

Assignment5_6104640427.R

user

2021-04-29

```
setwd("/Users/user/Desktop/Arm/EE435 R")
cat(rep("\n",50))

#install.packages("fGarch")
library(fGarch)

## Warning: package 'fGarch' was built under R version 4.0.5

## Loading required package: timeDate
## Loading required package: timeSeries
## Loading required package: fBasics
library(quantmod)
## Loading required package: xts
## Loading required package: zoo

##
## Attaching package: 'zoo'

## The following object is masked from 'package:timeSeries':
##
##   time<-

## The following objects are masked from 'package:base':
##
##   as.Date, as.Date.numeric

## Loading required package: TTR

##
## Attaching package: 'TTR'

## The following object is masked from 'package:fBasics':
##
##   volatility

## Registered S3 method overwritten by 'quantmod':
##   method             from
##   as.zoo.data.frame zoo
```

```

library(fBasics)
library(sn)

## Loading required package: stats4

##
## Attaching package: 'sn'

## The following object is masked from 'package:fBasics':
##
##      vech

## The following object is masked from 'package:stats':
##
##      sd

library(PerformanceAnalytics)

##
## Attaching package: 'PerformanceAnalytics'

## The following objects are masked from 'package:timeDate':
##
##      kurtosis, skewness

## The following object is masked from 'package:graphics':
##
##      legend

library(car)

## Loading required package: carData

##
## Attaching package: 'car'

## The following object is masked from 'package:fBasics':
##
##      densityPlot

library(tseries)
library(forecast)

#Question 1
getSymbols("CAT",from="2006-01-03",to="2017-04-13")

## 'getSymbols' currently uses auto.assign=TRUE by default, but will
## use auto.assign=FALSE in 0.5-0. You will still be able to use
## 'loadSymbols' to automatically load data. getOption("getSymbols.env")
## and getOption("getSymbols.auto.assign") will still be checked for
## alternate defaults.
##

```

```
## This message is shown once per session and may be disabled by setting
## options("getSymbols.warning4.0"=FALSE). See ?getSymbols for details.
```

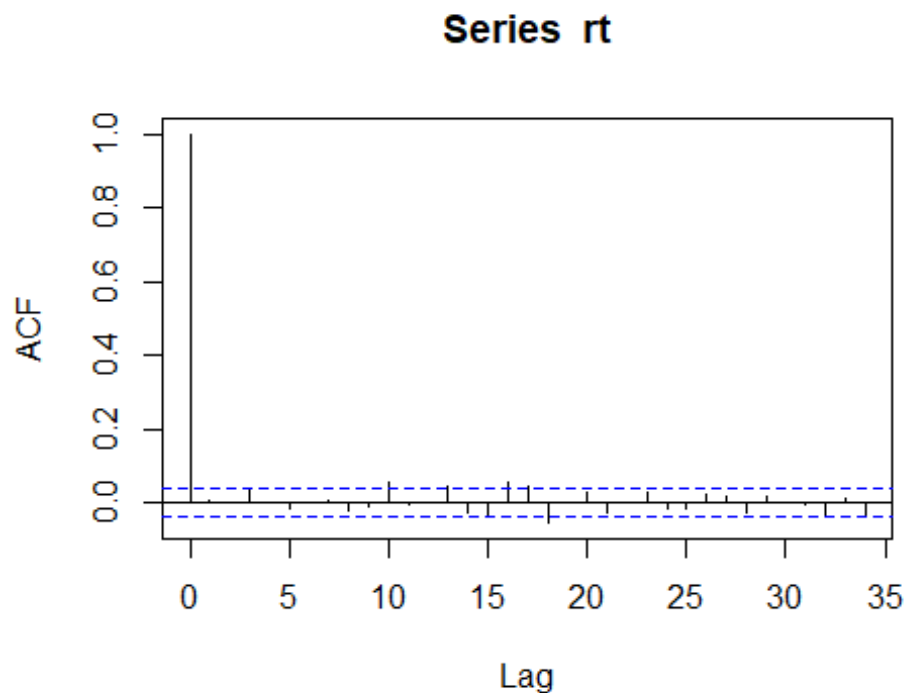
```
## [1] "CAT"
```

```
head(CAT)
```

```
##           CAT.Open CAT.High CAT.Low CAT.Close CAT.Volume CAT.Adjusted
## 2006-01-03    57.87    58.11    57.05    57.80    3697500    38.08682
## 2006-01-04    57.95    59.43    57.55    59.27    4577200    39.05544
## 2006-01-05    59.02    59.86    59.00    59.27    4590700    39.05544
## 2006-01-06    59.47    60.76    59.38    60.45    5692300    39.83300
## 2006-01-09    60.45    61.68    60.45    61.55    4408800    40.55783
## 2006-01-10    61.35    61.52    60.64    61.30    3188100    40.39312
```

```
par=(mfrow=c(2,2))
```

```
rt<-diff(log(as.numeric(CAT[,6])))
```



```
acf(rt)
```

```
# 1a
```

```
Box.test(rt, lag=10, type='Ljung')
```

```
##
```

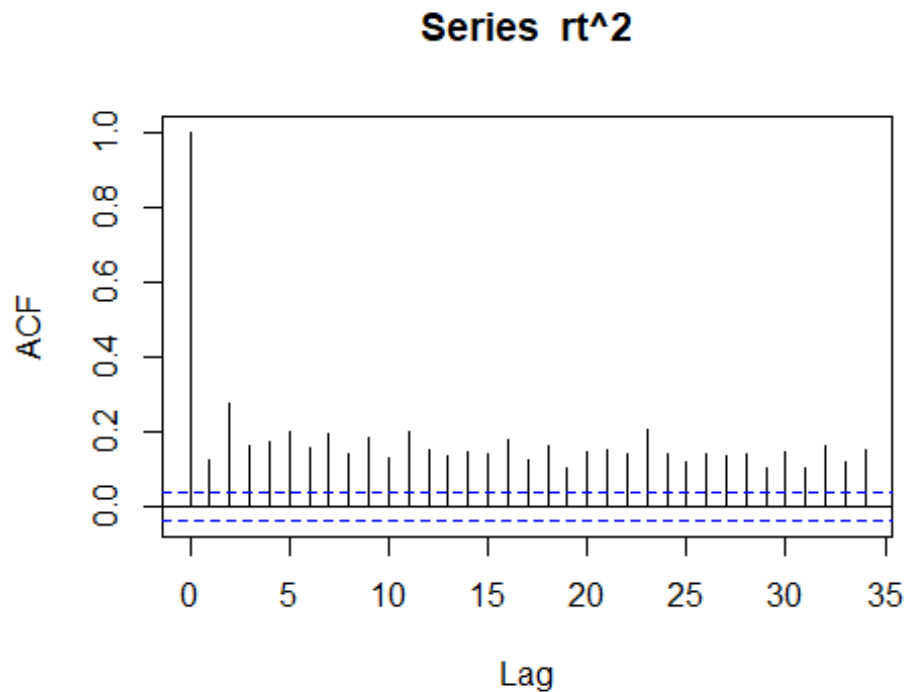
```
## Box-Ljung test
```

```
##
```

```
## data:  rt
## X-squared = 16.291, df = 10, p-value = 0.09159

# as p-value > 0.05 then we can not reject H0, so there is no autocorrelation
between log return

#1b
```



```
acf(rt^2)
```

```
Box.test(rt^2,lag=10,type='Ljung')

##
##  Box-Ljung test
##
## data:  rt^2
## X-squared = 917.21, df = 10, p-value < 2.2e-16

#as p-value < 0.05 then we reject H0, so there is autocorrelation between log
return, hence there is ARCH effects in rt with 95% CI

#1c
m1=garchFit(~arma(1,0)+garch(1,1),data=rt,trace=F)
```

```
## Warning: Using formula(x) is deprecated when x is a character vector of
length > 1.
```

```
## Consider formula(paste(x, collapse = " ")) instead.
```

```
summary(m1)
```

```
##
```

```
## Title:
```

```
## GARCH Modelling
```

```
##
```

```
## Call:
```

```
## garchFit(formula = ~arma(1, 0) + garch(1, 1), data = rt, trace = F)
```

```
##
```

```
## Mean and Variance Equation:
```

```
## data ~ arma(1, 0) + garch(1, 1)
```

```
## <environment: 0x00000000217b2f70>
```

```
## [data = rt]
```

```
##
```

```
## Conditional Distribution:
```

```
## norm
```

```
##
```

```
## Coefficient(s):
```

```
##          mu          ar1          omega          alpha1          beta1
```

```
## 4.8298e-04 1.6866e-02 4.4779e-06 4.9720e-02 9.3866e-01
```

```
##
```

```
## Std. Errors:
```

```
## based on Hessian
```

```
##
```

```
## Error Analysis:
```

```
##      Estimate Std. Error t value Pr(>|t|)
```

```
## mu      4.830e-04 3.075e-04 1.571 0.116297
```

```
## ar1     1.687e-02 2.006e-02 0.841 0.400353
```

```
## omega   4.478e-06 1.278e-06 3.503 0.000461 ***
```

```
## alpha1  4.972e-02 8.191e-03 6.070 1.28e-09 ***
```

```
## beta1   9.387e-01 1.031e-02 91.048 < 2e-16 ***
```

```
## ---
```

```
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
##
```

```
## Log Likelihood:
```

```
## 7378.56 normalized: 2.599916
```

```
##
```

```
## Description:
```

```
## Thu Apr 29 09:57:20 2021 by user: user
```

```
##
```

```
##
```

```
## Standardised Residuals Tests:
```

```
##      Statistic p-Value
```

```
## Jarque-Bera Test R Chi^2 3298.441 0
```

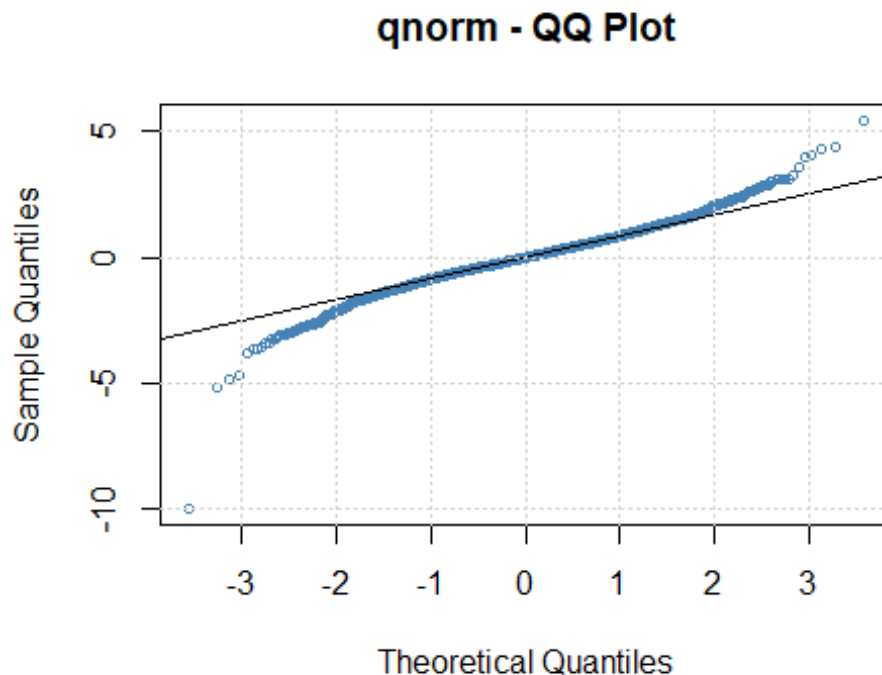
```
## Shapiro-Wilk Test R W 0.9663735 0
```

```
## Ljung-Box Test R Q(10) 12.37554 0.2607088
```

```
## Ljung-Box Test      R      Q(15) 14.79514 0.4662719
## Ljung-Box Test      R      Q(20) 19.20107 0.5087928
## Ljung-Box Test      R^2    Q(10) 0.980939 0.9998424
## Ljung-Box Test      R^2    Q(15) 3.682825 0.9986048
## Ljung-Box Test      R^2    Q(20) 6.9285   0.996913
## LM Arch Test        R      TR^2  2.723165 0.9972029
##
## Information Criterion Statistics:
##          AIC          BIC          SIC          HQIC
## -5.196308 -5.185823 -5.196314 -5.192526
```

#since Ljung-Box test for R we can't reject H_0 then we say that the model is adequate in mean equation
#also can't reject H_0 for R^2 , the volatility model is adequate

```
plot(m1,which=13)
```



#write fitted model

$$\text{mean eq: } \hat{r}_t = \frac{4.930e-04(1-\hat{\phi}_1)}{(3.075e-04)} + \frac{0.0169 r_{t-1}}{(0.020)}$$

$$\text{vol. eq: } \hat{\sigma}_t^2 = \frac{4.478e-06}{(1.278e-06)} + \frac{0.0497 a_{t-1}^2}{(0.0062)} + \frac{0.939 \hat{\sigma}_{t-1}^2}{(0.010)} \quad (\text{satisfy wk})$$

#1d

```
m2=garchFit(~garch(1,1),data=rt,cond.dist="std",trace=F)
```

```
## Warning: Using formula(x) is deprecated when x is a character vector of
length > 1.
```

```
## Consider formula(paste(x, collapse = " ")) instead.
```

```

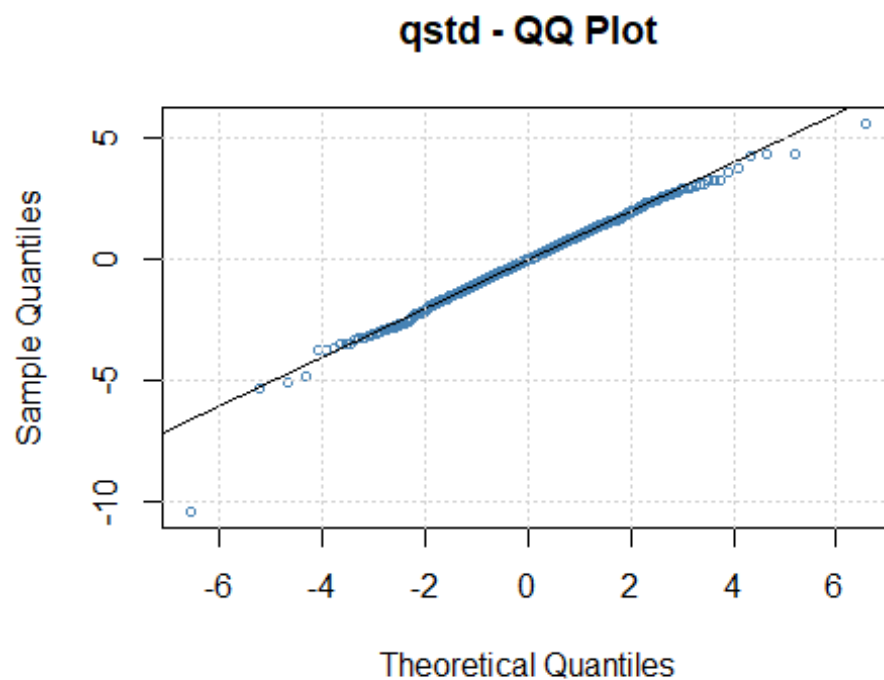
summary(m2)

##
## Title:
## GARCH Modelling
##
## Call:
## garchFit(formula = ~garch(1, 1), data = rt, cond.dist = "std",
## trace = F)
##
## Mean and Variance Equation:
## data ~ garch(1, 1)
## <environment: 0x00000001f106498>
## [data = rt]
##
## Conditional Distribution:
## std
##
## Coefficient(s):
##      mu      omega    alpha1    beta1    shape
## 5.9780e-04 4.2035e-06 7.2376e-02 9.2033e-01 5.0958e+00
##
## Std. Errors:
## based on Hessian
##
## Error Analysis:
##      Estimate Std. Error t value Pr(>|t|)
## mu      5.978e-04 2.702e-04 2.212 0.02695 *
## omega   4.203e-06 1.571e-06 2.675 0.00747 **
## alpha1  7.238e-02 1.374e-02 5.267 1.39e-07 ***
## beta1   9.203e-01 1.472e-02 62.503 < 2e-16 ***
## shape   5.096e+00 4.825e-01 10.561 < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Log Likelihood:
## 7507.106 normalized: 2.64521
##
## Description:
## Thu Apr 29 09:57:21 2021 by user: user
##
##
## Standardised Residuals Tests:
##
##      Statistic p-Value
## Jarque-Bera Test R Chi^2 4056.502 0
## Shapiro-Wilk Test R W 0.9639091 0
## Ljung-Box Test R Q(10) 14.77968 0.140303
## Ljung-Box Test R Q(15) 16.74279 0.3344718
## Ljung-Box Test R Q(20) 20.39783 0.433304
## Ljung-Box Test R^2 Q(10) 2.953085 0.9825066

```

```
## Ljung-Box Test      R^2  Q(15)  5.482428  0.9871938
## Ljung-Box Test      R^2  Q(20)  9.458146  0.9769677
## LM Arch Test        R    TR^2   4.273688  0.977976
##
## Information Criterion Statistics:
##      AIC      BIC      SIC      HQIC
## -5.286897 -5.276412 -5.286903 -5.283115
```

#since Ljung-Box test for R we can't reject H_0 then we say that the model is adequate in mean equation
#also can't reject H_0 for R^2 , the volatility model is adequate



```
plot(m2,which=13)
```

#write fitted model

```
#1e mean eq.  $\hat{r}_t = 5.978 \text{ e-}04$   

      (0.0003)  

      vol. eq.  $\hat{\sigma}_t^2 = 4.203 \text{ e-}06 + 0.072 \alpha_{t-1}^2 + 0.92 \sigma_{t-1}^2$   

      (1.571e-06) (0.014) (0.015)  

#1f  

predict(m2,5)
```

```
## meanForecast meanError standardDeviation
## 1 0.0005977987 0.01515760 0.01515760
## 2 0.0005977987 0.01524072 0.01524072
## 3 0.0005977987 0.01532280 0.01532280
## 4 0.0005977987 0.01540384 0.01540384
## 5 0.0005977987 0.01548387 0.01548387
```

#1g

```
predict(m2,5)
```

```
## meanForecast meanError standardDeviation
## 1 0.0005977987 0.01515760 0.01515760
## 2 0.0005977987 0.01524072 0.01524072
## 3 0.0005977987 0.01532280 0.01532280
## 4 0.0005977987 0.01540384 0.01540384
## 5 0.0005977987 0.01548387 0.01548387
```

$$\hat{f}_t \pm 1.96(\hat{G}_t)$$

$$\Rightarrow (-0.02911, 0.0303)$$

$$\Rightarrow (-0.0293, 0.0305)$$

$$\Rightarrow (-0.0294, 0.03063)$$

$$\Rightarrow (-0.0296, 0.0308)$$

$$\Rightarrow (-0.0298, 0.03095)$$

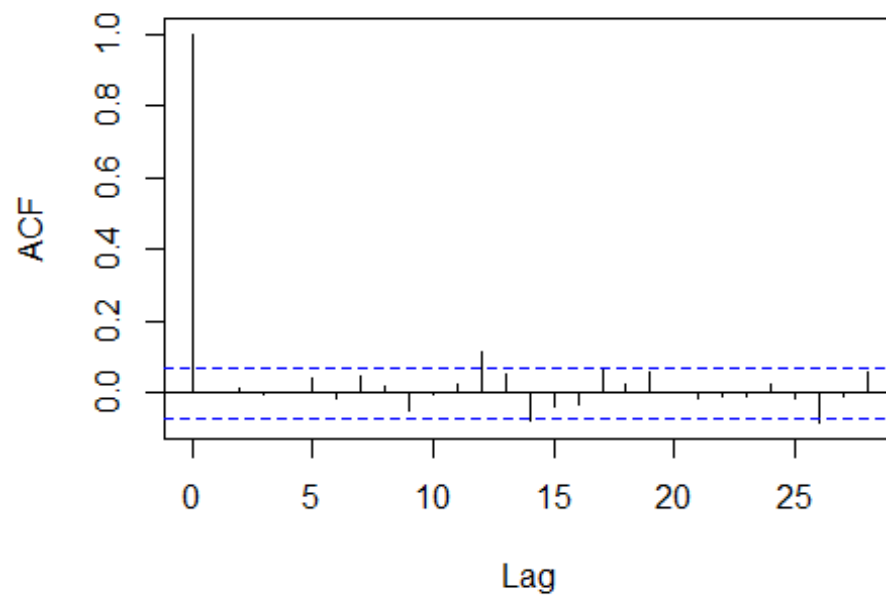
#2

```
k = read.table("m-kovw-5116.txt",header=T)
head(k)
```

```
## PERMNO date ko vwretd
## 1 11308 19520131 0.024390 0.017002
## 2 11308 19520229 0.009524 -0.025141
## 3 11308 19520331 0.016509 0.045870
## 4 11308 19520430 -0.016393 -0.049148
## 5 11308 19520529 0.028571 0.032847
## 6 11308 19520630 0.046296 0.039575
```

```
rk = log(k$ko+1)
acf(rk)
```

Series rk



#2a

```
table.Stats(rk)
```

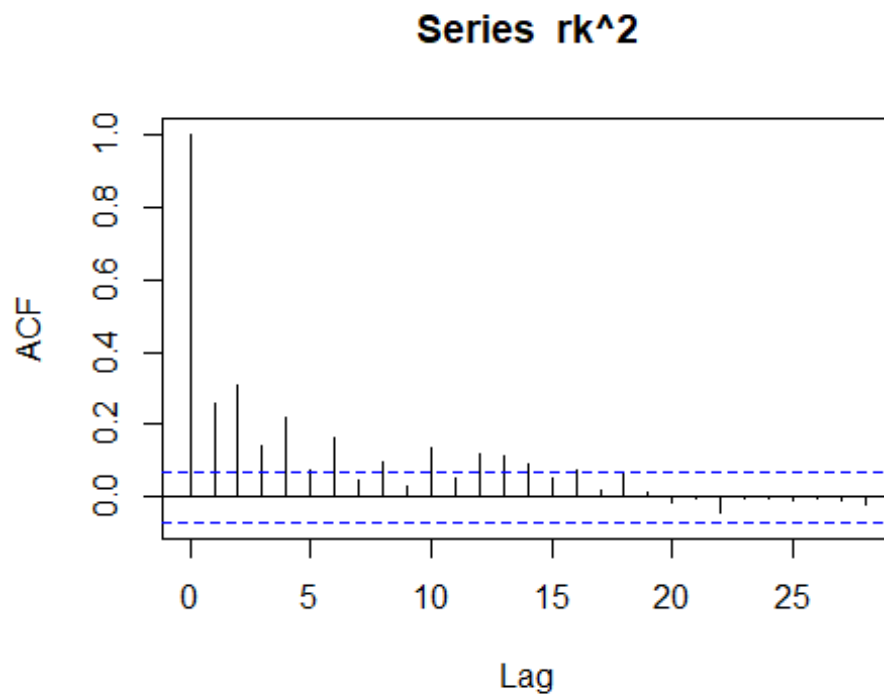
```
##
## Observations      780.0000
## NAs                0.0000
## Minimum           -0.3400
## Quartile 1        -0.0208
## Median             0.0108
## Arithmetic Mean    0.0103
## Geometric Mean     0.0086
## Quartile 3         0.0443
## Maximum            0.2288
## SE Mean            0.0021
## LCL Mean (0.95)    0.0063
## UCL Mean (0.95)    0.0144
## Variance           0.0033
## Stdev              0.0578
## Skewness           -0.4728
## Kurtosis           3.0868
```

```
t.test(rk)
```

```
##
## One Sample t-test
##
## data:  rk
```

```
## t = 4.9853, df = 779, p-value = 7.628e-07
## alternative hypothesis: true mean is not equal to 0
## 95 percent confidence interval:
##  0.00625636 0.01438347
## sample estimates:
## mean of x
## 0.01031992
```

#pv is less than 0.05 we reject H_0 then the expected value of log return is not equal to zero



```
acf(rk^2)
```

```
Box.test(rk, lag=10, type='Ljung')
```

```
##
## Box-Ljung test
##
## data: rk
## X-squared = 5.9201, df = 10, p-value = 0.8219
```

#as p-value > 0.05 then we can not reject H_0 , so there is no autocorrelation between log return

```
Box.test(rt^2, lag=10, type='Ljung')
```

```
##
## Box-Ljung test
##
## data: rt^2
## X-squared = 917.21, df = 10, p-value < 2.2e-16

#as p-value < 0.05 then we reject H0, so there is autocorrelation between log
return-squared, hence there is ARCH effects in rt with 95% CI

#2b
mk1=garchFit(~arma(1,0)+garch(1,1),data=rk,trace=F)

## Warning: Using formula(x) is deprecated when x is a character vector of
length > 1.
## Consider formula(paste(x, collapse = " ")) instead.

summary(mk1)

##
## Title:
## GARCH Modelling
##
## Call:
## garchFit(formula = ~arma(1, 0) + garch(1, 1), data = rk, trace = F)
##
## Mean and Variance Equation:
## data ~ arma(1, 0) + garch(1, 1)
## <environment: 0x00000001ef81360>
## [data = rk]
##
## Conditional Distribution:
## norm
##
## Coefficient(s):
##          mu          ar1          omega          alpha1          beta1
## 0.01124544 -0.02633742  0.00018112  0.09535029  0.84861593
##
## Std. Errors:
## based on Hessian
##
## Error Analysis:
##      Estimate Std. Error t value Pr(>|t|)
## mu      1.125e-02  1.897e-03   5.929 3.05e-09 ***
## ar1     -2.634e-02  3.881e-02  -0.679  0.49740
## omega    1.811e-04  5.852e-05   3.095  0.00197 **
## alpha1   9.535e-02  1.915e-02   4.978 6.42e-07 ***
## beta1    8.486e-01  2.766e-02  30.675 < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Log Likelihood:
```

```
## 1170.664    normalized:  1.500852
##
## Description:
## Thu Apr 29 09:57:21 2021 by user: user
##
## Standardised Residuals Tests:
##
##           Statistic p-Value
## Jarque-Bera Test   R    Chi^2  92.91946  0
## Shapiro-Wilk Test  R     W      0.9857081 6.655604e-07
## Ljung-Box Test     R    Q(10)  9.306169  0.5033144
## Ljung-Box Test     R    Q(15) 22.9901   0.0843502
## Ljung-Box Test     R    Q(20) 27.44814  0.1231201
## Ljung-Box Test     R^2  Q(10) 12.63377  0.2448749
## Ljung-Box Test     R^2  Q(15) 13.62088  0.5544545
## Ljung-Box Test     R^2  Q(20) 15.19817  0.7649584
## LM Arch Test       R     TR^2  10.65102  0.5590389
##
## Information Criterion Statistics:
##           AIC      BIC      SIC      HQIC
## -2.988883 -2.959016 -2.988965 -2.977396
```

#all pv is > 0.05 then the model is adequate in both mean and volatility equation

#fitted model

$$\text{mean eq: } \hat{r}_t = 0.011(1 - \hat{\theta}_1) - 0.016 r_{t-1}$$

(0.002) (0.039)

$$\text{vol eq: } \hat{\sigma}_t^2 = 0.0002 + 0.095 a_{t-1}^2 + 0.849 \hat{\sigma}_{t-1}^2$$

(5.852e-05) (0.019) (0.028)

#2c

```
mk2=garchFit(~arma(1,0)+garch(1,1),data=rk,cond.dist = "std",trace=F)
```

```
## Warning: Using formula(x) is deprecated when x is a character vector of
length > 1.
```

```
## Consider formula(paste(x, collapse = " ")) instead.
```

```
summary(mk2)
```

```
##
## Title:
## GARCH Modelling
##
## Call:
## garchFit(formula = ~arma(1, 0) + garch(1, 1), data = rk, cond.dist =
"std",
## trace = F)
##
## Mean and Variance Equation:
## data ~ arma(1, 0) + garch(1, 1)
## <environment: 0x00000002165eb40>
## [data = rk]
##
## Conditional Distribution:
```

```

## std
##
## Coefficient(s):
##          mu          ar1          omega          alpha1          beta1
shape
## 0.01124020 -0.01887601 0.00017395 0.09642927 0.85044151
7.47877780
##
## Std. Errors:
## based on Hessian
##
## Error Analysis:
##      Estimate Std. Error t value Pr(>|t|)
## mu      1.124e-02 1.810e-03 6.211 5.27e-10 ***
## ar1     -1.888e-02 3.691e-02 -0.511 0.60904
## omega   1.739e-04 6.596e-05 2.637 0.00836 **
## alpha1  9.643e-02 2.338e-02 4.124 3.72e-05 ***
## beta1   8.504e-01 3.267e-02 26.028 < 2e-16 ***
## shape   7.479e+00 1.840e+00 4.066 4.79e-05 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Log Likelihood:
## 1184.863 normalized: 1.519055
##
## Description:
## Thu Apr 29 09:57:22 2021 by user: user
##
##
## Standardised Residuals Tests:
##
##      Statistic p-Value
## Jarque-Bera Test R Chi^2 93.6433 0
## Shapiro-Wilk Test R W 0.9857385 6.832848e-07
## Ljung-Box Test R Q(10) 8.966733 0.5352637
## Ljung-Box Test R Q(15) 22.44818 0.09657967
## Ljung-Box Test R Q(20) 26.86769 0.1390276
## Ljung-Box Test R^2 Q(10) 12.48941 0.2536355
## Ljung-Box Test R^2 Q(15) 13.37442 0.5734021
## Ljung-Box Test R^2 Q(20) 14.90709 0.7816987
## LM Arch Test R TR^2 10.48089 0.5738501
##
## Information Criterion Statistics:
##      AIC      BIC      SIC      HQIC
## -3.022725 -2.986885 -3.022843 -3.008941

```

#all pv is > 0.05 then the model is adequate in both mean and volatility equation

#fitted model

$$\begin{aligned}
 \text{mean eq: } \hat{\mu}_t &= 0.011(1 - \hat{\mu}_t) - 0.019 r_{t-1} \\
 &\quad (0.002) \quad (0.037) \\
 \text{vol eq: } \hat{\sigma}_t^2 &= 0.0002 + 0.964 a_{t-1}^2 + 0.850 \hat{\sigma}_{t-1}^2 \\
 &\quad (6.596e-05) \quad (0.023) \quad (0.033)
 \end{aligned}$$

#2d

```
mk3=garchFit(~garch(1,1),data=rk,trace=F)
```

```
## Warning: Using formula(x) is deprecated when x is a character vector of
length > 1.
```

```
## Consider formula(paste(x, collapse = " ")) instead.
```

```
summary(mk3)
```

```
##
```

```
## Title:
```

```
## GARCH Modelling
```

```
##
```

```
## Call:
```

```
## garchFit(formula = ~garch(1, 1), data = rk, trace = F)
```

```
##
```

```
## Mean and Variance Equation:
```

```
## data ~ garch(1, 1)
```

```
## <environment: 0x000000001eae0710>
```

```
## [data = rk]
```

```
##
```

```
## Conditional Distribution:
```

```
## norm
```

```
##
```

```
## Coefficient(s):
```

```
##          mu          omega        alpha1        beta1
```

```
## 0.01098417 0.00018497 0.09479925 0.84780406
```

```
##
```

```
## Std. Errors:
```

```
## based on Hessian
```

```
##
```

```
## Error Analysis:
```

```
##      Estimate Std. Error t value Pr(>|t|)
```

```
## mu      1.098e-02  1.846e-03   5.950 2.68e-09 ***
```

```
## omega   1.850e-04  5.899e-05   3.135 0.00172 **
```

```
## alpha1  9.480e-02  1.912e-02   4.958 7.11e-07 ***
```

```
## beta1   8.478e-01  2.787e-02  30.416 < 2e-16 ***
```

```
## ---
```

```
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
##
```

```
## Log Likelihood:
```

```
## 1170.393 normalized: 1.500504
```

```
##
```

```
## Description:
```

```
## Thu Apr 29 09:57:22 2021 by user: user
```

```
##
```

```
##
```

```
## Standardised Residuals Tests:
```

```
##          Statistic p-Value
```

```
## Jarque-Bera Test R Chi^2 95.07163 0
```

```
## Shapiro-Wilk Test R W 0.9856773 6.481596e-07
## Ljung-Box Test R Q(10) 8.125181 0.6166108
## Ljung-Box Test R Q(15) 21.27199 0.128362
## Ljung-Box Test R Q(20) 25.62765 0.1784646
## Ljung-Box Test R^2 Q(10) 12.90586 0.228983
## Ljung-Box Test R^2 Q(15) 13.87463 0.5350581
## Ljung-Box Test R^2 Q(20) 15.35522 0.755734
## LM Arch Test R TR^2 10.96004 0.532346
##
## Information Criterion Statistics:
## AIC BIC SIC HQIC
## -2.990752 -2.966858 -2.990804 -2.981562
```

#all pv is > 0.05 then the model is adequate in both mean and volatility equation

$$\text{mean eq } \hat{r}_t : 0.011 \\ (0.002)$$

#fitted model

$$\text{vol. eq: } \hat{\sigma}_t^2 = 0.0002 + 0.045 \alpha_{t-1}^2 + 0.848 \sigma_{t-1}^2 \\ (5.899e-05) (0.019) (0.0279)$$

#2e

```
mk4=garchFit(~garch(1,1),data=rk,cond.dist = "std",trace=F)
```

```
## Warning: Using formula(x) is deprecated when x is a character vector of
length > 1.
```

```
## Consider formula(paste(x, collapse = " ")) instead.
```

```
summary(mk4)
```

```
##
## Title:
## GARCH Modelling
##
## Call:
## garchFit(formula = ~garch(1, 1), data = rk, cond.dist = "std",
## trace = F)
##
## Mean and Variance Equation:
## data ~ garch(1, 1)
## <environment: 0x000000002053d5c8>
## [data = rk]
##
## Conditional Distribution:
## std
##
## Coefficient(s):
## mu omega alpha1 beta1 shape
## 0.01105016 0.00017528 0.09632874 0.85006800 7.48604505
##
## Std. Errors:
## based on Hessian
##
## Error Analysis:
```

```

##          Estimate Std. Error t value Pr(>|t|)
## mu      1.105e-02  1.757e-03   6.291 3.16e-10 ***
## omega   1.753e-04  6.627e-05   2.645 0.00817 **
## alpha1  9.633e-02  2.337e-02   4.123 3.75e-05 ***
## beta1   8.501e-01  3.277e-02  25.941 < 2e-16 ***
## shape   7.486e+00  1.840e+00   4.069 4.72e-05 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Log Likelihood:
## 1184.68 normalized: 1.518821
##
## Description:
## Thu Apr 29 09:57:22 2021 by user: user
##
##
## Standardised Residuals Tests:
##
##          Statistic p-Value
## Jarque-Bera Test  R    Chi^2 95.31715 0
## Shapiro-Wilk Test  R    W    0.9857263 6.761141e-07
## Ljung-Box Test     R    Q(10) 8.228765 0.6065024
## Ljung-Box Test     R    Q(15) 21.34759 0.1260864
## Ljung-Box Test     R    Q(20) 25.67699 0.1767469
## Ljung-Box Test     R^2 Q(10) 12.61146 0.2462139
## Ljung-Box Test     R^2 Q(15) 13.4693 0.5660982
## Ljung-Box Test     R^2 Q(20) 14.93694 0.7800047
## LM Arch Test       R    TR^2 10.62989 0.560875
##
## Information Criterion Statistics:
##          AIC      BIC      SIC      HQIC
## -3.024822 -2.994954 -3.024903 -3.013334

```

#all pv is > 0.05 then the model is adequate in both mean and volatility equation

#2f
#using AIC and BIC then the lower is the more effective model hence, in (e) there is lower AIC and BIC which is better

#3

```
getSymbols("^GSPC",from="2005-01-02",to="2021-03-31")
```

```
## [1] "^GSPC"
```

```
rs<-diff(log(as.numeric(GSPC[,6])))
table.Stats(rs)
```

```
##
## Observations      4087.0000
## NAs                0.0000
## Minimum            -0.1277

```

```
## Quartile 1      -0.0039
## Median          0.0007
## Arithmetic Mean  0.0003
## Geometric Mean   0.0002
## Quartile 3      0.0056
## Maximum         0.1096
## SE Mean         0.0002
## LCL Mean (0.95) -0.0001
## UCL Mean (0.95)  0.0007
## Variance        0.0002
## Stdev           0.0125
## Skewness        -0.5633
## Kurtosis        14.0029
```

```
t.test(rs)
```

```
##
## One Sample t-test
##
## data: rs
## t = 1.4961, df = 4086, p-value = 0.1347
## alternative hypothesis: true mean is not equal to 0
## 95 percent confidence interval:
## -9.051939e-05  6.737464e-04
## sample estimates:
## mean of x
## 0.0002916135
```

#pv is > 0.05 then can't reject H_0 , the expected value of rt is zero

```
acf(rs)
```

```
Box.test(rs, lag=10, type='Ljung')
```

```
##
## Box-Ljung test
##
## data: rs
## X-squared = 131.85, df = 10, p-value < 2.2e-16
```

#we cant rej. H_0 then there is no serial correlation in rt

```
ms1=garchFit(arima()~garch(1,1), data=rs, trace=F)
```

```
## Warning: Using formula(x) is deprecated when x is a character vector of
length > 1.
## Consider formula(paste(x, collapse = " ")) instead.
```

```
summary(ms1)
```

```
##
## Title:
```

```

## GARCH Modelling
##
## Call:
## garchFit(formula = arima() ~ garch(1, 1), data = rs, trace = F)
##
## Mean and Variance Equation:
## data ~ garch(1, 1)
## <environment: 0x000000001ecd9580>
## [data = rs]
##
## Conditional Distribution:
## norm
##
## Coefficient(s):
##          mu          omega      alpha1      beta1
## 6.7965e-04 2.7630e-06 1.4185e-01 8.3682e-01
##
## Std. Errors:
## based on Hessian
##
## Error Analysis:
##      Estimate Std. Error t value Pr(>|t|)
## mu      6.797e-04 1.164e-04 5.837 5.33e-09 ***
## omega  2.763e-06 3.545e-07 7.794 6.44e-15 ***
## alpha1 1.418e-01 1.200e-02 11.822 < 2e-16 ***
## beta1  8.368e-01 1.198e-02 69.853 < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Log Likelihood:
## 13417.79 normalized: 3.283041
##
## Description:
## Thu Apr 29 09:57:22 2021 by user: user
##
##
## Standardised Residuals Tests:
##
##      Jarque-Bera Test  R      Chi^2 1128.761 0
##      Shapiro-Wilk Test  R      W      0.9727248 0
##      Ljung-Box Test     R      Q(10) 25.75991 0.004076864
##      Ljung-Box Test     R      Q(15) 33.37343 0.004166121
##      Ljung-Box Test     R      Q(20) 38.81779 0.007023858
##      Ljung-Box Test     R^2 Q(10) 15.24652 0.1233293
##      Ljung-Box Test     R^2 Q(15) 17.48525 0.2906928
##      Ljung-Box Test     R^2 Q(20) 18.66957 0.5433881
##      LM Arch Test       R      TR^2 15.93476 0.1942425
##
## Information Criterion Statistics:

```

```
##          AIC          BIC          SIC          HQIC
## -6.564125 -6.557944 -6.564127 -6.561936
```

```
plot(ms1,which=13)
```

#from Box test the only adequate for model is volatility equation, the mean equation is not adequate since the pv of residual are all <0.05 then reject H0

#fitted model

$$\text{mean eq.} \Rightarrow \hat{\epsilon}_t = 6.797 \times 10^{-4} \quad (1.164 \times 10^{-4})$$

$$\text{vol. eq.} \Rightarrow \hat{\sigma}_t^2 = 2.763 \times 10^{-6} + 0.142 a_{t-1}^2 + 0.837 \sigma_{t-1}^2$$

(3.545E-07) (0.012) (0.012)

#3c

```
ms2=garchFit(arima()~garch(1,1),data=rs,cond.dist = "std",trace=F)
```

```
## Warning: Using formula(x) is deprecated when x is a character vector of
length > 1.
```

```
## Consider formula(paste(x, collapse = " ")) instead.
```

```
summary(ms2)
```

```
##
## Title:
## GARCH Modelling
##
## Call:
## garchFit(formula = arima() ~ garch(1, 1), data = rs, cond.dist = "std",
## trace = F)
##
## Mean and Variance Equation:
## data ~ garch(1, 1)
## <environment: 0x000000001e6e8338>
## [data = rs]
##
## Conditional Distribution:
## std
##
## Coefficient(s):
##          mu          omega          alpha1          beta1          shape
## 8.4344e-04  1.7504e-06  1.4341e-01  8.5400e-01  5.1216e+00
##
## Std. Errors:
## based on Hessian
```

$$\text{mean eq.} \Rightarrow \hat{\epsilon}_t = 8.434 \times 10^{-4} \quad (1.047 \times 10^{-4})$$

$$\text{vol. eq.} \Rightarrow \hat{\sigma}_t^2 = 1.750 \times 10^{-6} + 0.143 a_{t-1}^2 + 0.854 \sigma_{t-1}^2$$

(3.696E-07) (0.015) (0.013)

```
## Error Analysis:
##      Estimate Std. Error t value Pr(>|t|)
## mu      8.434e-04  1.047e-04   8.057 8.88e-16 ***
## omega   1.750e-06  3.696e-07   4.736 2.19e-06 ***
## alpha1  1.434e-01  1.476e-02   9.719 < 2e-16 ***
## beta1   8.540e-01  1.301e-02  65.646 < 2e-16 ***
```

```
## shape 5.122e+00 4.333e-01 11.821 < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Log Likelihood:
## 13552.39 normalized: 3.315974
##
## Description:
## Thu Apr 29 09:57:23 2021 by user: user
##
##
## Standardised Residuals Tests:
##
##               Statistic p-Value
## Jarque-Bera Test  R      Chi^2 1437.833 0
## Shapiro-Wilk Test  R      W      0.9705412 0
## Ljung-Box Test     R      Q(10) 25.99939 0.003741002
## Ljung-Box Test     R      Q(15) 33.61634 0.003853714
## Ljung-Box Test     R      Q(20) 38.85139 0.006956808
## Ljung-Box Test     R^2    Q(10) 12.3947 0.2595084
## Ljung-Box Test     R^2    Q(15) 17.01071 0.3182243
## Ljung-Box Test     R^2    Q(20) 19.6441 0.4803813
## LM Arch Test       R      TR^2 13.90916 0.3065471
##
## Information Criterion Statistics:
##           AIC          BIC          SIC          HQIC
## -6.629501 -6.621775 -6.629504 -6.626765

plot(ms2,which=13)
```

#from JB test the model is not normal, and from Box test the only adequate for model is volatility equation, the mean equation is not adequate since the pv of residual are all <0.05 then reject H0

#3d

```
predict(ms2,5)
```

```
## meanForecast meanError standardDeviation
## 1 0.0008434408 0.009016638 0.009016638
## 2 0.0008434408 0.009101650 0.009101650
## 3 0.0008434408 0.009185660 0.009185660
## 4 0.0008434408 0.009268693 0.009268693
## 5 0.0008434408 0.009350777 0.009350777
```

#4

```
c = read.table("m-deciles.txt",header=T)
head(c)
```

```
## caldt CAP1RET CAP2RET CAP3RET CAP4RET CAP5RET CAP6RET
## 1 19510131 0.083681 0.082608 0.099147 0.079266 0.087845 0.086179
```

```
## 2 19510228 -0.000102 0.010265 0.008312 0.020972 0.009975 0.004891
## 3 19510331 -0.050423 -0.046779 -0.034764 -0.022521 -0.035481 -0.039383
## 4 19510430 0.037914 0.036413 0.045078 0.031518 0.041554 0.035598
## 5 19510531 -0.033197 -0.031897 -0.026911 -0.030087 -0.027572 -0.025027
## 6 19510629 -0.056899 -0.052380 -0.063182 -0.044404 -0.052655 -0.056175
##      CAP7RET  CAP8RET  CAP9RET  CAP10RET
## 1 0.063453 0.077874 0.054170 0.052145
## 2 0.015361 0.011638 0.017117 0.014894
## 3 -0.038677 -0.027989 -0.018675 -0.016890
## 4 0.044925 0.046933 0.044620 0.053184
## 5 -0.013628 -0.023333 -0.016724 -0.023748
## 6 -0.040582 -0.043436 -0.020323 -0.018880

rc = log(c$CAP9RET+1)
acf(rc)
```

```
#4a
table.Stats(rc)

##
## Observations      720.0000
## NAs                0.0000
## Minimum           -0.3276
## Quartile 1        -0.0190
## Median             0.0144
## Arithmetic Mean    0.0096
## Geometric Mean     0.0083
## Quartile 3         0.0410
## Maximum            0.2038
## SE Mean            0.0018
## LCL Mean (0.95)    0.0059
## UCL Mean (0.95)    0.0132
## Variance           0.0025
## Stdev              0.0496
## Skewness           -0.9583
## Kurtosis           4.4354

t.test(rc)

##
## One Sample t-test
##
## data: rc
## t = 5.1808, df = 719, p-value = 2.873e-07
## alternative hypothesis: true mean is not equal to 0
## 95 percent confidence interval:
## 0.005946562 0.013203545
## sample estimates:
```

```
## mean of x
## 0.009575054
```

```
#pv is less than 0.05 we can't reject h0 then the expected value of Log
return is zero
acf(rc^2)
```

```
Box.test(rc,lag=10,type='Ljung')
```

```
##
## Box-Ljung test
##
## data: rc
## X-squared = 24.257, df = 10, p-value = 0.006946
```

```
#as p-value < 0.05 then we reject H0, so there is autocorrelation between Log
return
```

```
#to us ARMA
```

```
mc1 = auto.arima(rc)
mc1
```

```
## Series: rc
## ARIMA(0,0,2) with non-zero mean
##
## Coefficients:
##          ma1          ma2          mean
##          0.1660 -0.0558  0.0096
## s.e.  0.0373  0.0370  0.0020
##
## sigma^2 estimated as 0.002392: log likelihood=1152.66
## AIC=-2297.32 AICc=-2297.26 BIC=-2279
```

```
summary(mc1)
```

```
## Series: rc
## ARIMA(0,0,2) with non-zero mean
##
## Coefficients:
##          ma1          ma2          mean
##          0.1660 -0.0558  0.0096
## s.e.  0.0373  0.0370  0.0020
##
## sigma^2 estimated as 0.002392: log likelihood=1152.66
## AIC=-2297.32 AICc=-2297.26 BIC=-2279
##
## Training set error measures:
##              ME      RMSE      MAE      MPE      MAPE      MASE
## Training set 1.149455e-06 0.048807 0.03675026 -137.9858 502.9481 0.7525704
##              ACF1
## Training set 0.00044559
```

#4b

```
Box.test(rc^2,lag=10,type='Ljung')
```

```
##
```

```
## Box-Ljung test
```

```
##
```

```
## data: rc^2
```

```
## X-squared = 19.824, df = 10, p-value = 0.03096
```

#as p-value < 0.05 then we reject H0, so there is autocorrelation between log return-squared, hence there is ARCH effects in rt with 95% CI

#4c

```
mc2=garchFit(~arma(1,0)+garch(1,0),data=rc,trace=F)
```

```
## Warning: Using formula(x) is deprecated when x is a character vector of  
length > 1.
```

```
## Consider formula(paste(x, collapse = " ")) instead.
```

```
summary(mc2)
```

```
##
```

```
## Title:
```

```
## GARCH Modelling
```

```
##
```

```
## Call:
```

```
## garchFit(formula = ~arma(1, 0) + garch(1, 0), data = rc, trace = F)
```

```
##
```

```
## Mean and Variance Equation:
```

```
## data ~ arma(1, 0) + garch(1, 0)
```

```
## <environment: 0x00000001ea631c8>
```

```
## [data = rc]
```

```
##
```

```
## Conditional Distribution:
```

```
## norm
```

```
##
```

```
## Coefficient(s):
```

```
##      mu      ar1      omega      alpha1
```

```
## 0.01053 0.14707 0.00200 0.18152
```

```
##
```

```
## Std. Errors:
```

```
## based on Hessian
```

```
##
```

```
## Error Analysis:
```

```
##      Estimate Std. Error t value Pr(>|t|)
```

```
## mu      0.0105300 0.0019275 5.463 4.68e-08 ***
```

```
## ar1      0.1470670 0.0424301 3.466 0.000528 ***
```

```
## omega    0.0020000 0.0001482 13.493 < 2e-16 ***
```

```
## alpha1   0.1815182 0.0651142 2.788 0.005309 **
```

```
## ---
```

```
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
##
## Log Likelihood:
## 1158.628    normalized: 1.609206
##
## Description:
## Thu Apr 29 09:57:24 2021 by user: user
##
##
## Standardised Residuals Tests:
##
##           Statistic p-Value
## Jarque-Bera Test   R    Chi^2 647.6357 0
## Shapiro-Wilk Test  R    W      0.962804 1.502752e-12
## Ljung-Box Test     R    Q(10) 8.582995 0.572082
## Ljung-Box Test     R    Q(15) 12.95811 0.6055337
## Ljung-Box Test     R    Q(20) 15.77362 0.7305655
## Ljung-Box Test     R^2 Q(10) 8.153476 0.6138486
## Ljung-Box Test     R^2 Q(15) 12.29206 0.6568012
## Ljung-Box Test     R^2 Q(20) 13.57787 0.851238
## LM Arch Test       R    TR^2 8.24593 0.7656286
##
## Information Criterion Statistics:
##           AIC      BIC      SIC      HQIC
## -3.207301 -3.181861 -3.207363 -3.197480
```

#all LjungBox test are having pv > 0.05 we cannot reject H0 then the model is adequate in both mean and volatility equation

#Fitted model

$$\text{mean eq. } \hat{r}_t = 0.011 \quad (0.002)$$

$$\text{vol. eq. } \hat{\sigma}_t^2 = 0.147 + 0.002 \hat{\sigma}_{t-1}^2 + 0.182 \hat{\sigma}_{t-1}^2 \quad \begin{matrix} (0.042) & (0.0001) & (0.065) \end{matrix}$$

#4d

```
mc3=garchFit(~arma(1,0)+garch(1,0),data=rc,cond.dist = "std",trace=F)

## Warning: Using formula(x) is deprecated when x is a character vector of
length > 1.
## Consider formula(paste(x, collapse = " ")) instead.

summary(mc3)

##
## Title:
## GARCH Modelling
##
## Call:
## garchFit(formula = ~arma(1, 0) + garch(1, 0), data = rc, cond.dist =
"std",
## trace = F)
##
## Mean and Variance Equation:
## data ~ arma(1, 0) + garch(1, 0)
## <environment: 0x00000000204bc258>
## [data = rc]
```

```
##
## Conditional Distribution:
## std
##
## Coefficient(s):
##      mu      ar1      omega      alpha1      shape
## 0.0116189 0.1076982 0.0019203 0.1900830 6.4225253
##
## Std. Errors:
## based on Hessian
##
## Error Analysis:
##      Estimate Std. Error t value Pr(>|t|)
## mu      0.0116189 0.0017710 6.561 5.35e-11 ***
## ar1      0.1076982 0.0403169 2.671 0.00756 **
## omega    0.0019203 0.0001818 10.564 < 2e-16 ***
## alpha1   0.1900830 0.0713692 2.663 0.00774 **
## shape    6.4225253 1.3115905 4.897 9.74e-07 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Log Likelihood:
## 1187.516 normalized: 1.649328
##
## Description:
## Thu Apr 29 09:57:24 2021 by user: user
##
##
## Standardised Residuals Tests:
##
##      Statistic p-Value
## Jarque-Bera Test R Chi^2 680.4834 0
## Shapiro-Wilk Test R W 0.9612945 7.49198e-13
## Ljung-Box Test R Q(10) 9.486455 0.4866411
## Ljung-Box Test R Q(15) 13.8214 0.5391158
## Ljung-Box Test R Q(20) 17.0087 0.6524086
## Ljung-Box Test R^2 Q(10) 7.567444 0.671006
## Ljung-Box Test R^2 Q(15) 11.42176 0.7221637
## Ljung-Box Test R^2 Q(20) 12.79422 0.8860373
## LM Arch Test R TR^2 7.723697 0.8063327
##
## Information Criterion Statistics:
##      AIC      BIC      SIC      HQIC
## -3.284768 -3.252967 -3.284863 -3.272491
```

#all LjungBox test are having $p_v > 0.05$ we cannot reject H_0 then the model is adequate in both mean and volatility equation

#fitted model

$$\begin{aligned} \text{mean eq. } \hat{\epsilon}_t &= 0.012 (1 - \hat{\theta}_1) + 0.108 \eta_{t-1} \\ &\quad (0.002) \quad (0.040) \\ \text{vol. eq. } \hat{\epsilon}_t^2 &= 0.002 + 0.190 a_{t-1}^2 \\ &\quad (0.0001) \quad (0.071) \end{aligned}$$

#4e

```
mc4=garchFit(~garch(1,0),data=rc,trace=F)
```

```
## Warning: Using formula(x) is deprecated when x is a character vector of
length > 1.
```

```
## Consider formula(paste(x, collapse = " ")) instead.
```

```
summary(mc4)
```

```
##
```

```
## Title:
```

```
## GARCH Modelling
```

```
##
```

```
## Call:
```

```
## garchFit(formula = ~garch(1, 0), data = rc, trace = F)
```

```
##
```

```
## Mean and Variance Equation:
```

```
## data ~ garch(1, 0)
```

```
## <environment: 0x00000000197ba480>
```

```
## [data = rc]
```

```
##
```

```
## Conditional Distribution:
```

```
## norm
```

```
##
```

```
## Coefficient(s):
```

```
## mu omega alpha1
```

```
## 0.012346 0.002016 0.194126
```

```
##
```

```
## Std. Errors:
```

```
## based on Hessian
```

```
##
```

```
## Error Analysis:
```

```
## Estimate Std. Error t value Pr(>|t|)
```

```
## mu 0.012346 0.001923 6.421 1.35e-10 ***
```

```
## omega 0.002016 0.000145 13.900 < 2e-16 ***
```

```
## alpha1 0.194126 0.062209 3.121 0.00181 **
```

```
## ---
```

```
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
##
```

```
## Log Likelihood:
```

```
## 1152.289 normalized: 1.600401
```

```
##
```

```
## Description:
```

```
## Thu Apr 29 09:57:24 2021 by user: user
```

```
##
```

```
##
```

```
## Standardised Residuals Tests:
```

```
## Statistic p-Value
```

```
## Jarque-Bera Test R Chi^2 746.8024 0
```

```
## Shapiro-Wilk Test R W 0.9570702 1.171061e-13
```

```
## Ljung-Box Test R Q(10) 18.72223 0.04393591
```

```
## Ljung-Box Test R Q(15) 23.27998 0.07837365
```

```
## Ljung-Box Test R Q(20) 27.61004 0.1189566
```

```
## Ljung-Box Test      R^2  Q(10)  7.012055  0.7243064
## Ljung-Box Test      R^2  Q(15)  10.3604   0.7964784
## Ljung-Box Test      R^2  Q(20)  11.97825  0.9168225
## LM Arch Test        R      TR^2   7.047101  0.8544853
```

```
##
## Information Criterion Statistics:
##      AIC      BIC      SIC      HQIC
## -3.192468 -3.173388 -3.192503 -3.185102
```

#all LjungBox test are having $p_v > 0.05$ we cannot reject H_0 then the model is adequate in both mean and volatility equation

#fitted model

$$\text{mean eq: } \hat{r}_t = \underset{(0.002)}{0.012}$$

$$\text{vol. eq: } \hat{\sigma}_t^2 = \underset{(0.0201)}{0.002} + \underset{(0.062)}{0.194} a_{t-1}^2$$

#4f

```
mc5=garchFit(~garch(1,0),data=rc,cond.dist = "std",trace=F)
```

```
## Warning: Using formula(x) is deprecated when x is a character vector of
length > 1.
```

```
## Consider formula(paste(x, collapse = " ")) instead.
```

```
summary(mc5)
```

```
##
## Title:
## GARCH Modelling
##
## Call:
## garchFit(formula = ~garch(1, 0), data = rc, cond.dist = "std",
## trace = F)
##
## Mean and Variance Equation:
## data ~ garch(1, 0)
## <environment: 0x000000001ec09ad0>
## [data = rc]
##
## Conditional Distribution:
## std
##
## Coefficient(s):
##      mu      omega    alpha1    shape
## 0.013356 0.001928 0.204163 6.220222
##
## Std. Errors:
## based on Hessian
##
## Error Analysis:
##      Estimate Std. Error t value Pr(>|t|)
## mu      0.013356   0.001685   7.927 2.22e-15 ***
## omega   0.001928   0.000185  10.421 < 2e-16 ***
## alpha1  0.204163   0.072375   2.821 0.00479 **
```

```

## shape    6.220223    1.236608    5.030 4.90e-07 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Log Likelihood:
## 1183.349    normalized:  1.64354
##
## Description:
## Thu Apr 29 09:57:24 2021 by user: user
##
##
## Standardised Residuals Tests:
##
##                               Statistic p-Value
## Jarque-Bera Test      R      Chi^2  746.3878  0
## Shapiro-Wilk Test     R      W      0.9574271 1.363165e-13
## Ljung-Box Test        R      Q(10)  18.51406  0.04688705
## Ljung-Box Test        R      Q(15)  22.99926  0.08415548
## Ljung-Box Test        R      Q(20)  27.3947   0.1245202
## Ljung-Box Test        R^2    Q(10)  6.667871  0.7563837
## Ljung-Box Test        R^2    Q(15)  10.0157   0.8187514
## Ljung-Box Test        R^2    Q(20)  11.63085  0.928196
## LM Arch Test          R      TR^2   6.819315  0.8693193
##
## Information Criterion Statistics:
##          AIC          BIC          SIC          HQIC
## -3.275969 -3.250529 -3.276031 -3.266148

#all LjungBox test are having pv > 0.05, except lag 10 in mean equation, we
cannot reject H0 then the model is adequate in volatility equation.
#but we still have in adequate model in mean equation if project lag is 10
#fitted model mean eq:  $\hat{r}_t^2 = 0.013$ 
#                               (0.002)
#4g vol eq:  $\hat{\sigma}_t^2 = 0.002 + 0.204 a_{t-1}^2$ 
#                               (0.0001) (0.071)
#using AIC and BIC then the lower is the more effective model hence, in (f)
there is lower AIC and BIC which is better

```