

Alpha = .05 (5% level of Significant, or 95% level of confidence)

n\k	k= 1	k= 2	k= 3	k= 4	k= 5	k= 6	k= 7	k= 8	k= 9	k= 10										
n= 6	0.610	1.400																		
n= 7	0.700	1.356	0.467	1.896																
n= 8	0.763	1.332	0.559	1.777	0.367	2.287														
9	0.824	1.320	0.629	1.699	0.455	2.128	0.296	2.588												
10	0.879	1.320	0.697	1.641	0.525	2.016	0.376	2.414	0.243	2.822										
11	0.927	1.324	0.758	1.604	0.595	1.928	0.444	2.283	0.315	2.645	0.203	3.004								
12	0.971	1.331	0.812	1.579	0.658	1.864	0.512	2.177	0.380	2.506	0.268	2.832	0.171	3.149						
13	1.010	1.340	0.861	1.562	0.715	1.816	0.574	2.094	0.444	2.390	0.328	2.692	0.230	2.985	0.147	3.266				
14	1.045	1.350	0.905	1.551	0.767	1.779	0.632	2.030	0.505	2.296	0.389	2.572	0.286	2.848	0.200	3.111	0.127	3.360		
15	1.077	1.361	0.946	1.543	0.814	1.750	0.685	1.977	0.562	2.220	0.447	2.471	0.343	2.727	0.251	2.979	0.175	3.216	0.111	3.438
16	1.106	1.371	0.982	1.539	0.857	1.728	0.734	1.935	0.615	2.157	0.502	2.388	0.398	2.624	0.304	2.860	0.222	3.090	0.155	3.304
17	1.133	1.381	1.015	1.536	0.897	1.710	0.779	1.900	0.664	2.104	0.554	2.318	0.451	2.537	0.356	2.757	0.272	2.975	0.198	3.184
18	1.158	1.391	1.046	1.535	0.933	1.696	0.820	1.872	0.710	2.060	0.603	2.258	0.502	2.461	0.407	2.668	0.321	2.873	0.244	3.073
19	1.180	1.401	1.074	1.536	0.967	1.685	0.859	1.848	0.752	2.023	0.649	2.206	0.549	2.396	0.456	2.589	0.369	2.783	0.290	2.974
20	1.201	1.411	1.100	1.537	0.998	1.676	0.894	1.828	0.792	1.991	0.691	2.162	0.595	2.339	0.502	2.521	0.416	2.704	0.336	2.885
21	1.221	1.420	1.125	1.538	1.026	1.669	0.927	1.812	0.829	1.964	0.731	2.124	0.637	2.290	0.546	2.461	0.461	2.633	0.380	2.806
22	1.239	1.429	1.147	1.541	1.053	1.664	0.958	1.797	0.863	1.940	0.769	2.090	0.677	2.246	0.588	2.407	0.504	2.571	0.424	2.735
23	1.257	1.437	1.168	1.543	1.078	1.660	0.986	1.785	0.895	1.920	0.804	2.061	0.715	2.208	0.628	2.360	0.545	2.514	0.465	2.670
24	1.273	1.446	1.188	1.546	1.101	1.656	1.013	1.775	0.925	1.902	0.837	2.035	0.750	2.174	0.666	2.318	0.584	2.464	0.506	2.613
25	1.288	1.454	1.206	1.550	1.123	1.654	1.038	1.767	0.953	1.886	0.868	2.013	0.784	2.144	0.702	2.280	0.621	2.419	0.544	2.560
26	1.302	1.461	1.224	1.553	1.143	1.652	1.062	1.759	0.979	1.873	0.897	1.992	0.816	2.117	0.735	2.246	0.657	2.379	0.581	2.513
27	1.316	1.469	1.240	1.556	1.162	1.651	1.084	1.753	1.004	1.861	0.925	1.974	0.845	2.093	0.767	2.216	0.691	2.342	0.616	2.470
28	1.328	1.476	1.255	1.560	1.181	1.650	1.104	1.747	1.028	1.850	0.951	1.959	0.874	2.071	0.798	2.188	0.723	2.309	0.649	2.431
29	1.341	1.483	1.270	1.563	1.198	1.650	1.124	1.743	1.050	1.841	0.975	1.944	0.900	2.052	0.826	2.164	0.753	2.278	0.681	2.396
30	1.352	1.489	1.284	1.567	1.214	1.650	1.143	1.739	1.071	1.833	0.998	1.931	0.926	2.034	0.854	2.141	0.782	2.251	0.712	2.363

n\k	k= 1	k= 2	k= 3	k= 4	k= 5	k= 6	k= 7	k= 8	k= 9	k= 10										
31	1.363	1.496	1.297	1.570	1.229	1.650	1.160	1.735	1.090	1.825	1.020	1.920	0.950	2.018	0.879	2.120	0.810	2.226	0.741	2.333
32	1.373	1.502	1.309	1.574	1.244	1.650	1.177	1.732	1.109	1.819	1.041	1.909	0.972	2.004	0.904	2.102	0.836	2.203	0.769	2.306
33	1.383	1.508	1.321	1.577	1.258	1.651	1.193	1.730	1.127	1.813	1.061	1.900	0.994	1.991	0.927	2.085	0.861	2.181	0.796	2.281
34	1.393	1.514	1.333	1.580	1.271	1.652	1.208	1.728	1.144	1.808	1.079	1.891	1.015	1.978	0.950	2.069	0.885	2.162	0.821	2.257
35	1.402	1.519	1.343	1.584	1.283	1.653	1.222	1.726	1.160	1.803	1.097	1.884	1.034	1.967	0.971	2.054	0.908	2.144	0.845	2.236
36	1.411	1.525	1.354	1.587	1.295	1.654	1.236	1.724	1.175	1.799	1.114	1.876	1.053	1.957	0.991	2.041	0.930	2.127	0.868	2.216
37	1.419	1.530	1.364	1.590	1.307	1.655	1.249	1.723	1.190	1.795	1.131	1.870	1.071	1.948	1.011	2.029	0.951	2.112	0.891	2.197
38	1.427	1.535	1.373	1.594	1.318	1.656	1.261	1.722	1.204	1.792	1.146	1.864	1.088	1.939	1.029	2.017	0.970	2.098	0.912	2.180
39	1.435	1.540	1.382	1.597	1.328	1.658	1.273	1.722	1.218	1.789	1.161	1.859	1.104	1.932	1.047	2.007	0.990	2.085	0.932	2.164
40	1.442	1.544	1.391	1.600	1.338	1.659	1.285	1.721	1.230	1.786	1.175	1.854	1.120	1.924	1.064	1.997	1.008	2.072	0.952	2.149
45	1.475	1.566	1.430	1.615	1.383	1.666	1.336	1.720	1.287	1.776	1.238	1.835	1.189	1.895	1.139	1.958	1.089	2.022	1.038	2.088
50	1.503	1.585	1.462	1.628	1.421	1.674	1.378	1.721	1.335	1.771	1.291	1.822	1.246	1.875	1.201	1.930	1.156	1.986	1.110	2.044
55	1.528	1.601	1.490	1.641	1.452	1.681	1.414	1.724	1.374	1.768	1.334	1.814	1.294	1.861	1.253	1.909	1.212	1.959	1.170	2.010
60	1.549	1.616	1.514	1.652	1.480	1.689	1.444	1.727	1.408	1.767	1.372	1.808	1.335	1.850	1.298	1.894	1.260	1.939	1.222	1.984
65	1.567	1.629	1.536	1.662	1.503	1.696	1.471	1.731	1.438	1.767	1.404	1.805	1.370	1.843	1.336	1.882	1.301	1.923	1.266	1.964
70	1.583	1.641	1.554	1.672	1.525	1.703	1.494	1.735	1.464	1.768	1.433	1.802	1.401	1.838	1.369	1.874	1.337	1.910	1.305	1.948
75	1.598	1.652	1.571	1.680	1.543	1.709	1.515	1.739	1.487	1.770	1.458	1.801	1.428	1.834	1.399	1.867	1.369	1.901	1.339	1.935
80	1.611	1.662	1.586	1.688	1.560	1.715	1.534	1.743	1.507	1.772	1.480	1.801	1.453	1.831	1.425	1.861	1.397	1.893	1.369	1.925
85	1.624	1.671	1.600	1.696	1.575	1.721	1.550	1.747	1.525	1.774	1.500	1.801	1.474	1.829	1.448	1.857	1.422	1.886	1.396	1.916
90	1.635	1.679	1.612	1.703	1.589	1.726	1.566	1.751	1.542	1.776	1.518	1.801	1.494	1.827	1.469	1.854	1.445	1.881	1.420	1.909
95	1.645	1.687	1.623	1.709	1.602	1.732	1.579	1.755	1.557	1.778	1.535	1.802	1.512	1.827	1.489	1.852	1.465	1.877	1.442	1.903
100	1.654	1.694	1.634	1.715	1.613	1.736	1.592	1.758	1.571	1.780	1.550	1.803	1.528	1.826	1.506	1.850	1.484	1.874	1.462	1.898
150	1.720	1.747	1.706	1.760	1.693	1.774	1.679	1.788	1.665	1.802	1.651	1.817	1.637	1.832	1.622	1.846	1.608	1.862	1.593	1.877
200	1.758	1.779	1.748	1.789	1.738	1.799	1.728	1.809	1.718	1.820	1.707	1.831	1.697	1.841	1.686	1.852	1.675	1.863	1.665	1.874

Final Exam: Monday, 13th May: 13:30-16:30 hr

- What can you bring?
 1. One calculator (Simple or Scientific or Financial)
 2. A4 CheatSheet - can be written on both sides.
MUST be the original copy of your own hand-writing.
- What will be on the exam?
 - Multiple regression onward. (page 47 onward).
- Exam problems will be similar to the homework & practice questions.

Some useful concepts

i) Biasedness of $\hat{\beta}_{OLS}$

→ Happens when at least one of SLR 1-4, MLR 1-4 or TS 1-3 is violated.

→ The zero conditional mean assumption is usually violated, leading to the omitted variable bias

$$\text{SLR 4: } E(u|X) = 0 \text{ or } \text{Cov}(u, X) = 0$$

$$\text{MLR 4: } E(u|X_1, X_2, \dots, X_k) = 0 \text{ or}$$
$$\text{Cov}(u, X_i | X_2, \dots, X_k) = 0$$
$$\text{Cov}(u, X_2 | X_1, \dots, X_k) = 0 \text{ etc}$$

$$\text{TS 3: } E(u_t | X) = 0$$

either one of these needs to be satisfied for a reliable estimation.

If this can be satisfied, the $\hat{\beta}_{OLS}$ unbiased?

If only this can be satisfied, $\hat{\beta}_{OLS}$ will not be unbiased. But $\hat{\beta}_{OLS}$ will still be consistent. So, if the sample size "N" gets large, $\hat{\beta}_{OLS}$ will become more and more precise.

1) if strictly exogenous, then we need $E(u_t | X_{1t}, \dots, X_{kt}, X_{1,t-2}, \dots, X_{k,t-1}, X_{1,t-2}, \dots \text{ etc})$
all X in all time periods. \Rightarrow unlikely to be true.

2) if weakly exogenous, then we need $E(u_t | X_{1t}, \dots, X_{kt})$
all X in the same time period \Rightarrow more realistic.

2) Heteroskedasticity - does not affect unbiasedness. But if we don't recognize it and use the usual Homosked. calculation for the std. err. ($\sqrt{\text{var}(\hat{\beta}_{OLS})}$), our inferences (t-test, F-test, LM-test, etc.) will be invalid.

$$\text{Heteroskedasticity} \leadsto \text{Cov}(\text{Var}(u), X) \neq 0$$

3) Serial- / Auto-correlation - same impact as heterosk.

$$\text{Serial correlation} \rightarrow \text{Cov}(u_t, u_{t+1}) \neq 0$$

$$\text{Auto correlation} \rightarrow \text{Cov}(u_i, u_{i+1}) \neq 0$$

Practice Questions

- 1) Understand all the homeworks for chapter 3, 4, 6
- 2) Suggested problems for chapter 3, 7, 8, 12 (check Moodle)

In-class exercise

Chapters 3, 6, 9 The following equation describes the median housing price in a community in terms of amount of pollution (*nox* for nitrous oxide) and the average number of rooms in houses in the community (*rooms*):

$$\log(\text{price}) = \beta_0 + \beta_1 \log(\text{nox}) + \beta_2 \text{rooms} + u.$$

- (i) What are the probable signs of β_1 and β_2 ? What is the interpretation of β_1 ? Explain.
- (ii) Why might *nox* [or more precisely, $\log(\text{nox})$] and *rooms* be negatively correlated? If this is the case, does the simple regression of $\log(\text{price})$ on $\log(\text{nox})$ produce an upward or a downward biased estimator of β_1 ?
- (iii) Using the data in HPRICE2, the following equations were estimated:

$$\widehat{\log(\text{price})} = 11.71 - 1.043 \log(\text{nox}), n = 506, R^2 = .264.$$

$$\widehat{\log(\text{price})} = 9.23 - .718 \log(\text{nox}) + .306 \text{rooms}, n = 506, R^2 = .514.$$

Is the relationship between the simple and multiple regression estimates of the elasticity of *price* with respect to *nox* what you would have predicted, given your answer in part (ii)? Does this mean that $-.718$ is definitely closer to the true elasticity than -1.043 ?