

Exercise 4

Keynesian Cross and Fiscal Policy

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1. Answer the following questions.

1.1 Suppose **Govt Multiplier is 5** and $\Delta G = 5$. Find ΔY .

$$\begin{aligned} \text{govt multiplier} &= \frac{\Delta Y^*}{\Delta G} = 5 \\ \frac{\Delta Y^*}{5} &= 5 \quad \therefore \Delta Y^* = 25 \times \end{aligned}$$

1.2 Suppose **Tax Multiplier is -3** and $\Delta Y = -9$. Find ΔT .

$$\begin{aligned} \text{tax multiplier} &= \frac{\Delta Y^*}{\Delta T} = -3 \\ \frac{-9}{\Delta T} &= -3 \quad \therefore \Delta T = 3 \times \end{aligned}$$

1.3 Suppose $\Delta Y = 10$ and $\Delta I = 2$. Find **Investment Multiplier**.

$$\text{investment multiplier} = \frac{\Delta Y^*}{\Delta I} = \frac{10}{2} = 5 \times$$

2. From $Y = C + I + G$ where $C = C_0 + C_1(Y - T)$, find

2.1 Equilibrium Output Y^*

2.2 $\Delta Y / \Delta I$

2.3 $\Delta Y / \Delta G$

2.4 $\Delta Y / \Delta T$

2.5 Balanced-Budget Multiplier (BBM)

2.6 Explain what the BBM is.

2.1) $Y = AE$

$$Y = AE = C + I + G$$

$$Y = C_0 + C_1(Y - T) + I + G$$

$$Y = C_0 + C_1 Y - C_1 T + I + G$$

$$Y - C_1 Y = C_0 - C_1 T + I + G$$

$$Y(1 - C_1) = C_0 - C_1 T + I + G$$

$$Y^* = \frac{1}{(1 - C_1)} (C_0 - C_1 T + I + G)$$

2.2) $\frac{\Delta Y^*}{\Delta I} = \frac{1}{1 - \text{slope } AE} = \frac{1}{1 - C_1}$

2.3) $\frac{\Delta Y^*}{\Delta G} = \frac{1}{1 - \text{slope } AE} = \frac{1}{1 - C_1}$

2.4) $\frac{\Delta Y^*}{\Delta T} = \frac{-\text{mpc}}{1 - \text{slope } AE} = \frac{-C_1}{1 - C_1}$

2.5) $\frac{\Delta Y^*}{\Delta G} + \frac{\Delta Y^*}{\Delta T} = \frac{1 - \text{mpc}}{1 - \text{mpc}}$

2.6) BBM is a change in output when G and T increase by 1 unit

3. Assume a **closed economy with government**. The country has the following components of aggregate expenditure.

$$C = 300 + 0.75(Y_d)$$

$$I = 50$$

$$G = 50$$

$$T = 50 \text{ (lump-sum tax)}$$

- 3.1 Use the $Y = AE$ (standard) approach to find the equilibrium output.

$$Y = AE$$

$$Y = C + I + G$$

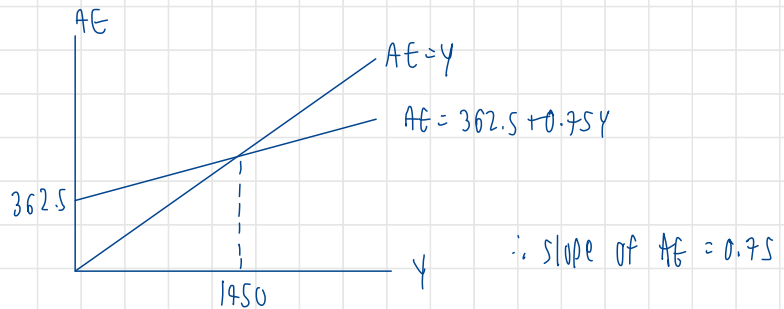
$$Y = 300 + 0.75(Y - 50) + 50 + 50$$

$$Y = 362.5 + 0.75Y$$

$$\frac{1}{4}Y = 362.5$$

$$Y^* = 1450$$

- 3.2 Draw the Keynesian Cross, and find the intercept on the vertical axis and the slope of the AE schedule.



- 3.3 Use the **Leakage = Injection** (or saving/investment) approach to find the equilibrium level of output. Y^*
(Hint: the equilibrium condition is $S + T = I + G$, with $Y_d = Y - T = C + S$)

$$\text{leakage} = \text{injection}$$

$$S + T = I + G$$

$$(Y - C) + T = I + G$$

$$Y - 300 - 0.75(Y - 50) = 50 + 50$$

$$Y - 300 - 0.75Y + 37.5 = 100$$

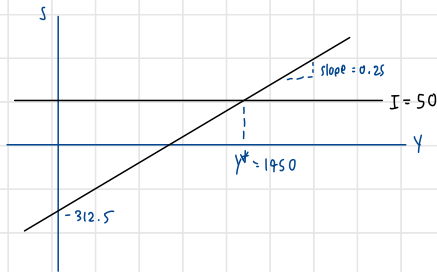
$$Y = 362.5 + 0.75Y$$

$$\frac{1}{4}Y = 362.5$$

$$Y^* = 1450$$

3.4 Draw the saving/investment curve to show the equilibrium.

$$S = Y - C$$



$$\text{intercept} \Rightarrow Y_d = C + I$$

$$Y - S = 300 + 0.75(Y - S) + 5$$

$$Y - S = 262.5 + 0.75Y + 5$$

$$S = -312.5 + 0.25Y$$

3.5 Suppose that the government decides to build more roads, raising government spending by 50 units, but this project is to be financed by the increase in net taxes of 50 units. Use the $Y = AE$ (standard) approach to find the new equilibrium output.

$G \uparrow$ by 50

$T \uparrow$ by 50

$$Y = AE$$

$$Y = C + I + G$$

$$Y = 300 + 0.75(Y - 100) + 50 + 100$$

$$Y = 450 + 0.75Y - 75$$

$$Y = 375 + 0.75Y$$

$$0.25Y = 375$$

$$Y^* = 1500$$

When $G \uparrow$ 50

$$Y = 300 + 0.75(Y - 50) + 50 + 100$$

$$0.25Y = 912.5$$

$$Y = 1650$$

When $T \uparrow$ 50

$$Y = 300 + 0.75Y - 75 + 100$$

$$0.25Y = 325$$

$$Y = 1300$$

3.6 Use the **Balanced-Budget Multiplier (BBM)** derived from Question 2.5 to find the new equilibrium output.

$$\frac{200}{50} + \frac{-150}{50} = 1$$

$$\frac{\Delta Y^*}{\Delta G} + \frac{\Delta Y^*}{\Delta T} = \frac{200}{-150} = 1$$

G and T increase by 1, Y^* will increase by 1

G and T increase by 50, Y^* will increase by 50

$$\therefore 1450 + 50 = 1500$$

$$\text{new } Y^* = 1500$$

4. From $Y = C + I + G + (X - M)$
where $C = C_0 + C_1(Y - T)$ and $M = M_0 + M_1(Y)$, find

4.1 Equilibrium Output Y^*

4.2 $\Delta Y / \Delta I$

4.3 $\Delta Y / \Delta G$

4.4 $\Delta Y / \Delta T$

4.5 Balanced-Budget Multiplier (BBM)

$$\begin{aligned} 4.1) \quad Y &= C_0 + C_1 Y - C_1 T + I + G + X - M_0 - M_1 Y \\ Y - C_1 Y + M_1 Y &= C_0 - C_1 T + I + G + X - M_0 \\ Y(1 - C_1 + M_1) &= C_0 - C_1 T + I + G + X - M_0 \\ Y^* &= \frac{1}{1 - C_1 + M_1} (C_0 - C_1 T + I + G + X - M_0) \end{aligned}$$

$$\begin{aligned} 4.2) \quad \frac{\Delta Y}{\Delta I} &= \frac{1}{1 - \text{slope}} = \frac{1}{1 - (C_1 - M_1)} \\ &= \frac{1}{1 - C_1 + M_1} \end{aligned}$$

$$4.3) \quad \frac{\Delta Y}{\Delta G} = \frac{1}{1 - \text{slope}} = \frac{1}{1 - C_1 + M_1}$$

$$4.4) \quad \frac{\Delta Y}{\Delta T} = \frac{-C_1}{1 - C_1 + M_1}$$

$$4.5) \quad \frac{\Delta Y}{\Delta G} + \frac{\Delta Y}{\Delta T} = \frac{1 - C_1}{1 - C_1 + M_1}$$

5. Assume an open economy with government. The country has the following components of aggregate expenditure.

$$C = 200 + 0.7(Y_d) \quad \text{MPC}$$

$$I = 75$$

$$G =$$

$$75$$

$$T = 50$$

$$X = 50$$

$$M = 50 + 0.1Y \quad \text{MPM}$$

- 5.1 Use the $Y = AE$ approach to find the equilibrium. Is $Y = 300$ an equilibrium?

If it is not, explain the adjustment process towards equilibrium.

$$\begin{aligned} Y &= AE \\ &= C + I + G + (X - M) \\ &= 200 + 0.7(Y - 50) + 75 + 75 + 50 - 50 - 0.1Y \\ Y &= 200 + 0.7Y - 35 + 75 + 75 - 0.1Y \\ Y &= 315 + 0.6Y \\ 0.4Y &= 315 \\ Y^* &= 787.5 \end{aligned}$$

$\therefore$ if $y = 300$, there are a shortage therefore, we need to adjust towards equilibrium which equal to 787.5 by increase in production and resale inventories

$$MPC = 0.7 / MPM = 0.1$$

5.2 Based on what you have derived in Question 4, calculate the investment, government spending, tax, and balanced-budget multipliers.

$$\text{Investment multiplier ; } \frac{\Delta Y^*}{\Delta I} = \frac{1}{1 - \text{slope}} = \frac{1}{1 - 0.6} = \frac{1}{0.4} = 2.5$$

$$\text{government spending multiplier ; } \frac{\Delta Y^*}{\Delta G} = \frac{1}{1 - 0.6} = \frac{1}{0.4} = 2.5$$

$$\text{tax multiplier ; } \frac{\Delta Y^*}{\Delta T} = \frac{-C_1}{1 - 0.6} = \frac{-0.7}{0.4} = -1.75$$

$$\text{BBM ; } \frac{\Delta Y^*}{\Delta T} + \frac{\Delta Y^*}{\Delta G} = \frac{1 - C_1}{1 - C_1 + M_1} = \frac{1 - 0.7}{0.4} = \frac{0.3}{0.4} = 0.75$$

5.3 Interpret the value of each of the multipliers.

investment multiplier - when I increases by 1, Y^* increases by 2.5

government spending multiplier - when G increases by 1, Y^* increases by 2.5

tax multiplier - when T increases by 1, Y^* decrease by 1.75

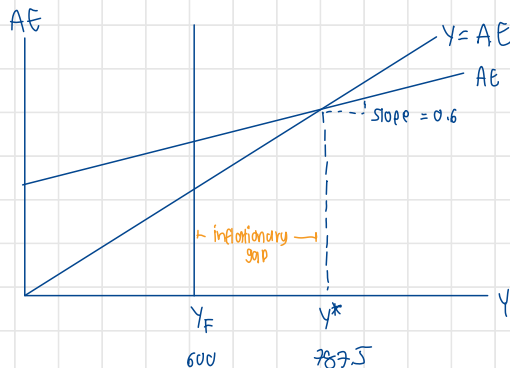
balance-budget multiplier - when τ and α increases by 1, Y^* increases by 0.75

Suppose that the full-employment output (Y_F) is 600;

5.4 What type of output gap is the economy currently experiencing?

inflationary gap

5.5 Draw the Keynesian Cross. Identify its slope and intercept. Also, illustrate the output gap.



$$\text{output gap is } 187.5 = \Delta Y^* = 187.5$$

Now, government wants to correct the output gap by moving the economy to the full-employment level, and is considering different policies.

(Hint: use the multipliers from Question 5.2 to answer the following questions)

5.6 If the government wants to adjust **only its spending (G)**, how much G should be changed?

$$\begin{aligned}
 Y &= 2.5 & G &= 1 \\
 Y^* \rightarrow Y_F &= -187.5 & \frac{187.5}{2.5} &= -75
 \end{aligned}
 \quad \left. \vphantom{\begin{aligned} Y &= 2.5 \\ Y^* \rightarrow Y_F &= -187.5 \end{aligned}} \right\} \begin{aligned} \frac{\Delta Y^*}{\Delta G} &= 2.5 \\ \Delta G &= \frac{-187.5}{2.5} = -75 \end{aligned}$$

$$\Delta G = -75$$

5.7 If the government wants to adjust **only its net taxes (T)**, how much T should be changed?

$$\begin{aligned}
 \Delta Y^* &= -187.5 & \frac{-187.5}{\Delta T} &= -1.75 \Rightarrow \Delta T = 107.14 \\
 \frac{\Delta Y^*}{\Delta T} &= -1.75 & \Delta T &= 107.14
 \end{aligned}$$

5.8 If the government wants to boost **only investment (I)**, how much I should be changed?

$$\begin{aligned}
 \frac{\Delta Y^*}{\Delta I} &= 2.5 \\
 \Delta I &= \frac{-187.5}{2.5} & \therefore \Delta I &= -75
 \end{aligned}$$

5.9 If the government wants to implement a balanced-budget policy, what should the government do with G and T?

$$\begin{aligned}
 0.75 & \quad 1 \\
 -187.5 & \quad \frac{-187.5}{0.75} = -250
 \end{aligned}$$

$\therefore$ G and T decrease by 250

7. Let $S = -200 + 0.5Y$ and $I = 50$, be the saving function and investment.

real wage = injection
 $S = I$

7.1 Use the saving/investment approach to find the equilibrium output.

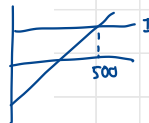
7.2 Find the equilibrium saving. (Hint: substitute Y^* into S)

Suppose people decide to save more, increasing autonomous saving by 100.

7.3 Use the saving/investment approach to find the new equilibrium output.

7.4 Find the new equilibrium saving. (Hint: substitute new Y^* into S)

7.5 Comment on your result.



7.1) $S = I$
 $-200 + 0.5Y = 50$
 $0.5Y = 250$
 $Y^* = 500$

7.2) $S = -200 + 0.5(500)$
 $S^* = 50$

7.3) $S = -100 + 0.5Y$
 find new equilibrium ; $S = I$
 $-100 + 0.5Y = 50$
 $0.5Y = 150$
 $Y^* = 300$

7.4) new equilibrium saving (S^*)
 $S = -100 + 0.5Y$
 $= -100 + 0.5(300)$
 $S^* = 50$

7.4) as paradox of thrift theory, when people save more it means they will spend less and income in economy will decrease which means people will receive lower income. therefore, less goods are produced (from 500 to 300)

