

Assignment 5 -- Solution

From the data set Assign_TimeSeries:

1. Estimate Autoregressive Integrated Moving Average (ARIMA(p,d,q)) model for spot return (spot) and future return (future) – determine the most appropriated order for p, d, and q using BIC given the maximum lag equals 3.

```
. do "J:\TU\ECON\EE435\Assignments\Assignment05.do"
. *Define Variable y
.   g y = spot
(4 missing values generated)
. *Specify order p d q
. forvalue d = 0(1)0 {
2.   forvalue p = 1(1)3 {
3.     forvalue q = 1(1)3 {
4.       display "estimate arima`p'`d'`q'"
5.       capture: quietly arch y, arima(`p',`d',`q') nolog
6.       if _rc~=0 {
7.         display "flat log when pdq =" `p'`d'`q'
8.         continue
9.       }
10.      estimates store arima`p'`d'`q'
11.      display "arima`p'`d'`q' already estimated"
12.    }
13.  }
14. estimates table arima1`d'1 arima1`d'2 arima1`d'3, star(0.1 0.05 0.01) stat(aic bic ll)
15. estimates table arima2`d'1 arima2`d'2 arima2`d'3, star(0.1 0.05 0.01) stat(aic bic ll)
16. estimates table arima3`d'1 arima3`d'2 arima3`d'3, star(0.1 0.05 0.01) stat(aic bic ll)
17. }
estimate arima101
arima101 already estimated
estimate arima102
arima102 already estimated
estimate arima103
arima103 already estimated
estimate arima201
arima201 already estimated
estimate arima202
arima202 already estimated
estimate arima203
arima203 already estimated
estimate arima301
arima301 already estimated
estimate arima302
arima302 already estimated
estimate arima303
arima303 already estimated
```

Variable	arima101	arima102	arima103
y			
_cons	.00235741	.00235788	.00235884
ARMA			
ar			
L1.	-.39230156***	.42864188***	.65151421**
ma			
L1.	.44524247***	-.38281716***	-.60599959**
L2.		-.06805846***	-.07856536***
L3.			.01544447
SI GMA2			
_cons	.03191009***	.0318591***	.0318577***
Statistics			
aic	-4655.2422	-4665.5424	-4663.9162
bic	-4627.4551	-4630.8085	-4622.2356
ll	2331.6211	2337.7712	2337.9581

Legend: * p<.1; ** p<.05; *** p<.01

Variable	arima201	arima202	arima203
y			
_cons	.00235716	.00235872	.00235613

ARMA			
ar			
L1.	.38030326***	.44305108***	-.29690212
L2.	-.06527105***	.06478823	.18533487
ma			
L1.	-.33479683**	-.39733898***	.34286602
L2.		-.13333505	-.22071408
L3.			-.04555167

SIGMA2			
_cons	.0318617***	.03185804***	.03185812***

Statistics			
aic	-4664.9752	-4663.7362	-4661.7463
bic	-4630.2413	-4622.0556	-4613.1189
ll	2337.4876	2337.8681	2337.8731

Legend: * p<.1; ** p<.05; *** p<.01			

Variable	arima301	arima302	arima303

y			
_cons	.00235766	.00235746	.00235826

ARMA			
ar			
L1.	.77459277***	.75374093	-.00990197
L2.	-.08502045***	-.07129309	.14114161
L3.	.02488932	.02349443	.27351658*
ma			
L1.	-.72897906***	-.70811284	.05503806
L2.		-.01280924	-.19123469
L3.			-.29976449**

SIGMA2			
_cons	.03185649***	.0318562***	.03184624***

Statistics			
aic	-4664.1345	-4662.137	-4662.6339
bic	-4622.4539	-4613.5097	-4607.0598
ll	2338.0672	2338.0685	2339.317

Legend: * p<.1; ** p<.05; *** p<.01			

. drop y

. *Define Variable y
 . g y = future
 (4 missing values generated)

```

. *Specify order p d q
. forvalue d = 0(1)0 {
2.   forvalue p = 1(1)3 {
3.     forvalue q = 1(1)3 {
4.       display "estimate arima`p'`d'`q'"
5.       capture: quietly arima y, arima(`p',`d',`q') nolog
6.       if _rc~=0 {
7.         display "flatlog when pdq =" `p'`d'`q'
8.         continue
9.       }
10.      estimates store arima`p'`d'`q'
11.      display "arima`p'`d'`q' already estimated"
12.    }
13.  }
14. estimates table arima1`d'1 arima1`d'2 arima1`d'3, star(0.1 0.05 0.01) stat(aic bic ll)
15. estimates table arima2`d'1 arima2`d'2 arima2`d'3, star(0.1 0.05 0.01) stat(aic bic ll)
16. estimates table arima3`d'1 arima3`d'2 arima3`d'3, star(0.1 0.05 0.01) stat(aic bic ll)
17. }
estimate arima101
arima101 already estimated
estimate arima102
arima102 already estimated
estimate arima103
arima103 already estimated
estimate arima201
arima201 already estimated
estimate arima202
arima202 already estimated
estimate arima203
arima203 already estimated
estimate arima301
arima301 already estimated
estimate arima302
arima302 already estimated

```

estimate arima303
 arima303 already estimated

Variable	arima101	arima102	arima103
y			
_cons	.00261517	.00261579	.00261577
ARMA			
ar			
L1.	.57881552***	.16418729	-.99197565***
ma			
L1.	-.61268782***	-.1922571	.96411185***
L2.		-.03062454**	-.06339421***
L3.			-.03780679***
sigma			
_cons	.20593659***	.20590197***	.20586946***
Statistics			
aic	-2469.7286	-2470.3208	-2470.7314
bic	-2441.9415	-2435.587	-2429.0509
ll	1238.8643	1240.1604	1241.3657

Legend: * p<.1; ** p<.05; *** p<.01

Variable	arima201	arima202	arima203
y			
_cons	.00261336	.00261592	.00261574
ARMA			
ar			
L1.	.19702513	.15238162	-.89451145***
L2.	-.02960415**	.01290458	.09684725
ma			
L1.	-.22511772	-.18046541	.8667681***
L2.		-.0438418	-.15730465
L3.			-.03516023***
sigma			
_cons	.2059025***	.20590188***	.20586829***
Statistics			
aic	-2470.3006	-2468.3228	-2468.821
bic	-2435.5668	-2426.6422	-2420.1936
ll	1240.1503	1240.1614	1241.4105

Legend: * p<.1; ** p<.05; *** p<.01

Variable	arima301	arima302	arima303
y			
_cons	.0026159	.0026158	.00261599
ARMA			
ar			
L1.	.43865033	-.86030504***	-.52633415***
L2.	-.0229658	.09653429	-.40298947**
L3.	.00955072	-.03405749***	.51822432***
ma			
L1.	-.46673101	.83253098***	.495946***
L2.		-.15579179	.35985892**
L3.			-.55439735***
sigma			
_cons	.20590156***	.20586899***	.20582887***
Statistics			
aic	-2468.3416	-2468.7519	-2469.7457
bic	-2426.661	-2420.1245	-2414.1716
ll	1240.1708	1241.3759	1242.8729

Legend: * p<.1; ** p<.05; *** p<.01

end of do-file

According to BIC, the optimal lag for spot is ARIMA(1,0,2) or ARMA(1,2) and for future is ARIMA(1,0,1) or ARMA(1,1).

- Estimate GARCH(p,q) for spot return (spot) using future return (future) as explanatory variable for mean equation – Test whether there exists significant GARCH effect and determine the most appropriated order p and q for variance equation using SBIC given the maximum lag equals to 2.

. reg spot future

Source	SS	df	MS			
Model	115.395382	1	115.395382	Number of obs =	7683	
Residual	130.581975	7681	.017000648	F(1, 7681) =	6787.71	
Total	245.977357	7682	.032019963	Prob > F =	0.0000	
				R-squared =	0.4691	
				Adj R-squared =	0.4691	
				Root MSE =	.13039	

spot	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]
future	.594594	.007217	82.39	0.000	.5804466 .6087413
_cons	.0008007	.0014877	0.54	0.590	-.0021155 .0037169

. estat archlm

LM test for autoregressive conditional heteroskedasticity (ARCH)

lags(p)	chi 2	df	Prob > chi 2
1	4.919	1	0.0266

H0: no ARCH effects vs. H1: ARCH(p) disturbance

. arch spot future, arch(1/1) nolog

ARCH family regression

Sample: 2 - 7684
 Distribution: Gaussian
 Log likelihood = 4828.862

Number of obs = 7683
 Wald chi2(1) = 199295.46
 Prob > chi2 = 0.0000

spot	Coef.	OPG Std. Err.	z	P> z	[95% Conf. Interval]
spot					
future	.6210706	.0013912	446.43	0.000	.6183439 .6237973
_cons	.0009981	.0014105	0.71	0.479	-.0017665 .0037626
ARCH					
arch L1	.1165968	.0073186	15.93	0.000	.1022526 .130941
_cons	.0152236	.0000738	206.28	0.000	.015079 .0153683

. estat ic

Model	Obs	ll (null)	ll (model)	df	AIC	BIC
.	7683	.	4828.862	4	-9649.723	-9621.936

Note: N=obs used in calculating BIC; see [R] BIC note

. arch spot future, arch(1/2) nolog

ARCH family regression

Sample: 2 - 7684
 Distribution: Gaussian
 Log likelihood = 5115.985

Number of obs = 7683
 Wald chi2(1) = 129655.42
 Prob > chi2 = 0.0000

spot	Coef.	OPG Std. Err.	z	P> z	[95% Conf. Interval]
spot					
future	.6005641	.0016679	360.08	0.000	.5972952 .6038331
_cons	-.0000788	.0009416	-0.08	0.933	-.0019243 .0017668

ARCH							
arch	L1.	.1095337	.0080471	13.61	0.000	.0937617	.1253057
	L2.	.3383839	.0067081	50.44	0.000	.3252362	.3515316
	_cons	.0108903	.0001084	100.43	0.000	.0106777	.0111028

. estat ic

Model	Obs	ll (null)	ll (model)	df	AIC	BIC
.	7683	.	5115.985	5	-10221.97	-10187.24

Note: N=Obs used in calculating BIC; see [R] BIC note

. arch spot future, arch(1/1) garch(1/1) nolog

ARCH family regression

Sample: 2 - 7684
 Distribution: Gaussian
 Log likelihood = 5137.242
 Number of obs = 7683
 Wald chi2(1) = 126855.94
 Prob > chi2 = 0.0000

spot		Coef.	OPG Std. Err.	z	P> z	[95% Conf. Interval]	
spot	future	.6471733	.001817	356.17	0.000	.643612	.6507347
	_cons	.0000654	.001113	0.06	0.953	-.002116	.0022468
ARCH							
arch	L1.	.1833993	.0074921	24.48	0.000	.1687151	.1980835
garch	L1.	.6065925	.0136351	44.49	0.000	.5798682	.6333168
	_cons	.0038578	.0001449	26.62	0.000	.0035738	.0041418

. estat ic

Model	Obs	ll (null)	ll (model)	df	AIC	BIC
.	7683	.	5137.242	5	-10264.48	-10229.75

Note: N=Obs used in calculating BIC; see [R] BIC note

. arch spot future, arch(1/1) garch(1/2) nolog

ARCH family regression

Sample: 2 - 7684
 Distribution: Gaussian
 Log likelihood = 5155.231
 Number of obs = 7683
 Wald chi2(1) = 131273.02
 Prob > chi2 = 0.0000

spot		Coef.	OPG Std. Err.	z	P> z	[95% Conf. Interval]	
spot	future	.6400245	.0017665	362.32	0.000	.6365623	.6434868
	_cons	-.0002536	.0010592	-0.24	0.811	-.0023297	.0018225
ARCH							
arch	L1.	.1704474	.0078817	21.63	0.000	.1549996	.1858951
garch	L1.	.8489987	.0319169	26.60	0.000	.7864427	.9115547
	L2.	-.206975	.0208913	-9.91	0.000	-.2479213	-.1660288
	_cons	.0035026	.0001258	27.84	0.000	.003256	.0037492

. estat ic

Model	Obs	ll (null)	ll (model)	df	AIC	BIC
.	7683	.	5155.231	6	-10298.46	-10256.78

Note: N=Obs used in calculating BIC; see [R] BIC note

. arch spot future, arch(1/2) garch(1/1) nolog

ARCH family regression

Sample: 2 - 7684
 Distribution: Gaussian
 Log likelihood = 5199.879
 Number of obs = 7683
 Wald chi2(1) = 127298.70
 Prob > chi2 = 0.0000

spot		Coef.	OPG Std. Err.	z	P> z	[95% Conf. Interval]	
spot	future	.6259136	.0017543	356.79	0.000	.6224753	.629352
	_cons	-.0008745	.0009739	-0.90	0.369	-.0027832	.0010343
ARCH							
	arch						
	L1.	.103905	.0084471	12.30	0.000	.087349	.1204609
	L2.	.237832	.006037	39.40	0.000	.2259997	.2496642
	garch						
	L1.	.3403756	.0079198	42.98	0.000	.3248531	.3558981
	_cons	.006225	.0001099	56.63	0.000	.0060095	.0064404

. estat ic

Model	Obs	ll (null)	ll (model)	df	AIC	BIC
.	7683	.	5199.879	6	-10387.76	-10346.08

Note: N=obs used in calculating BIC; see [R] BIC note

. arch spot future, arch(1/2) garch(1/2) nolog

ARCH family regression

Sample: 2 - 7684
 Distribution: Gaussian
 Log likelihood = 5221.741
 Number of obs = 7683
 Wald chi2(1) = 120955.67
 Prob > chi2 = 0.0000

spot		Coef.	OPG Std. Err.	z	P> z	[95% Conf. Interval]	
spot	future	.6237113	.0017934	347.79	0.000	.6201963	.6272262
	_cons	-.0010619	.0009468	-1.12	0.262	-.0029175	.0007937
ARCH							
	arch						
	L1.	.101415	.0082531	12.29	0.000	.0852392	.1175908
	L2.	.2988581	.0063882	46.78	0.000	.2863375	.3113788
	garch						
	L1.	.0765849	.0154151	4.97	0.000	.0463719	.1067979
	L2.	.1771549	.0174297	10.16	0.000	.1429932	.2113165
	_cons	.006862	.0001357	50.58	0.000	.0065961	.0071278

. estat ic

Model	Obs	ll (null)	ll (model)	df	AIC	BIC
.	7683	.	5221.741	7	-10429.48	-10380.85

Note: N=obs used in calculating BIC; see [R] BIC note

According to ARCH-LM test, there exists significant ARCH effect. The most appropriated order p and q for variance equation using SBIC given the maximum lag equals to 2 is GARCH(2, 2)

3. Estimate VARs models using spot return (spot) and future return (future) as endogenous variables and determine the most appropriated lags models using SBIC.

. varsoc spot future

Selection-order criteria
 Sample: 6 - 7684
 Number of obs = 7679

Lag	LL	LR	df	p	FPE	AIC	HQIC	SBIC
0	5979.48				.000723	-1.55684	-1.55622	-1.55503
1	6150.21	341.45	4	0.000	.000692	-1.60026	-1.5984	-1.59483
2	6239.97	179.52	4	0.000	.000677	-1.6226	-1.6195	-1.61355
3	6273	66.06	4	0.000	.000672	-1.63016	-1.62582	-1.6175*
4	6289.45	32.907*	4	0.000	.000669*	-1.6334*	-1.62782*	-1.61712

Endogenous: spot future
 Exogenous: _cons

. var spot future, lag(1/3)

Vector autoregression

Sample: 5 - 7684
 Log likelihood = 6274.733
 FPE = .0006714
 Det(Sigma_ml) = .000669

No. of obs = 7680
 AIC = -1.630399
 HQIC = -1.626056
 SBIC = -1.617737

Equation	Parms	RMSE	R-sq	chi 2	P>chi 2
spot	7	.17791	0.0122	95.07421	0.0000
future	7	.204367	0.0181	141.3296	0.0000

	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]
spot					
spot					
L1.	-.0323987	.0159661	-2.03	0.042	-.0636918 -.0011057
L2.	-.1099664	.0160841	-6.84	0.000	-.1414905 -.0784422
L3.	-.0418984	.0159205	-2.63	0.008	-.0731019 -.0106949
future					
L1.	.0933035	.0138966	6.71	0.000	.0660668 .1205403
L2.	.0688434	.0141336	4.87	0.000	.0411421 .0965447
L3.	.0317131	.0139194	2.28	0.023	.0044315 .0589946
_cons	.0023077	.0020298	1.14	0.256	-.0016705 .006286
future					
spot					
L1.	.2004382	.0183405	10.93	0.000	.1644915 .2363849
L2.	.0600679	.018476	3.25	0.001	.0238557 .0962801
L3.	.0609707	.018288	3.33	0.001	.0251268 .0968146
future					
L1.	-.1528221	.0159632	-9.57	0.000	-.1841093 -.1215349
L2.	-.0926647	.0162354	-5.71	0.000	-.1244855 -.0608439
L3.	-.0524571	.0159894	-3.28	0.001	-.0837958 -.0211184
_cons	.0026168	.0023316	1.12	0.262	-.0019531 .0071866

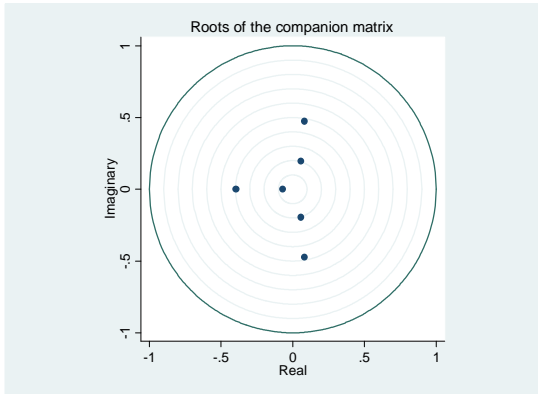
4. Perform stability test and Granger exogeneity test.

. varstable, graph

Eigenvalue stability condition

Eigenvalue	Modulus
.0829301 + .4737693i	.480973
.0829301 - .4737693i	.480973
-.3959128	.395913
.05719759 + .1954789i	.203675
.05719759 - .1954789i	.203675
-.06956341	.069563

All the eigenvalues lie inside the unit circle.
 VAR satisfies stability condition.



```
. vargranger
```

Granger causality Wald tests

Equation	Excluded	chi 2	df	Prob > chi 2
spot	future	58.069	3	0.000
spot	ALL	58.069	3	0.000
future	spot	125.3	3	0.000
future	ALL	125.3	3	0.000

5. Perform Impulse response analysis and determine which variable has more impact.

```
. irf create order1, o(spot future) step(10) set(irf01)
(file irf01.irf created)
(file irf01.irf now active)
(file irf01.irf updated)
```

```
. irf table oirf, impulse(spot future) response(spot future)
```

Results from order1

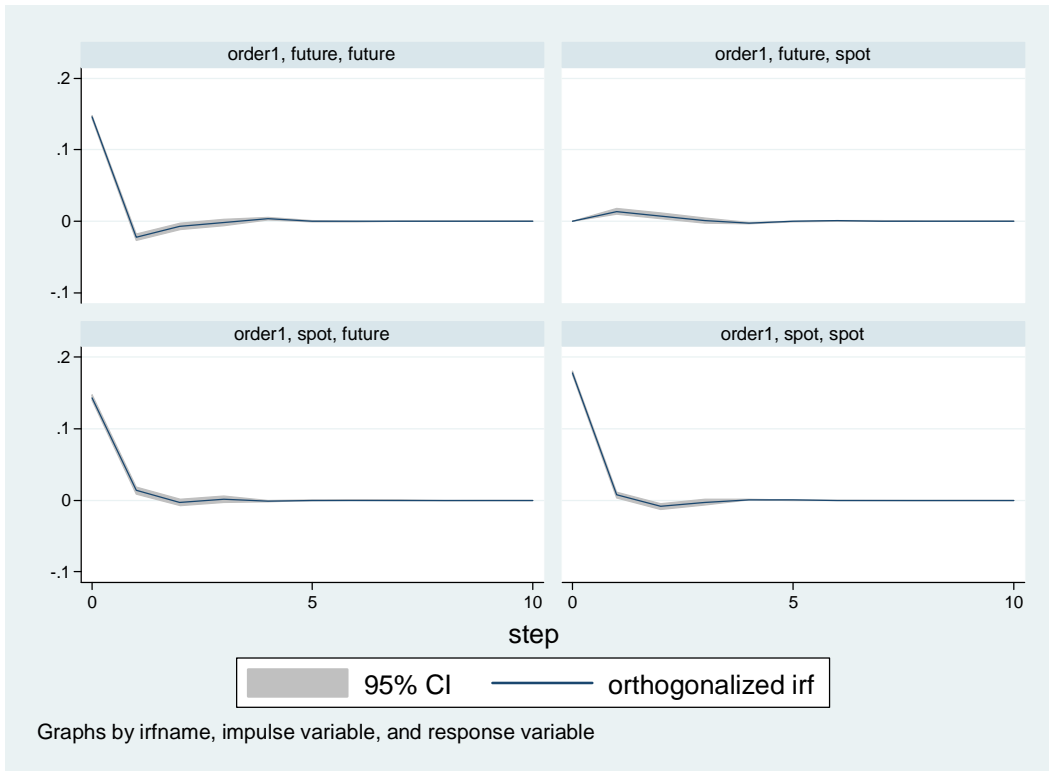
step	(1) oirf	(1) Lower	(1) Upper	(2) oirf	(2) Lower	(2) Upper
0	.177829	.175017	.180641	.143437	.139471	.147402
1	.007622	.003634	.01161	.013723	.009126	.018321
2	-.008647	-.012632	-.004662	-.003179	-.007773	.001415
3	-.002812	-.006788	.001165	.001257	-.003325	.005839
4	.001056	.000349	.001764	-.001236	-.00202	-.000451
5	.000508	.000035	.00098	-.000245	-.000701	.00021
6	-.000083	-.00028	.000115	.00008	-.000104	.000264
7	-.000146	-.000267	-.000025	.000154	.000013	.000294
8	4.6e-06	-.000041	.00005	-.000021	-.000056	.000013
9	.000031	6.8e-06	.000054	-.000028	-.000052	-3.8e-06
10	5.4e-06	-1.0e-05	.000021	-4.3e-06	-.000019	.00001

step	(3) oirf	(3) Lower	(3) Upper	(4) oirf	(4) Lower	(4) Upper
0	0	0	0	.145444	.143144	.147744
1	.01357	.009603	.017538	-.022227	-.026791	-.017663
2	.007499	.003558	.011441	-.007361	-.011912	-.00281
3	.00066	-.003215	.004536	-.002127	-.006604	.00235
4	-.002825	-.004018	-.001631	.003583	.001998	.005169
5	-.000341	-.001009	.000328	-.000034	-.00066	.000592
6	.00047	.000208	.000732	-.000413	-.000688	-.000138
7	.000213	-.000033	.00046	-.00022	-.000492	.000051
8	-.000094	-.000155	-.000034	.000124	.000058	.00019
9	-.000057	-.000109	-4.2e-06	.000046	-5.3e-06	.000097
10	9.1e-06	-.000013	.000031	-.000011	-.000031	8.6e-06

95% lower and upper bounds reported

- (1) irfname = order1, impulse = spot, and response = spot
- (2) irfname = order1, impulse = spot, and response = future
- (3) irfname = order1, impulse = future, and response = spot
- (4) irfname = order1, impulse = future, and response = future

```
. irf graph oirf, impulse(spot future) response(spot future)
```



```
. irf table coi rf, impulse(spot future) response(spot future)
```

Results from order1

step	(1) coi rf	(1) Lower	(1) Upper	(2) coi rf	(2) Lower	(2) Upper
0	.177829	.175017	.180641	.143437	.139471	.147402
1	.185451	.180502	.190399	.15716	.151277	.163044
2	.176804	.170404	.183203	.153981	.146686	.161275
3	.173992	.16649	.181494	.155238	.146795	.16368
4	.175048	.167609	.182487	.154002	.145719	.162285
5	.175556	.168363	.182748	.153757	.145689	.161824
6	.175473	.16832	.182625	.153837	.14578	.161893
7	.175327	.16814	.182513	.15399	.145903	.162078
8	.175331	.168135	.182528	.153969	.145881	.162057
9	.175362	.16817	.182554	.153941	.145858	.162023
10	.175367	.168179	.182556	.153937	.145855	.162018

step	(3) coi rf	(3) Lower	(3) Upper	(4) coi rf	(4) Lower	(4) Upper
0	0	0	0	.145444	.143144	.147744
1	.01357	.009603	.017538	.123217	.118267	.128167
2	.02107	.015385	.026754	.115856	.109296	.122416
3	.02173	.014984	.028476	.113729	.106101	.121358
4	.018905	.013154	.024656	.117313	.11086	.123766
5	.018564	.013156	.023973	.117279	.111077	.123481
6	.019035	.013538	.024531	.116866	.110547	.123185
7	.019248	.013625	.024871	.116646	.110216	.123075
8	.019154	.013546	.024761	.11677	.110373	.123166
9	.019097	.013518	.024676	.116815	.110443	.123188
10	.019106	.013531	.024681	.116804	.11043	.123178

95% lower and upper bounds reported

- (1) irfname = order1, impulse = spot, and response = spot
- (2) irfname = order1, impulse = spot, and response = future
- (3) irfname = order1, impulse = future, and response = spot
- (4) irfname = order1, impulse = future, and response = future

```
. irf graph coi rf, impulse(spot future) response(spot future)
```

