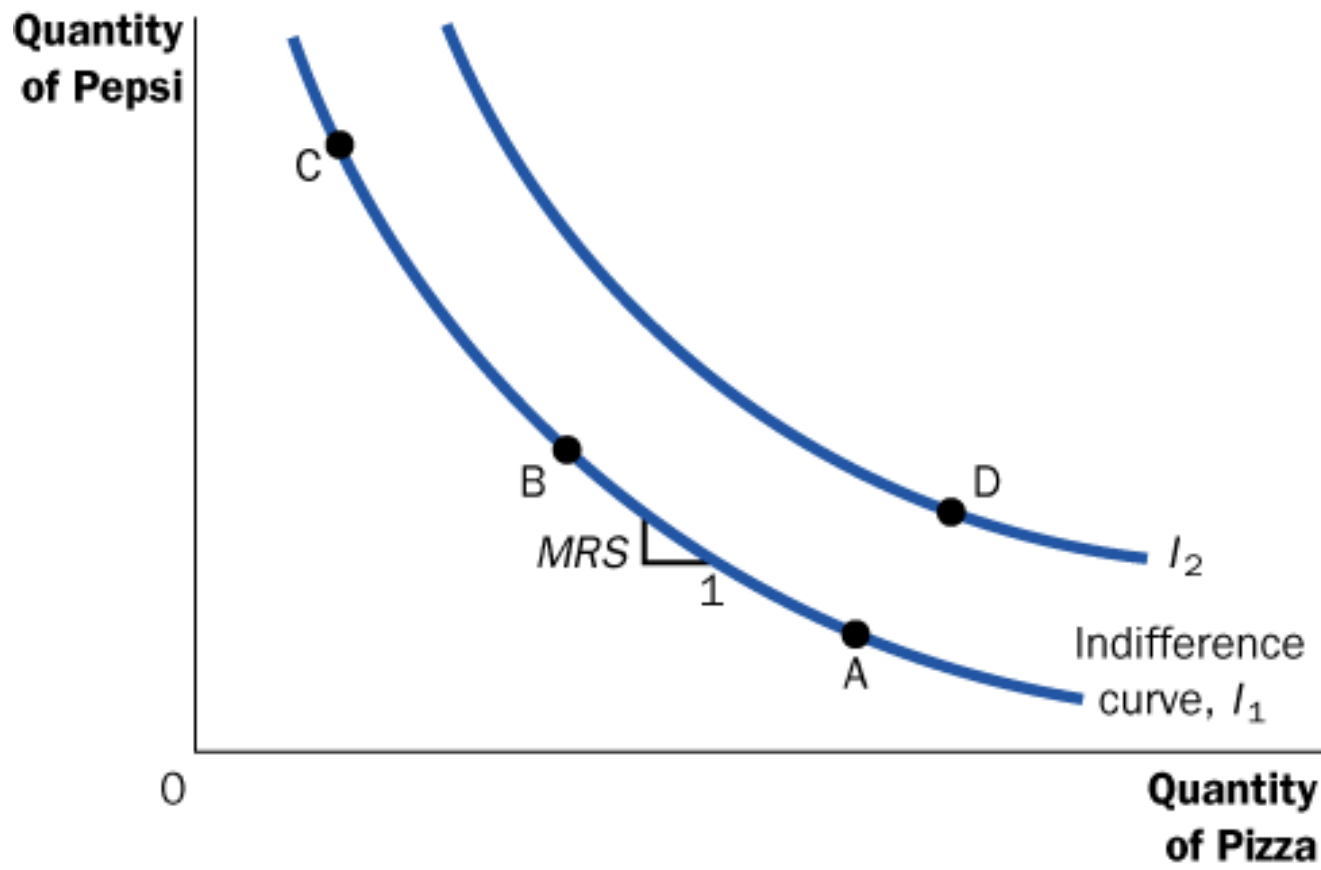


Recap (Consumer's Behavior)

- Before midterm, we discussed about two approaches in understanding consumer's preferences:
 - Cardinal approach – utility
 - Ordinal approach – indifference curve, MRS
- Next sub-topics:
 - Budget line (or budget constraint)
 - Consumer's equilibrium (or consumer's optimization)
 - Change in equilibrium when price changes
 - Demand curve derivation
 - Applications

Part III. Consumer's Equilibrium

- Recall: **Indifference curve** shows consumption bundles that give the consumer the same level of satisfaction.



Extra Notes on Indifference Curve (1)

- MRS is the slope of the indifference curve, and MRS is diminishing (in absolute value) as X increases.
- At any point on indifference curve, the slope is $\frac{\Delta Y}{\Delta X}$.
- As the consumer consumes more X and reduces consumption of Y, her utility changes by:

$$\Delta X > 0 \rightarrow \Delta U_x \approx MU_x \times \Delta X$$

$$\Delta Y < 0 \rightarrow \Delta U_y \approx MU_y \times \Delta Y$$

- But on the an indifference curve, the utility is the same:

$$\Delta U = \rightarrow \Delta U_x + \Delta U_y = 0$$

Extra Notes on Indifference Curve (2)

- So,

$$\Delta U_x = -\Delta U_y$$

$$MU_x \Delta X \approx -MU_y \Delta Y$$

$$\rightarrow \frac{\Delta Y}{\Delta X} \approx -\frac{MU_x}{MU_y}$$

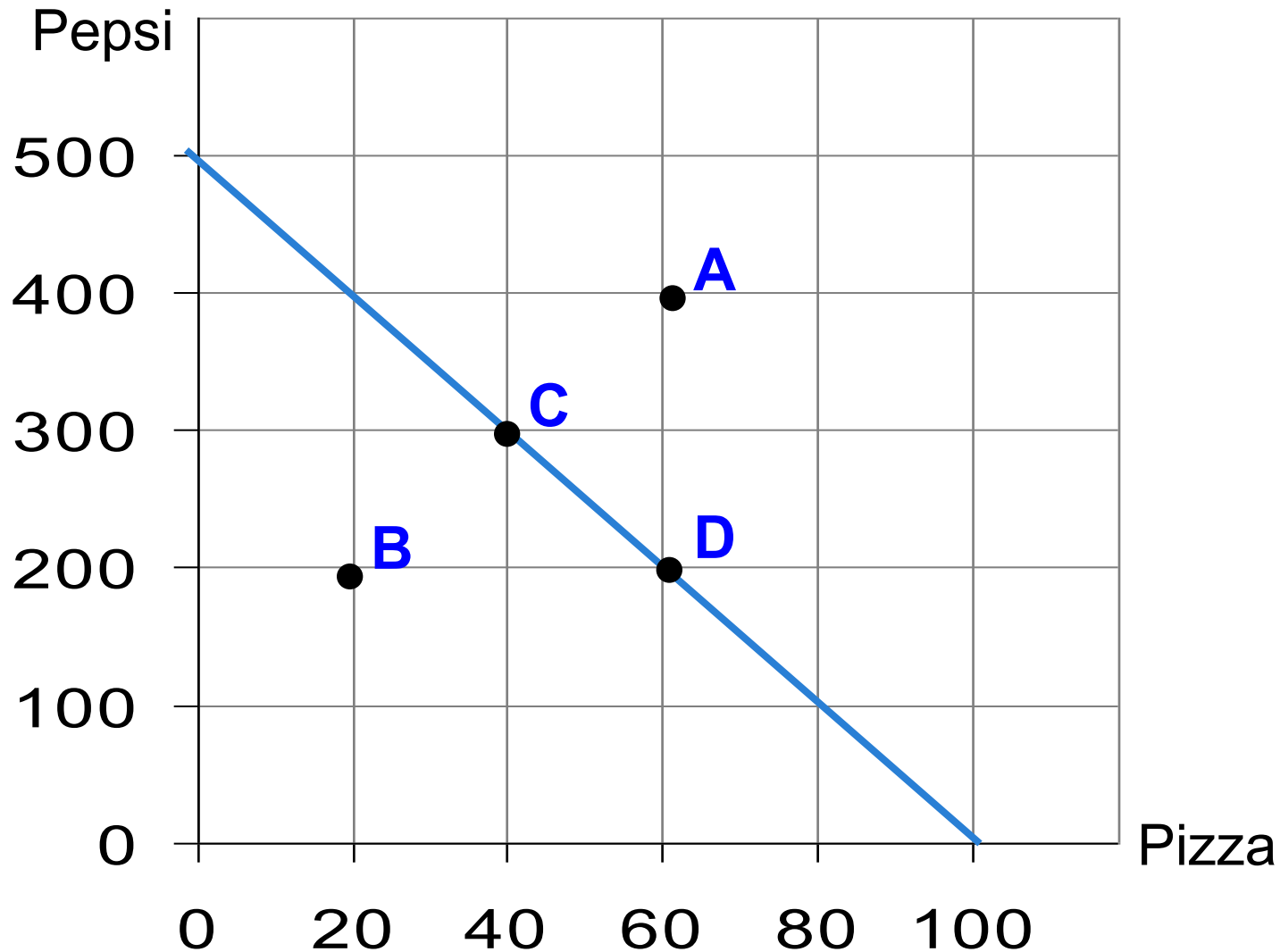
$$\rightarrow \frac{dY}{dX} = -\frac{MU_x}{MU_y} : \text{MRS}$$

Budget Constraint

- **Budget constraint (or budget line):** the limit on the consumption bundles that a consumer can afford.
 - It shows all combinations (bundles) of the two goods that the consumer can afford to buy.
- Consider the case of 2 goods: Pizza (X) and Pepsi (Y). Suppose $P_x = \$10$, $P_y = \$2$, and budget (B) = \$1000.
- The budget line can be written as:

$$P_x X + P_y Y = B$$

Graph: Budget Constraint



Slope of the Budget Constraint

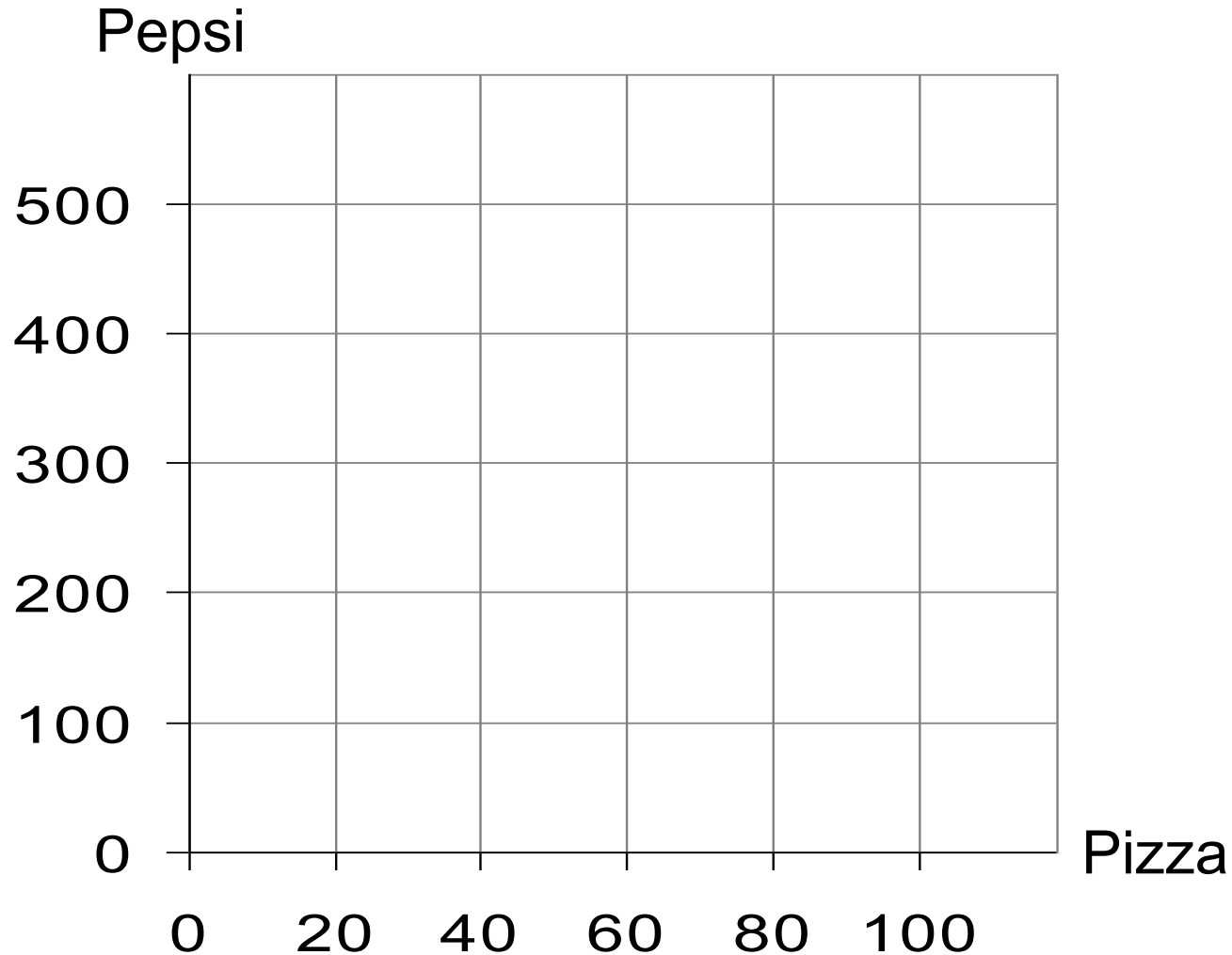
- The **slope of the budget constraint** equals:
 - the rate at which the consumer can trade Pepsi for pizza
 - the opportunity cost of pizza in terms of Pepsi
 - the relative price of pizza.

That is:

$$\textit{Slope of Budget line} = -\frac{P_x}{P_y}$$

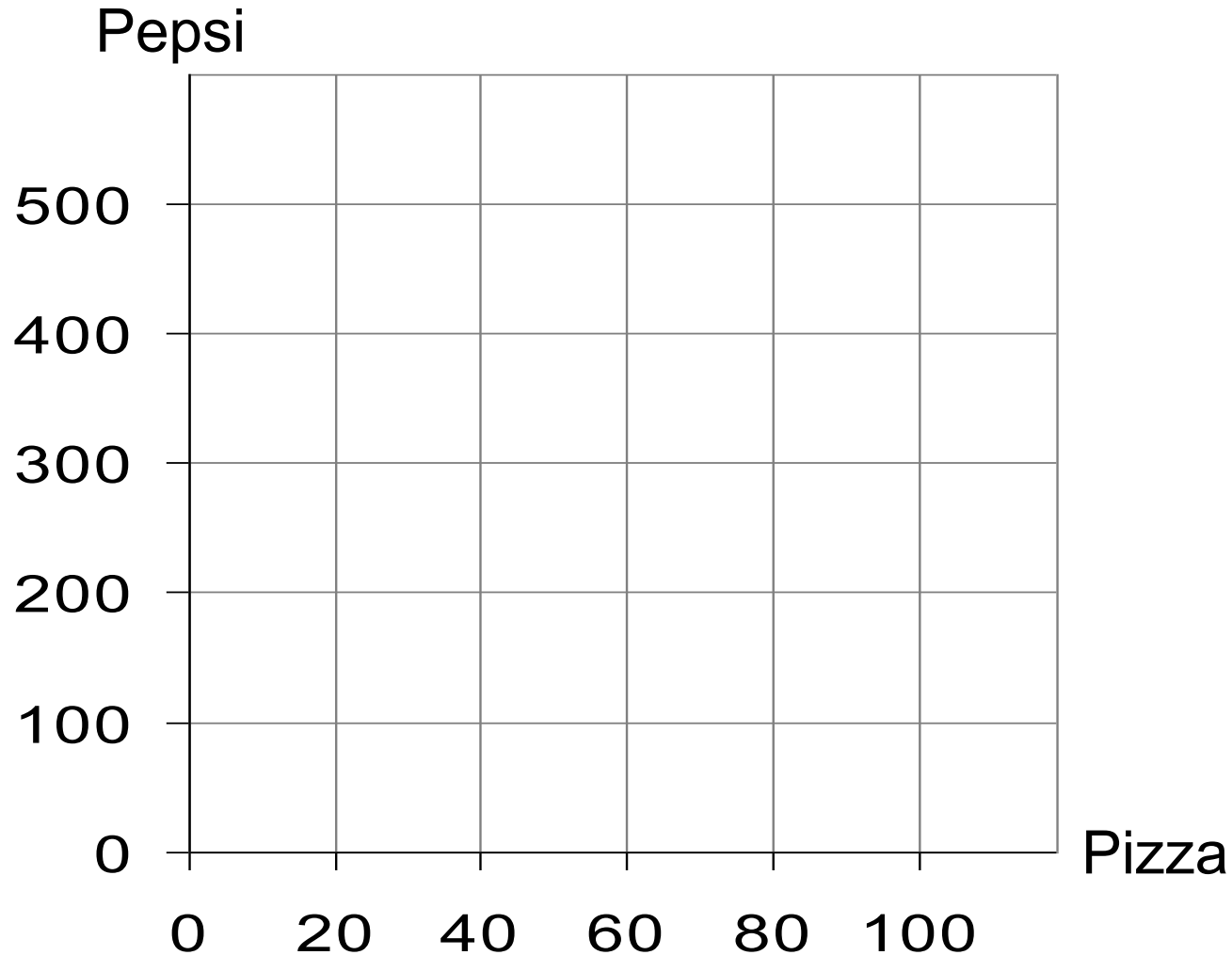
Change in Budget Constraint: Higher Income

- Suppose budget increases to \$1200.



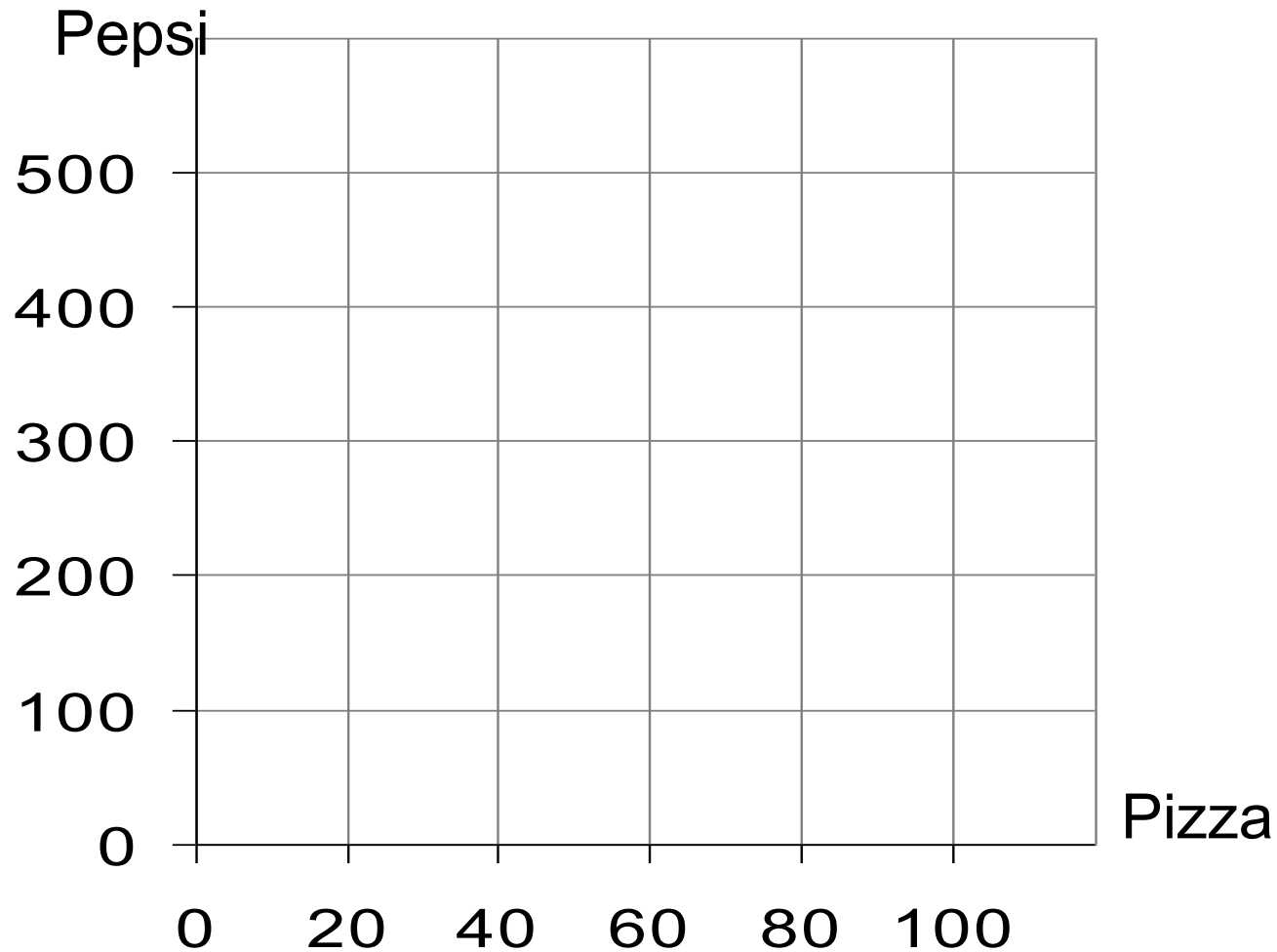
Change in Budget Constraint: P_x changes.

- Suppose P_x increases from \$10 to \$12.5.



Change in Budget Constraint: P_x & P_y change by the same proportion.

- Suppose $P'_x = \$12.5$ and $P'_y = \$2.5$.

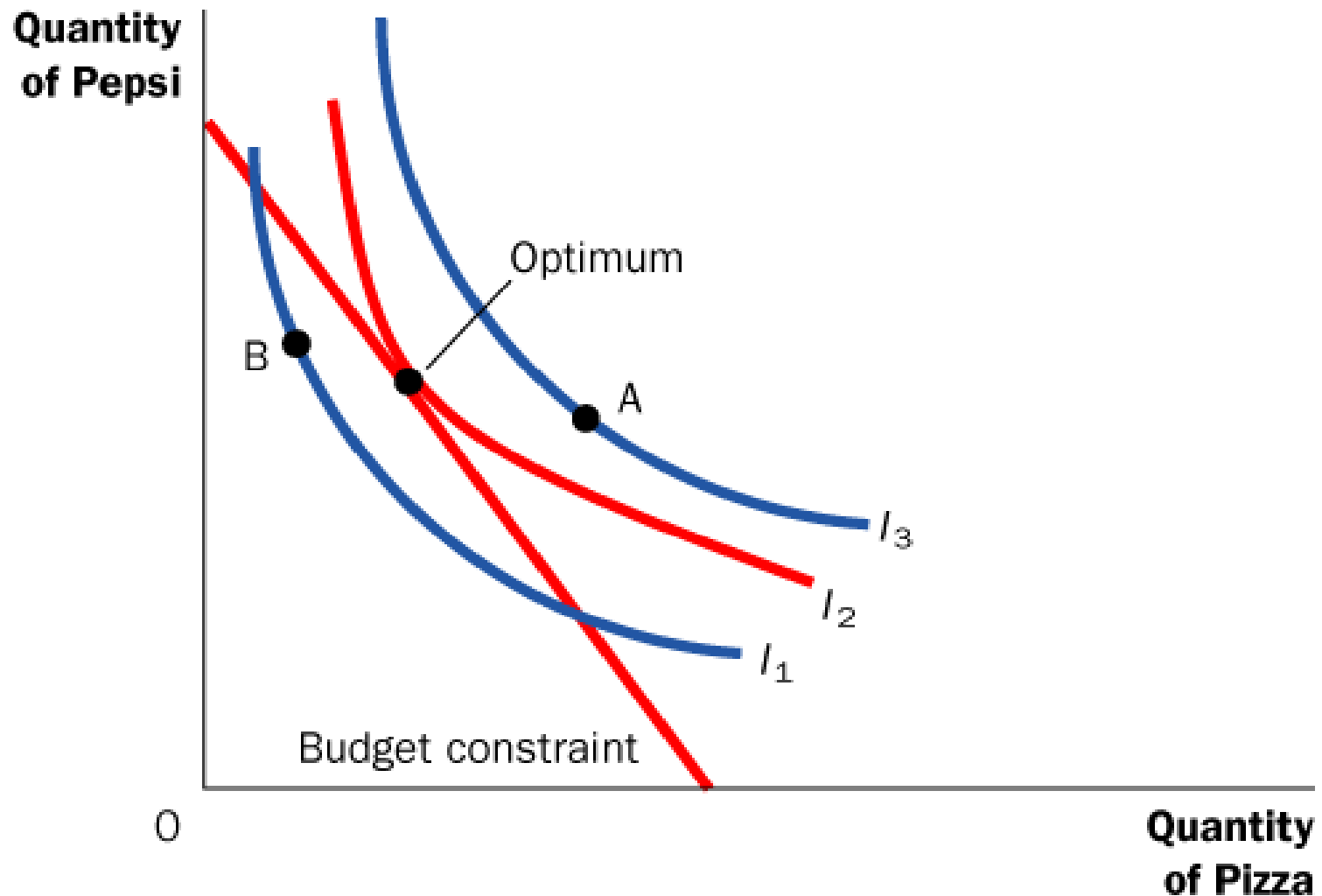


Consumer's Problem: Optimization

- Consumer's problem is to maximize his/her utility (i.e. satisfaction) under the budget constraint.
- The **optimal bundle** is at the point where the budget constraint touches the highest indifference curve.
 - i.e., the indifference curve and budget constraint have the same slope.
- Since the slope of IC is the MRS and the slope of the budget constraint is the relative price, the optimal bundle

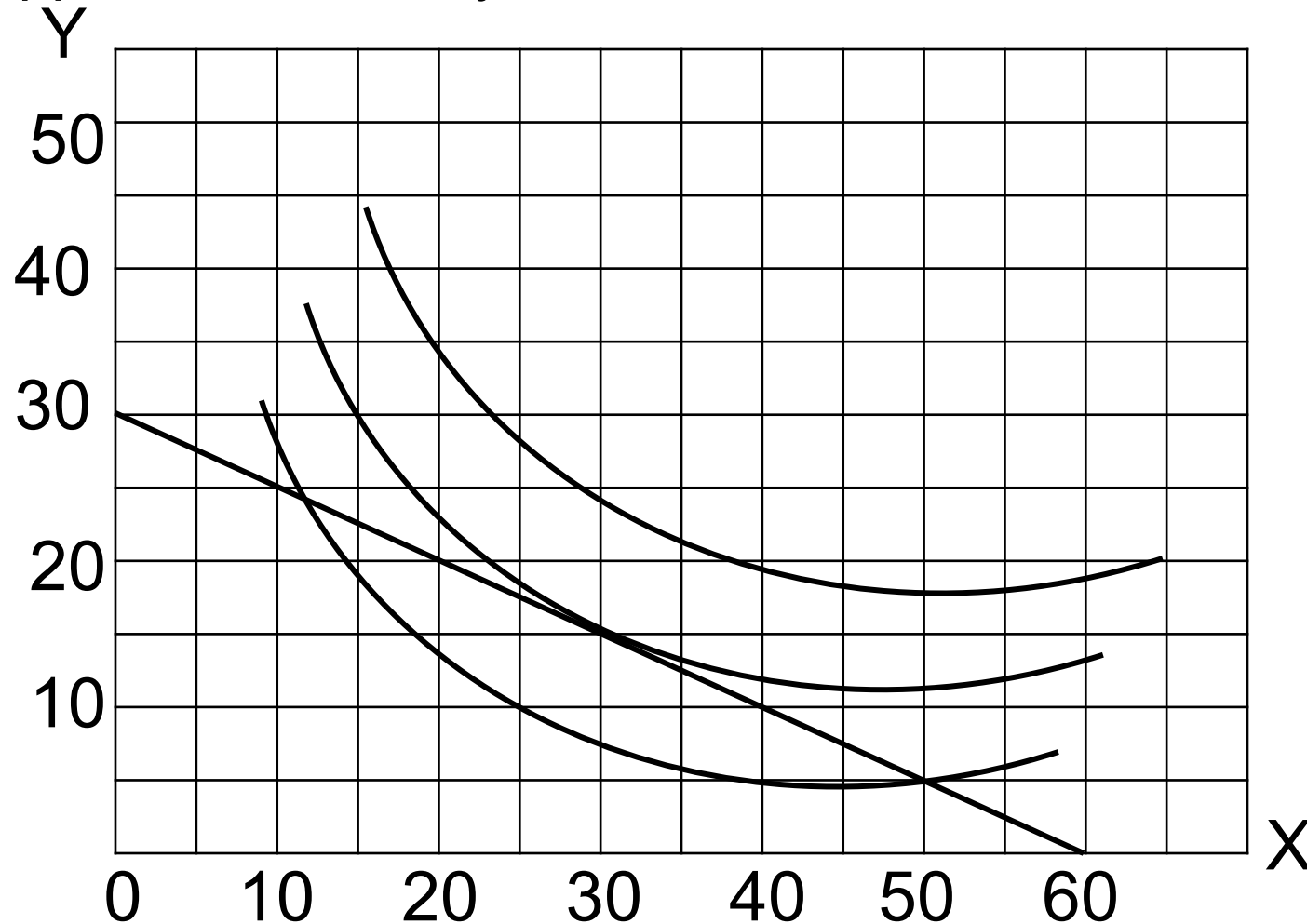
is where:
$$\frac{P_x}{P_y} = \frac{MU_x}{MU_y}$$

Graph: Consumer's Optimal Choice



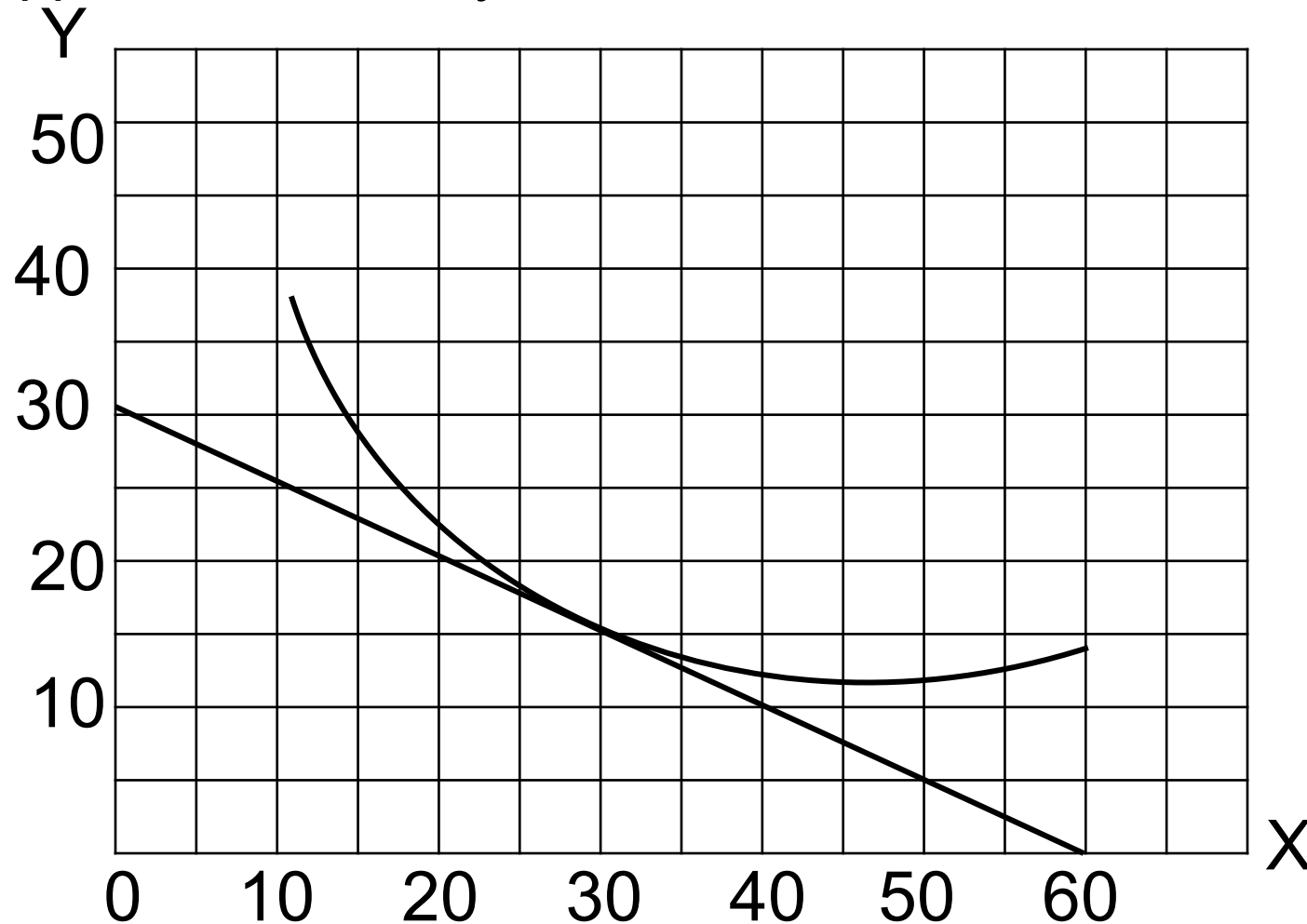
Example: Optimization

- Suppose $P_x = \$2$, $P_y = \$4$, and $B = 120$.



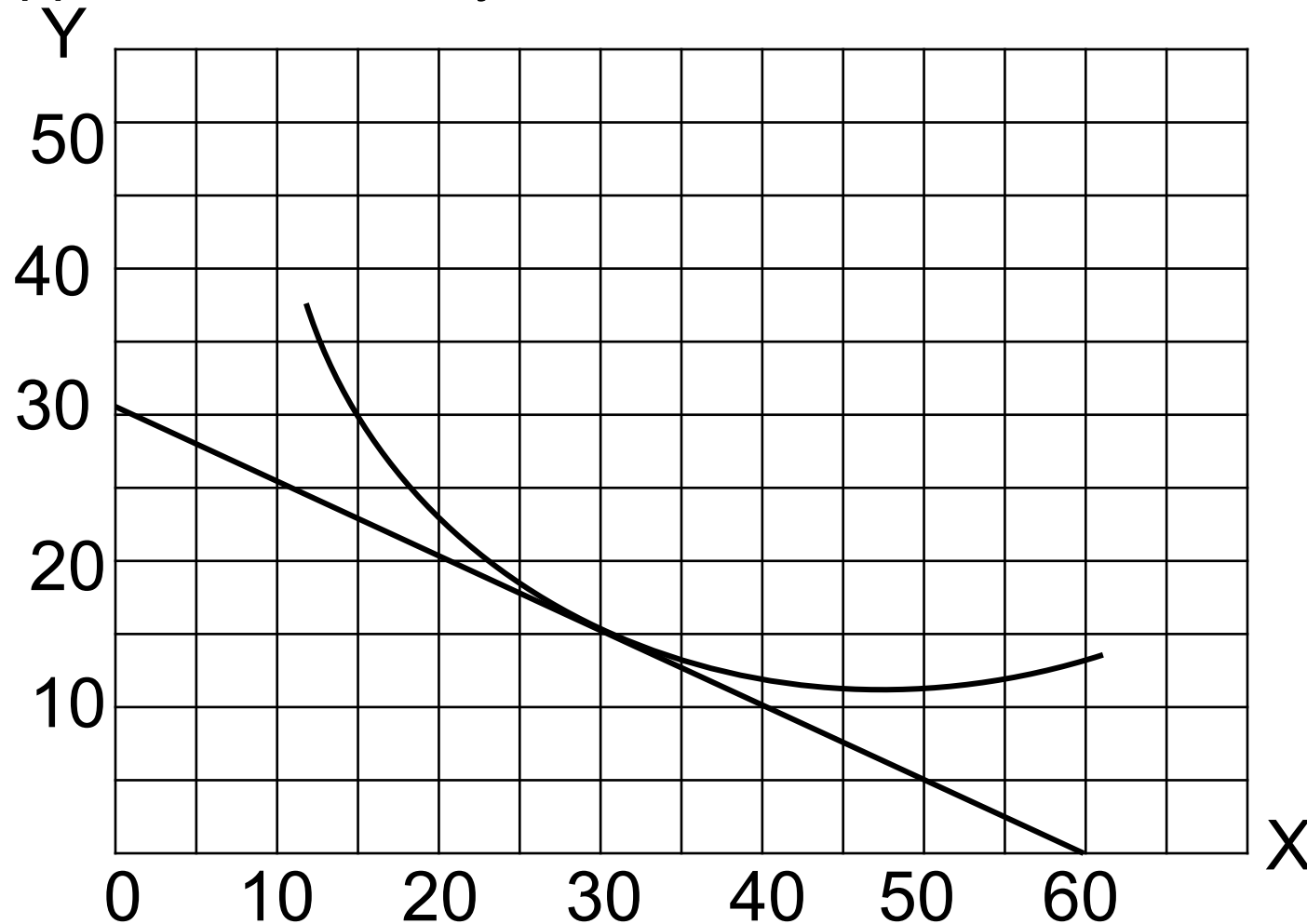
Example: Effect of Income Increase

- Suppose $P_x = \$2$, $P_y = \$4$, and $B = 150$.



Example: Effect of Income Reduction

- Suppose $P_x = \$2$, $P_y = \$4$, and $B = 90$.

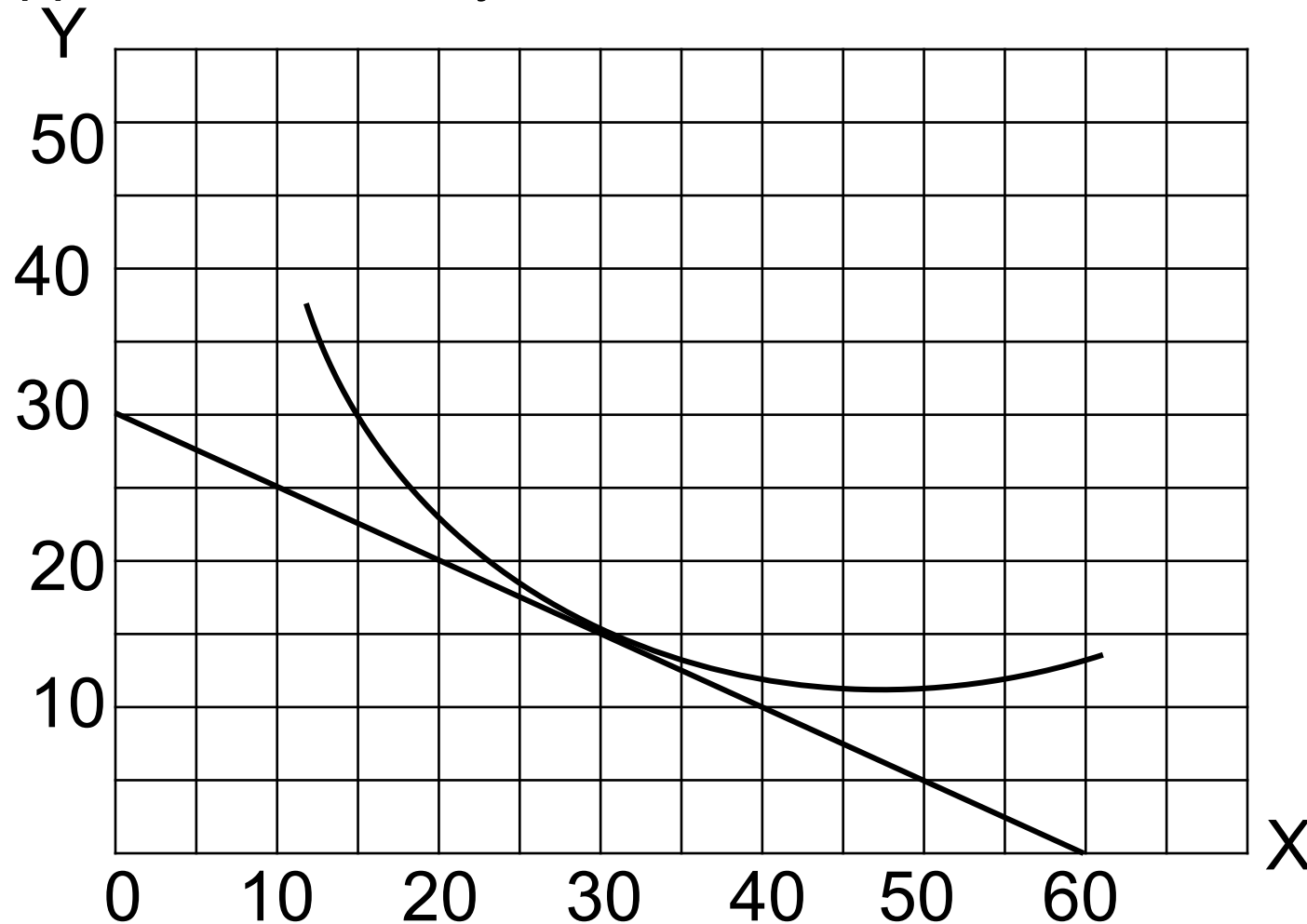


Income Consumption Curve (ICC)

- A change in income, *ceteris paribus*, will shift the consumer's budget constraint.
- For each level of income, there will be a utility maximizing points where IC is tangent to the relevant budget line.
- **Income Consumption Curve (ICC)** is the line that connects all the utility-maximizing points for different levels of income, given prices P_x and P_y constant.
- I.e. , ICC shows how the consumer's purchases react to a change in money income with relative prices being held constant.

Graph: ICC

- Suppose $P_x = \$2$, $P_y = \$4$, and $B = 90, 120, 150$.

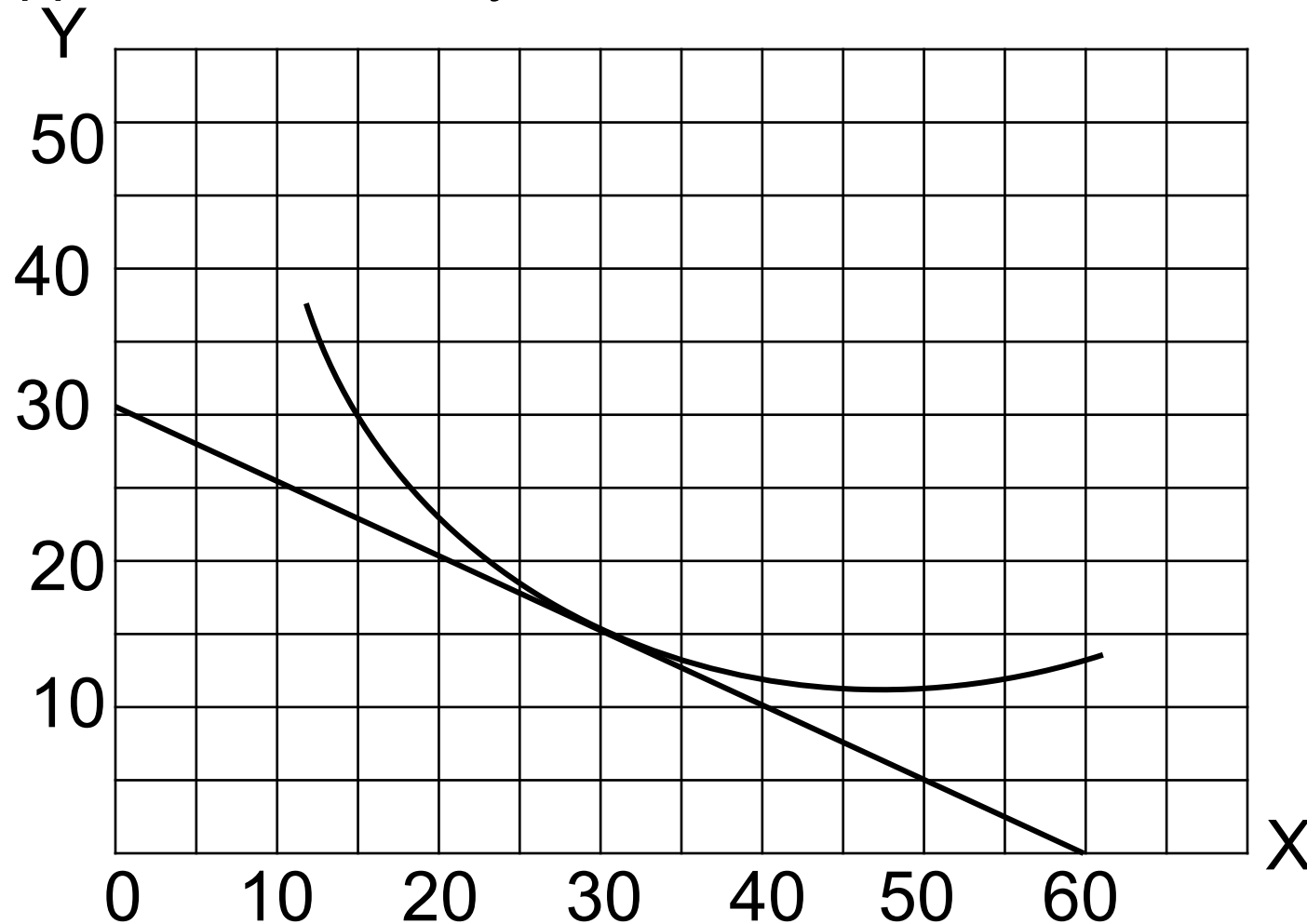


Exercise: Inferior good

- Suppose X is a normal good but Y is an inferior good.
- Use a diagram to show the effects of an increase in income on the consumer's optimal bundle of X and Y .

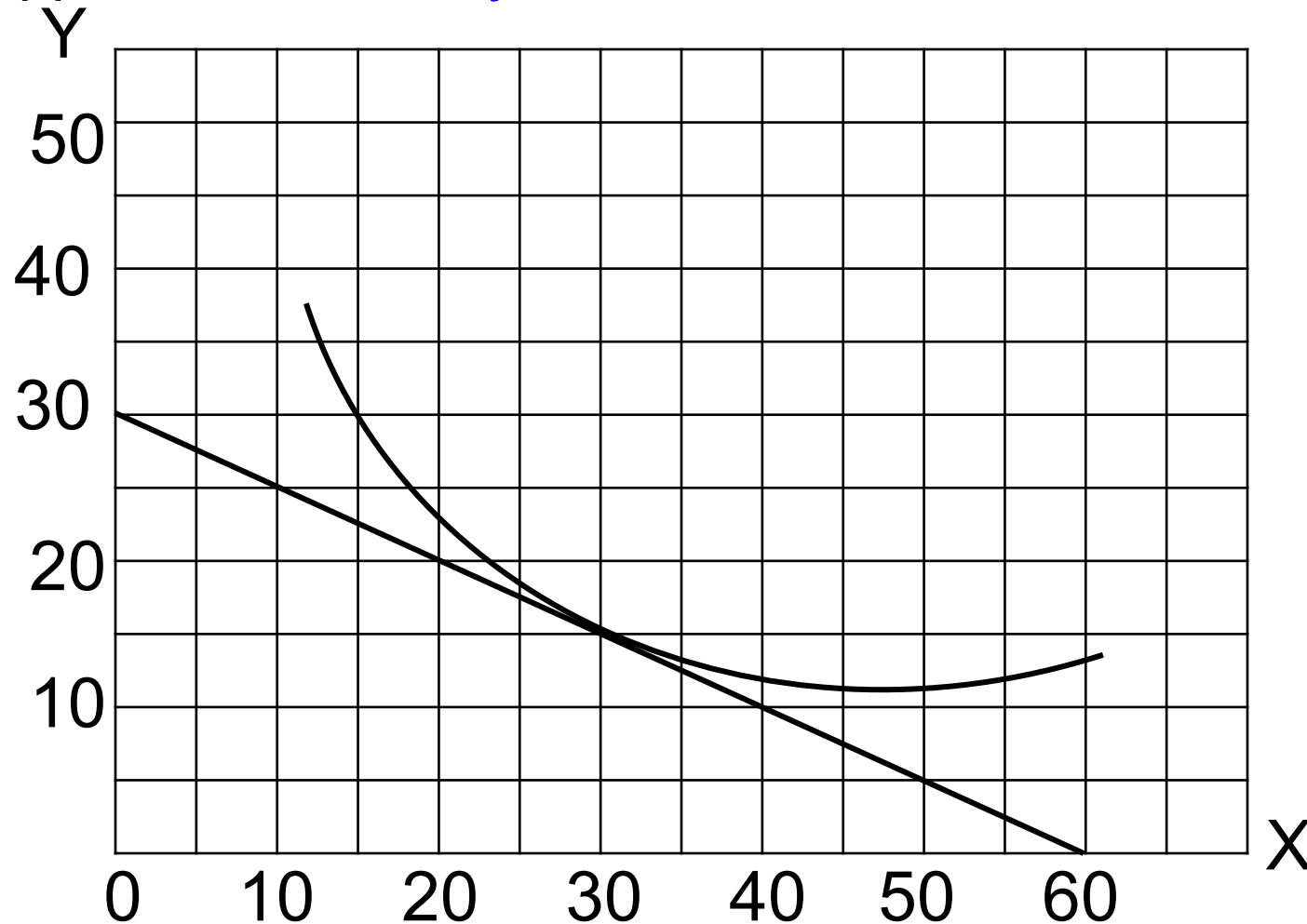
Example: Effect of Price Change (1)

- Suppose $P'_x = \$3$, $P_y = \$4$, and $B = 120$.



Example: Effect of Price Change (2)

- Suppose $P_x = \$2$, $P'_y = \$6$, and $B = 120$.

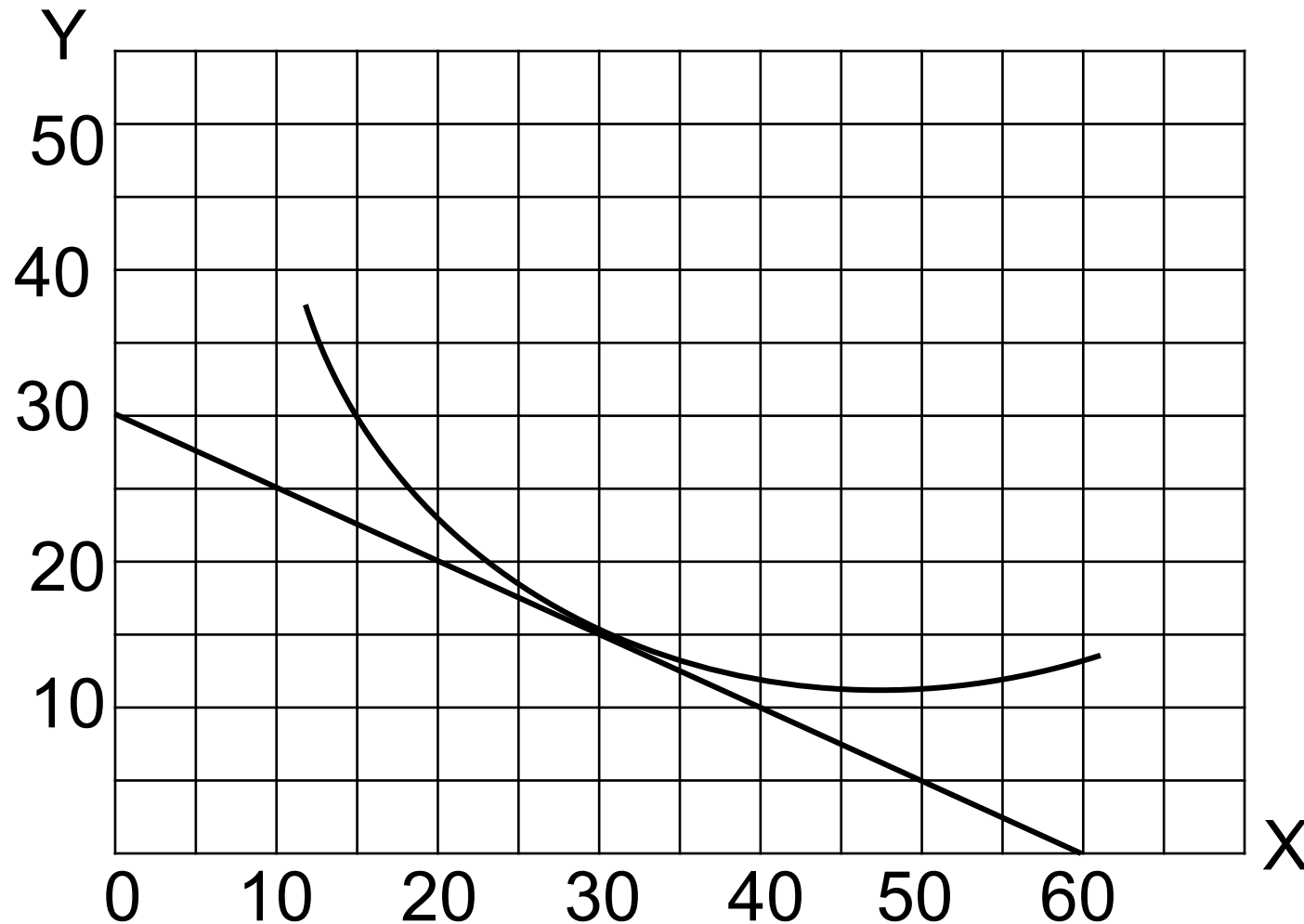


Price Consumption Curve

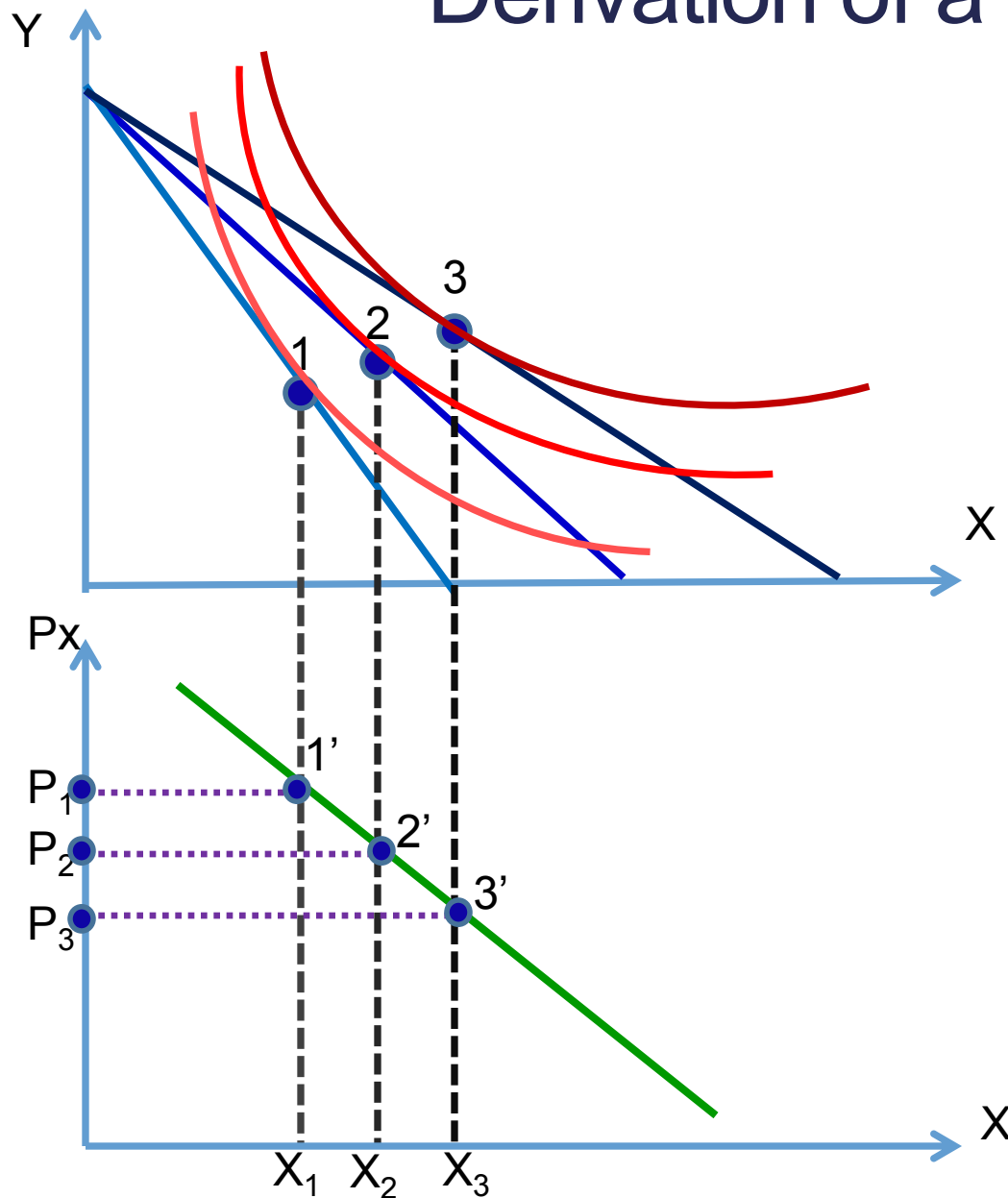
- A change in relative prices of two goods changes the slope of the budget constraint.
- Suppose P_x changes while P_y is constant. For each P_x , there is a different utility-maximizing consumption bundle.
- **Price Consumption Curve (PCC)** is the line that connects all the utility-maximizing points for different P_x 's, given income and P_y constant.
- I.e. , PCC shows how the consumer's purchases react to a change in one price with income and other prices being held constant.

Graph: PCC

- Suppose $P_x = \$2, \$3, \$4$, $P_y = \$4$, and $B = 120$.



Derivation of a Demand Curve



Income and Substitution Effects

- A fall in P_x has two effects:

Substitution effect

- Change in X due to change in relative price with *real income unchanged*
- A fall in P_x makes Y more expensive relative to X , causing consumer to buy more X and less Y

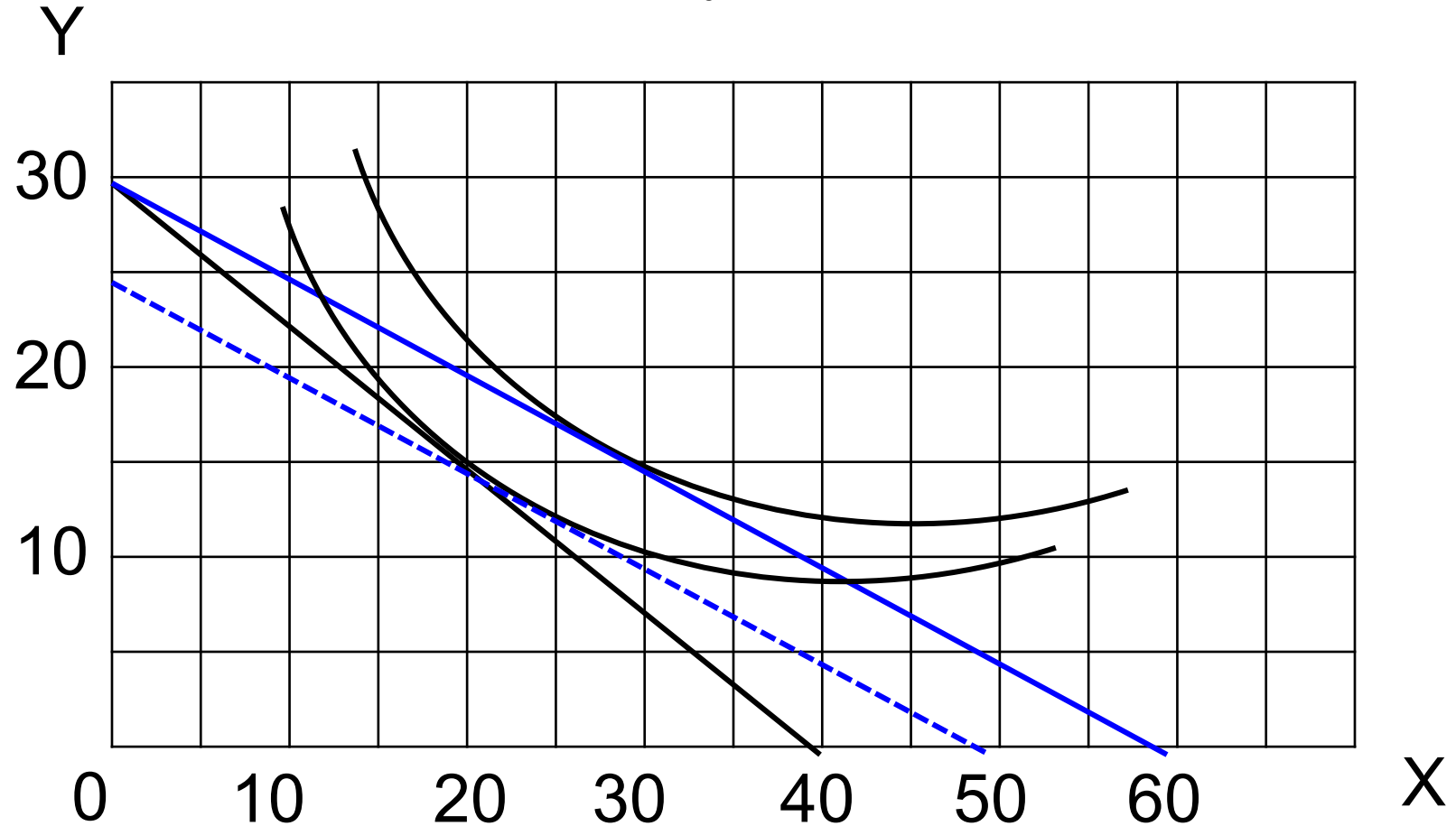
(Note: Real income is kept unchanged by staying on the original IC.)

Income effect

- Change in X due to change in real income
- A fall in P_x increases the consumer's purchasing power, allowing him to reach a higher IC

Graph

- Suppose $P_x = \$3$, $P'_x = \$2$, $P_y = \$4$, and $B = 120$.



Applications:

- Giffen good
- Subsidy
- Vouchers
- Work & leisure
- Intertemporal consumption