

Upstream

$$MC = 2$$

Find MR

$$P = 10 - 2Q$$

$$TR = (10 - 2Q)Q$$

$$TR = 10Q - 2Q^2$$

$$MR = 10 - 4Q$$

Find P_u^* and Q_u^*

$$MR = MC$$

$$\text{sub } Q=2 \text{ in } P = 10 - 2Q$$

$$10 - 4Q = 2$$

$$P = 10 - 2(2)$$

$$8 = 4Q$$

$$P = 6$$

$$Q = 2$$

Downstream

$$MR = 10 - 4Q$$

$$MC = PV^* = 6$$

$$MR = MC$$

$$10 - 4Q = 6$$

$$4 = 4Q$$

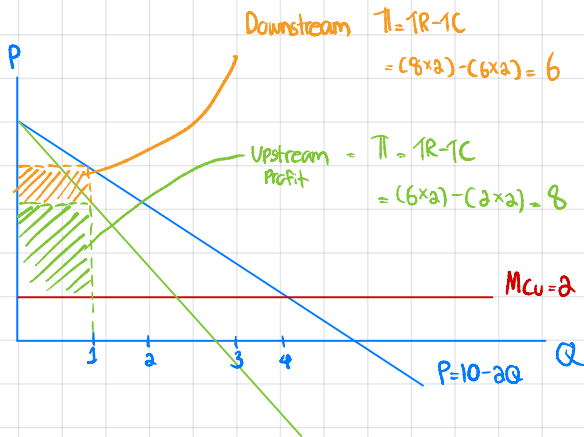
$$Q = 1$$

$$\text{sub } Q=1 \text{ in } P = 10 - 2Q$$

$$P = 10 - 2$$

$$= 8$$

Case 2 firm



∴ If there are 2 firm

$$P_u^* = 6, Q_u^* = 2, P_D^* = 8, Q_D^* = 1$$

$$\pi_u^* = 8, \pi_D^* = 6$$

Case merge firm

$$MR = MC$$

$$\text{sub } Q=2 \text{ in } P = 10 - 2Q$$

$$10 - 4Q = 2$$

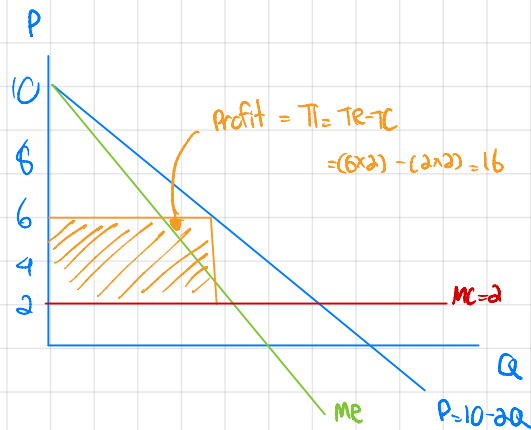
$$P = 10 - 2(2)$$

$$8 = 4Q$$

$$P = 6$$

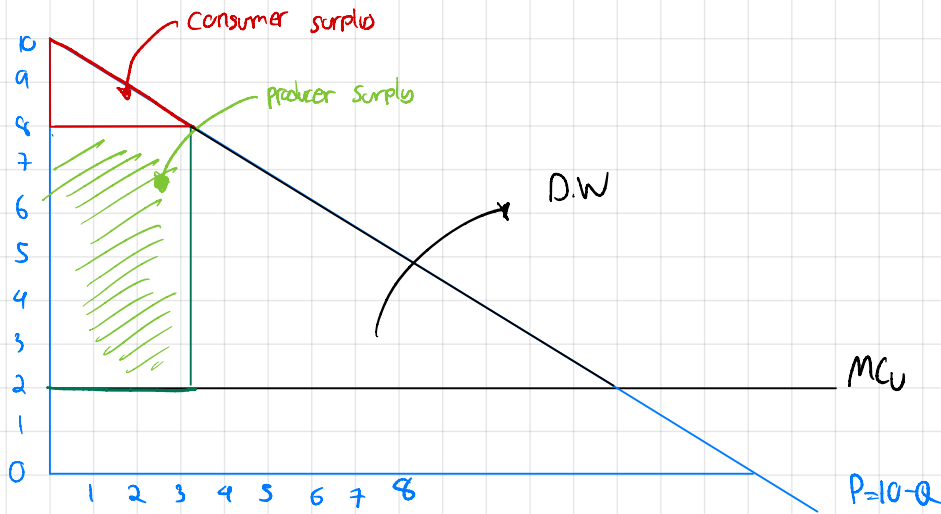
$$Q = 2$$

∴ If merge firm $P^* = 6, Q^* = 2, \pi^* = 8$

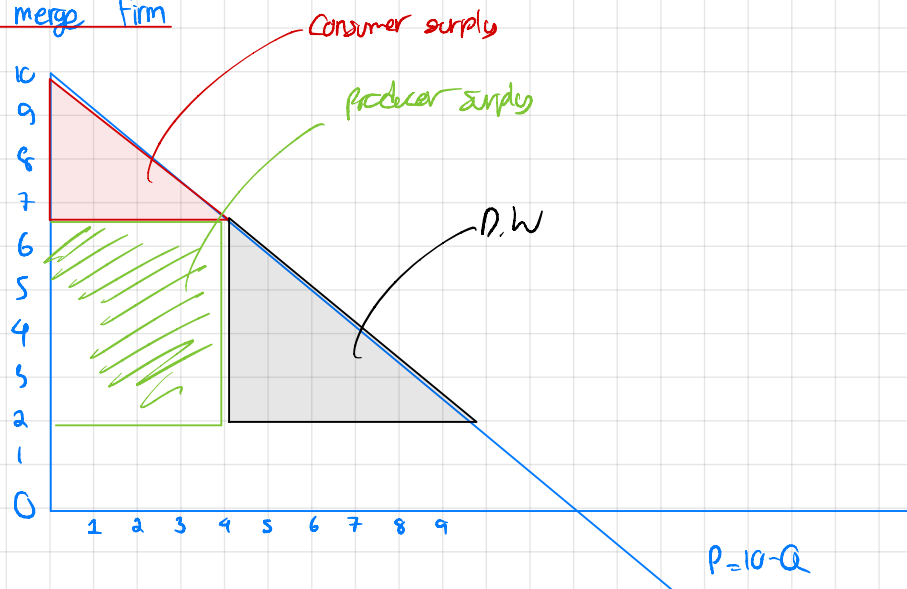


Welfare

Case a firm



Case merge firm



∴ As the firm merge both consumer and producer will have a gain in the economic welfare as the size of dead weight loss get decrease.