

RISK

→ uncertain

→ Fluctuation of return

from normal level



Average

Mean of return weighted by

Probability sum of

$$E(V) = \text{Prob} \times \text{payoff}$$

invest for 100 millions brant

AD

possibility

① shopping center

② condominium

Expected

Payoff (cost)

180

120

Normal curve

CO.2

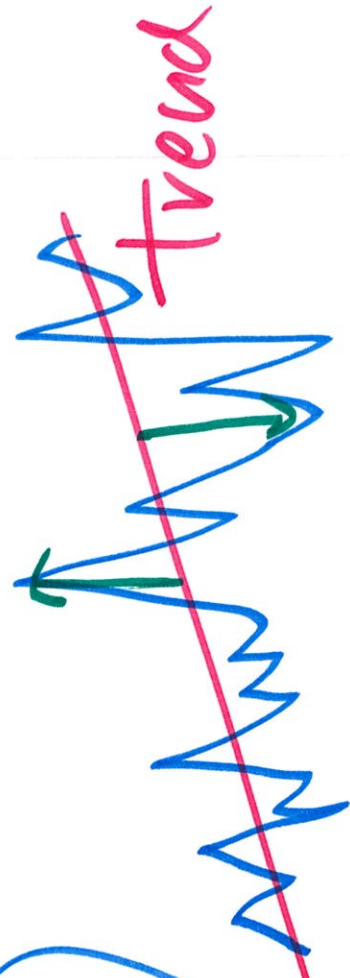
Recession

-90

110

probability

RISK



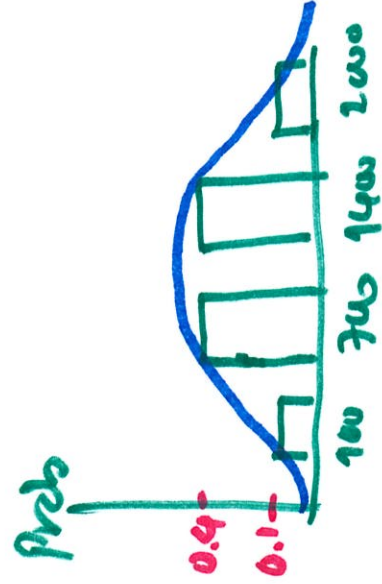
→ standard deviation

Possibility	Prob	Payoff	Prob x Payoff	EV	(Deviation) ²
# 1	0.1	100	0.1(100)	10	$(100 - 1050)^2 = (-950)^2$
# 2	0.4	700	0.4(700)	280	$(700 - 1050)^2 = (-350)^2$
# 3	0.4	1400	0.4(1400)	560	$(1400 - 1050)^2 = (+350)^2$
# 4	0.1	2000	0.1(2000)	200	$(2000 - 1050)^2 = (+950)^2$

$$\begin{aligned}
 \text{EV} &= \text{sum}(\text{Prob} \times \text{Payoff}) \\
 &= 0.1(100) + 0.4(700) + 0.4(1400) + 0.1(2000) \\
 &= 1050
 \end{aligned}$$

$$\begin{aligned}
 \text{variance} &= \text{sum}[\text{Prob} \times (\text{Deviation})^2] \\
 &= 0.1(902,500) + 0.4(122,500) + 0.4(122,500) \\
 &\quad + 0.1(902,500) \\
 &= 278,500
 \end{aligned}$$

$$\begin{aligned}
 \text{Standard deviation} &= \sqrt{\text{variance}} \\
 &= \sqrt{278,500} = 528
 \end{aligned}$$



Hedging → buy two different assets,
 whose prices / returns move
 on different directions

Probability	Payoff of possibility	
	GE	Texaco
oil price increase $\frac{1}{2}$	100	120
oil price decrease $\frac{1}{2}$	120	100

Strategy: Buy only ONE asset calculate $E(V)$

① Buy GE $E(V) = \frac{1}{2}(100) + \frac{1}{2}(120) = 110$

② Buy Texaco $E(V) = \frac{1}{2}(120) + \frac{1}{2}(100) = 110$

calculate variance & standard deviation

$$SD \rightarrow \sigma_{GE} = \sqrt{\frac{1}{2}(100-110)^2 + \frac{1}{2}(120-110)^2}$$
$$= \sqrt{100}$$

$$= 10$$
$$\sigma_{TEXAO} = \sqrt{\frac{1}{2}(120-110)^2 + \frac{1}{2}(100-110)^2}$$
$$= \sqrt{100}$$
$$= 10$$

strategy \rightarrow invest in both asset

Payoff table	GE	TAXACO	Total Payoff	Prob
Possibility				
oil price decrease # 1	60	50	110	$1/2$
oil price increase # 2	50	60	110	$1/2$

① Calculate EV)

$$E(V)_{\text{Hedging}} = \frac{1}{2}(110) + \frac{1}{2}(110) = 110$$

② calculate standard deviation

$$SD = \sqrt{\frac{1}{2}(110 - 110)^2 + \frac{1}{2}(110 - 110)^2} = 0$$

By hedging strategy, we must eliminate risk

$$\rightarrow STD = 0$$

spreading \rightarrow Buying more than one asset

But, these assets should not be completely related

\rightarrow could move in the same direction
or opposite direction

Payoff Table

Possibility	GE	Microsoft	Total Payoff	Prob
# 1 price move in the same side (increase)	60	60	120	$\frac{1}{4}$
# 2 only GE price increases	60	50	110	$\frac{1}{4}$
# 3 only MS price increases	50	60	110	$\frac{1}{4}$
# 4 prices of two asset decrease	50	50	100	$\frac{1}{4}$

① CALCULATE E(CV)

$$\begin{aligned} E(CV)_{\text{spreading}} &= \frac{1}{4}(120) + \frac{1}{4}(110) + \frac{1}{4}(110) + \frac{1}{4}(100) \\ &= \frac{1}{4}(440) = 110 \end{aligned}$$

② CALCULATE STANDARD DEVIATION

$$\begin{aligned} SD &= \sqrt{\frac{1}{4}(120-110)^2 + \frac{1}{4}(110-110)^2 + \frac{1}{4}(110-110)^2 + \frac{1}{4}(100-110)^2} \\ &= \sqrt{\frac{1}{4} \cdot 100} = 5 \end{aligned}$$