

### Assignment 3

1.

```
. probit y x1 x2 x3 x4
```

```
Iteration 0: log likelihood = -248.43455
Iteration 1: log likelihood = -150.03919
Iteration 2: log likelihood = -147.48531
Iteration 3: log likelihood = -147.46882
Iteration 4: log likelihood = -147.46881
```

```
Probit regression                               Number of obs   =       400
                                                LR chi2(4)      =      201.93
                                                Prob > chi2     =      0.0000
Log likelihood = -147.46881                    Pseudo R2      =      0.4064
```

	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
x1	.3590739	.0371539	9.66	0.000	.2862536	.4318941
x2	-.8525746	.144481	-5.90	0.000	-1.135752	-.569397
x3	-.5735764	.2202882	-2.60	0.009	-1.005333	-.1418195
x4	-1.248569	.226762	-5.51	0.000	-1.693014	-.8041238
_cons	1.45664	.2037279	7.15	0.000	1.057341	1.85594

```
. fitstat
```

Measures of Fit for **probit** of **y**

```
Log-Lik Intercept Only:   -248.435   Log-Lik Full Model:     -147.469
D(395):                   294.938   LR(4):                  201.931
                           Prob > LR:         0.000
McFadden's R2:           0.406   McFadden's Adj R2:     0.386
Maximum Likelihood R2:   0.396   Cragg & Uhler's R2:    0.557
McKelvey and Zavoina's R2: 0.640   Efron's R2:            0.446
Variance of y*:          2.775   Variance of error:     1.000
Count R2:                 0.818   Adj Count R2:          0.416
AIC:                      0.762   AIC*n:                 304.938
BIC:                      -2071.691  BIC':                  -177.966
```

**For Probit model**, the overall test is indicated from the value of LR Chi-square Test. From the table, the value of LR Chi-square Test (LR chi2(4)) equals to 201.93. This is the Likelihood Ratio (LR) Chi-Square test that at least one of the predictors' regression coefficient is not equal to zero in the model. Moreover, the model is statistically significant because the p-value is less than 0.000. When we consider individual test, we look at the value of Z-test. And from the table, P-value of all independent variables are lower than 0.05. It means that all independent variables are statistically significant or can explain the dependent variables. For Pseudo R-square of this Probit model, the estimated result is 0.4064. However, pseudo R-squared only has meaning when compared to pseudo R-squared of other model with the same type, the same data, the same outcome. It indicates how well does the estimated result contribute to the likelihood of the model. The model that has higher pseudo R-squared is the better one. Lastly, Counted R-square of the Probit model is 0.818 or 81.8%. This means that the model can correctly predict the outcome by 81.8% or actual result is the same as predicted result by 81.8%.

```
. logit y x1 x2 x3 x4
```

```
Iteration 0: log likelihood = -248.43455
Iteration 1: log likelihood = -154.06753
Iteration 2: log likelihood = -148.00091
Iteration 3: log likelihood = -147.90887
Iteration 4: log likelihood = -147.90869
Iteration 5: log likelihood = -147.90869
```

```
Logistic regression                Number of obs   =      400
                                   LR chi2(4)       =      201.05
                                   Prob > chi2        =      0.0000
Log likelihood = -147.90869        Pseudo R2       =      0.4046
```

y	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
x1	.6299401	.0708979	8.89	0.000	.4909828	.7688974
x2	-1.488248	.2597744	-5.73	0.000	-1.997396	-.9790992
x3	-.9562902	.3882611	-2.46	0.014	-1.717268	-.1953124
x4	-2.155321	.4055058	-5.32	0.000	-2.950097	-1.360544
_cons	2.5165	.3714373	6.78	0.000	1.788496	3.244503

. fitstat

Measures of Fit for **logit** of **y**

Log-Lik Intercept Only:	-248.435	Log-Lik Full Model:	-147.909
D(395):	295.817	LR(4):	201.052
		Prob > LR:	0.000
McFadden's R2:	0.405	McFadden's Adj R2:	0.385
Maximum Likelihood R2:	0.395	Cragg & Uhler's R2:	0.555
McKelvey and Zavoina's R2:	0.622	Efron's R2:	0.445
Variance of y*:	8.707	Variance of error:	3.290
Count R2:	0.818	Adj Count R2:	0.416
AIC:	0.765	AIC*n:	305.817
BIC:	-2070.811	BIC':	-177.086

**For Logit model**, the overall test is indicated from the value of LR Chi-square Test. From the table, the value of LR Chi-square Test (LR chi2(4)) equals to 201.05. This is the Likelihood Ratio (LR) Chi-Square test that at least one of the predictors' regression coefficient is not equal to zero in the model. Moreover, the model is statistically significant because the p-value is less than 0.000. When we consider individual test, we look at the value of Z-test. And from the table, P-value of all independent variables are lower than 0.05. It means that all independent variables are statistically significant or can explain the dependent variables. For Pseudo R-square of this Probit model, the estimated result is 0.4046. However, pseudo R-squared only has meaning when compared to pseudo R-squared of other model with the same type, the same data, the same outcome. It indicates how well does the estimated result contribute to the likelihood of the model. The model that has higher pseudo R-squared is the better one. Lastly, Counted R-square of the Probit model is 0.818 or 81.8%. This means that the model can correctly predict the outcome by 81.8% or actual result is the same as predicted result by 81.8%.

## 2.

To compare the goodness of fit of the two models, we consider Pseudo (McFadden) R2 of the two models. We can see from the tables that Pseudo R2 of Probit model is 0.4064, while Logit model's Pseudo R2 is only 0.4046. So, we can conclude that Probit model better fits the data than the Logit model.

3.

```
. probit y, nolog
```

```
Probit regression                Number of obs   =       400  
                                LR chi2(0)      =       0.00  
                                Prob > chi2       =       .  
Log likelihood = -248.43455      Pseudo R2      =     0.0000
```

y	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
_cons	.4887764	.0654634	7.47	0.000	.3604706	.6170822

**Overall LR-test** = 2 (log likelihood of unrestricted model – log likelihood of restricted model)  
= 2(-147.46881+248.43455)  
= 201.93

4.

. logit y x1 x2 x3 x4, nolog

```

Logistic regression          Number of obs   =       400
                             LR chi2(4)           =       201.05
                             Prob > chi2          =       0.0000
Log likelihood = -147.90869   Pseudo R2       =       0.4046
  
```

y	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
x1	.6299401	.0708979	8.89	0.000	.4909828	.7688974
x2	-1.488248	.2597744	-5.73	0.000	-1.997396	-.9790992
x3	-.9562902	.3882611	-2.46	0.014	-1.717268	-.1953124
x4	-2.155321	.4055058	-5.32	0.000	-2.950097	-1.360544
_cons	2.5165	.3714373	6.78	0.000	1.788496	3.244503

. mfx, predict(xb)

```

Marginal effects after logit
  y = Linear prediction (log odds) (predict, xb)
    = 1.32418
  
```

variable	dy/dx	Std. Err.	z	P> z	[ 95% C.I. ]		X
x1	.6299401	.0709	8.89	0.000	.490983	.768897	.454973
x2	-1.488248	.25977	-5.73	0.000	-1.9974	-.979099	.809344
x3	-.9562902	.38826	-2.46	0.014	-1.71727	-.195312	.556712
x4	-2.155321	.40551	-5.32	0.000	-2.9501	-1.36054	-.119684

$$\begin{aligned}
 \hat{l} &= 2.52 + 0.62(0.45) - 1.49(0.81) - 0.96(0.56) + 2.16(0.12) \\
 &= 1.32
 \end{aligned}$$

5.

. mfx

Marginal effects after logit

y = Pr(y) (predict)  
= .7898763

variable	dy/dx	Std. Err.	z	P> z	[ 95% C.I. ]	X
x1	.1045522	.01146	9.12	0.000	.082083 .127022	.454973
x2	-.247007	.04388	-5.63	0.000	-.333011 -.161003	.809344
x3	-.1587171	.06397	-2.48	0.013	-.2841 -.033334	.556712
x4	-.3577223	.06679	-5.36	0.000	-.488633 -.226812	-.119684

. mfx, at(median)

Marginal effects after logit

y = Pr(y) (predict)  
= .84127022

variable	dy/dx	Std. Err.	z	P> z	[ 95% C.I. ]	X
x1	.0841188	.00961	8.76	0.000	.065292 .102946	.655749
x2	-.1987326	.03349	-5.93	0.000	-.264373 -.133093	.692745
x3	-.1276979	.04944	-2.58	0.010	-.224597 -.030799	.488768
x4	-.28781	.05616	-5.12	0.000	-.397881 -.177739	-.109732

6.

. mfx, at(0.5 1 0.5 0)

Marginal effects after probit  
y = Pr(y) (predict)  
= .69034

variable	dy/dx	Std. Err.	z	P> z	[ 95% C.I. ]	X
x1	.1266183	.01307	9.69	0.000	.101001 .152235	.5
x2	-.3006389	.05452	-5.51	0.000	-.4075 -.193778	1
x3	-.2022572	.07644	-2.65	0.008	-.352085 -.05243	.5
x4	-.4402764	.08419	-5.23	0.000	-.605293 -.27526	0

7. Counted R2 = 81.75%

. estat clas

Logistic model for y

Classified	True		Total
	D	~D	
+	251	49	300
-	24	76	100
Total	275	125	400

Classified + if predicted Pr(D) >= .5  
True D defined as y != 0

Sensitivity	Pr( +  D)	91.27%
Specificity	Pr( - ~D)	60.80%
Positive predictive value	Pr( D  +)	83.67%
Negative predictive value	Pr(~D  -)	76.00%
False + rate for true ~D	Pr( + ~D)	39.20%
False - rate for true D	Pr( -  D)	8.73%
False + rate for classified +	Pr(~D  +)	16.33%
False - rate for classified -	Pr( D  -)	24.00%
Correctly classified		81.75%

8. Counted R2 = 79.50%

. estat clas, cut(0.7)

Logistic model for y

Classified	True		Total
	D	~D	
+	217	24	241
-	58	101	159
Total	275	125	400

Classified + if predicted  $\Pr(D) \geq .7$

True D defined as  $y \neq 0$

Sensitivity	$\Pr(+ D)$	78.91%
Specificity	$\Pr(- \sim D)$	80.80%
Positive predictive value	$\Pr(D +)$	90.04%
Negative predictive value	$\Pr(\sim D -)$	63.52%
False + rate for true ~D	$\Pr(+ \sim D)$	19.20%
False - rate for true D	$\Pr(- D)$	21.09%
False + rate for classified +	$\Pr(\sim D +)$	9.96%
False - rate for classified -	$\Pr(D -)$	36.48%
Correctly classified		79.50%