q = 150$
 $Q = 50$

$$P = 50 + 10$$

$$P = 60$$



- Suppose the government tries to control the rent prices through a price ceiling of \$40. Discuss the implication of this policy. Is there any deadweight loss?

The policy is helping consumer by reducing the price of apartment renting.

