

Chapter 6 #3

i) we can take derivative of rdintens with respect to sale and set it equal to 0

$$0.000000014 \text{ sales}^2 = 0.0003$$

$$\text{sales} = 21,428.57$$

The we know that at sales = 21,428.57 the marginal effect of sales on rdintens become (-).

ii) The t-static on $\hat{\beta}_{\text{sales}^2}$ is $-.00000007 / .000000037 = -1.89$, which significant against the one-sided alternative $H_1: \beta_{\text{sales}^2} < 0$.

$$\begin{aligned} \text{iii) rdintens} &= 2.613 + .0003 \text{ sales} - .000000007 \text{ sales}^2 \\ &= 2.613 + 0.003 (1000 * \text{salesbil}) - .000000007 (1000 * \text{salesbil})^2 \\ &= 2.613 + 0.3 \text{ salesbil} - .007 \text{ salesbil}^2 \end{aligned}$$

(s.d.) (.429) (.14) (.0037)

recall that $\text{s.e.}(\hat{\beta}_j) = \frac{\hat{\sigma}^2}{[SST_j(1-R^2)]^{1/2}}$ (3.58). Rescaling sale will have no effect on $\hat{\sigma}^2$ or R^2

since it does not change the fit of the regression. It will, however, affect SST_{sales} and SST_{sales^2} .

$$\begin{aligned} \text{Specifically, } SST_{\text{salesbil}} &= \sum_{i=1}^n (\text{salesbil}_i - \text{salesbil})^2 \\ &= \frac{\sum_{i=1}^n (\text{sales}_i - \text{sales})^2}{1000^2} \\ &= \frac{SST_{\text{sales}}}{1000^2} \end{aligned}$$

$$\text{similarly } SST_{\text{salesbil}^2} = \frac{SST_{\text{sales}^2}}{1000^4}$$

\therefore we need to scale the standard error of $\hat{\beta}_{\text{salesbil}}$ and $\hat{\beta}_{\text{salesbil}^2}$ up by 1000 and 1000² respectively.

iv) equation in part iii because it's easier to read due to it contain fewer zeros to the right of decimal. of course the interpretation of the two equations is identical once of different scales are accounted for.

Chapter 7 #1

i) in the regression equation, the dependant variable is sleep and the independent variables are total work, education, age and dummy male. The coefficient on male is 87.75, so a man is estimated to sleep almost one and one-half more per week than a comparable woman. Further, $t_{\text{male}} = \frac{87.75}{34.33} \approx 2.56$, which is close to the 1% critical value against a two-sided alternative (about 2.58). Thus, the evidence for a gender differential is fairly strong.

ii) The t static on totwrk is $\frac{-163}{.018} \approx -9.06$, which is very statistically significant. The coefficient implies that one more hour of work (60 minutes) is associated with 0.163 (001) = 9.8 mins. less sleep.

iii) The null we are interested in testing here is that the coefficients on age and age² are jointly zero. so we would need to run a restricted version of the regression above where these two variables are omitted and calculate it.

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 chapter 7 #8

i) $\log(\text{wage}) = \beta_0 + \beta_1 \text{usage} + \beta_2 \text{exper} + \beta_3 \text{female} + u$

ii) $\log(\text{wage}) = \beta_0 + \beta_1 \text{usage} + \beta_2 \text{educ} + \beta_3 \text{exper} + \beta_4 \text{female} + \beta_5 \text{usage} \cdot \text{female} + u$

Testing that there are no difference in the effect of drug usage for men and women would involve testing $H_0: \beta_5 = 0$ against

$H_a: \beta_5 \neq 0$

iii) Assuming no interaction effect between usage and sex, the model would look like.

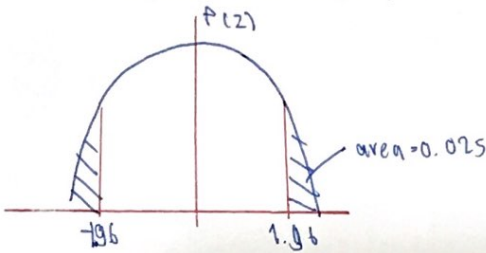
$\log(\text{wage}) = \beta_0 + \beta_1 \text{light} + \beta_2 \text{moderate} + \beta_3 \text{heavy} + \beta_4 \text{educ} + \beta_5 \text{exper} + \beta_6 \text{female} + u$
 in this model, non-user is the omitted category.

iv) The null hypothesis here is $H_0: \beta_1 = \beta_2 = \beta_3 = 0$. Naturally this is going to be an F-test on $q = 3$ restrictions. We are also going to have degrees of freedom $df = n - k - 1$ for a sample of size n , since we have 6 independent variables in the unrestricted model. So we would be obtaining a critical value from the $F_{q, n-k-1}$ distribution.

v) - There may be omitted variables which determine both marijuana usage and wages. For example, people living in urban areas may have easier access to marijuana and may earn higher wages on average. In this example our estimate would be downward biased.

chapter 7 #11

i) A male student have 3.83 more score than a female student.



d.f. = $856 - 2 - 1 = 853$

95% confidence interval = $[3.83 - 1.96(0.74), 3.83 + 1.96(0.74)]$
 $= [2.3706, 5.2804]$

95% confidence interval for β_{male} is excluding zero.

ii) from 3rd model, $H_0: \beta_1 = \beta_3 = 0$
 $H_a: \text{otherwise}$

$F = \frac{(SSR_r - SSR_{ur})/q}{SSR_{ur} / (n - k - 1)} = \frac{R_{ur}^2 - R_r^2 / q}{(1 - R_{ur}^2) / (n - k - 1)} = \frac{(0.349 - 0.329) / 2}{(1 - 0.349) / (856 - 3 - 1)} = 13.0876$

$F = 13.0876 > 2.6$, we reject H_0 at 5% level so gender has an impact on score.

iii) the interaction between male and deviation of colgpa from mean may be better explain

Chapter 7

i) the two signs that are pretty clear are $\beta_3 < 0$ (because hspers is defined so that the smaller the number the better the student) and $\beta_4 > 0$. The effect of size of graduating class (β_1 and β_2) is not clear. It is also unclear whether males and females (β_5) have systematically different GPAs. We may think that $\beta_6 < 0$, that is, athletes do worse than other students with comparable characteristics. But remember, we are controlling for ability to some degree with hspers and sat.

$$\text{ii) } \text{colgpa} = 1.241 - 0.569 \text{ hsize} + 0.0468 \text{ hsize}^2 - 0.132 \text{ hspers} + 0.00165 \text{ sat} + 0.155 \text{ female} + 0.169 \text{ athlete}$$

$$n = 4,137 \quad R^2 = 0.293.$$

Holding other factors fixed, an athlete is predicted to have a GPA about .169 points higher than a nonathlete. The t statistic $\frac{0.169}{0.042} = 4.02$ which is very significant.

iii) with sat dropped from the model, the coefficient on athlete becomes about .0084 (se = 0.0448) which is not significant. This happens because we don't control for SAT scores, and athletes score lower on average than nonathletes. Part ii shows that, once we account for SAT differences, athletes do better than nonathletes. Even if we don't control for SAT score, there is no difference.

iv) To facilitate testing the hypothesis that there is no difference between woman athletes and women nonathletes, we should choose one of these as the base group. We choose female nonathletes.

The estimate equation is

$$\text{colgpa} = 1.386 - 0.0568 \text{ hsize} + 0.0467 \text{ hsize}^2 - 0.132 \text{ hspers} + 0.00165 \text{ sat} + 0.175 \text{ femath} + 0.013 \text{ maleath} - 0.155 \text{ male nonath}$$

$$n = 4,137 \quad R^2 = 0.293$$

The coefficient on female athlete shows that colgpa is predicted to be about .175 points higher for a female athlete than female nonathlete. Other variable in the equation fixed. The hypothesis that there is no difference between female athlete and female nonathletes is tested by using the t statistic on femath. In this case, $t = 2.08$, which is statically significant at the 5% level against a 2 sided alternative.

v) whether we add the interaction female · sat to the equation in part (ii) or part (iv), the outcome is practically the same. For example, when female · sat is added to the equation in part (ii), its coefficient is about .000051 and its t statistic is about .40. There is very little evidence that the effect of sat differs by gender.