

## Formulas

$$\mu = E(X) = \sum_{i=1}^N x_i P(X = x_i)$$

$$\begin{aligned} \text{Variance}(X) = \text{Var}(X) &= E(X - \mu)^2 = E(X^2) - (E(X))^2 \\ &= \sum_{i=1}^N (x_i - \mu)^2 P(X = x_i) \end{aligned}$$

$$P(X = x) = \binom{n}{x} p^x (1-p)^{n-x}, x = 0, 1, \dots, n$$

$$E(X) = np \quad \text{Var}(X) = np(1-p)$$

$$P(X = x) = \frac{e^{-\lambda} \lambda^x}{x!}, x = 0, 1, \dots \quad \lambda = E(X) = \text{Var}(X)$$

$$\chi^2 = \frac{(n-1)S^2}{\sigma^2} \quad \frac{(n-1)S^2}{\chi_{n-1, \frac{\alpha}{2}}^2} < \sigma^2 < \frac{(n-1)S^2}{\chi_{n-1, 1-\frac{\alpha}{2}}^2}$$

$$Z = \frac{x-\mu}{\sigma} \quad Z = \frac{\bar{x}-\mu}{\frac{\sigma}{\sqrt{n}}} \quad Z = \frac{\bar{x}-\mu}{\frac{s}{\sqrt{n}}} \quad t = \frac{\bar{x}-\mu}{\frac{s}{\sqrt{n}}}$$

$$\bar{x} \pm Z_{\frac{\alpha}{2}} \frac{\sigma}{\sqrt{n}} \quad \bar{x} \pm Z_{\frac{\alpha}{2}} \frac{s}{\sqrt{n}} \quad \bar{x} \pm t_{n-1, \frac{\alpha}{2}} \frac{s}{\sqrt{n}}$$

$$p \pm Z_{\frac{\alpha}{2}} \sqrt{\frac{p(1-p)}{n}}$$

$$Z = \frac{p - \pi}{\sqrt{\frac{\pi(1-\pi)}{n}}} \quad Z = \frac{p - \pi}{\sqrt{\frac{p(1-p)}{n}}}$$

$$f_X(x) = \sum_{j=1}^{\infty} f(x, y_j) \quad f(x|y) = \frac{f(x,y)}{f_Y(y)}$$

$$E(X|Y = y) = \sum_{i=1}^{\infty} x_i f(x_i|y)$$

$$\text{Cov}(X, Y) = E(X - E(X))(Y - E(Y)) = E(XY) - E(X)E(Y)$$

$$E(XY) = \sum_{i=1}^{\infty} \sum_{j=1}^{\infty} x_i y_j f(x_i, y_j) \quad E(Y) = \sum_{j=1}^{\infty} y_j f_Y(y_j)$$

$$S^2 = \frac{1}{n-1} \sum_{i=1}^n (x_i - \bar{x})^2 = \frac{1}{n-1} \left( \sum_{i=1}^n x_i^2 - n\bar{x}^2 \right)$$

$$\text{Var}(X + Y) = \text{Var}(X) + \text{Var}(Y) + 2\text{Cov}(X, Y)$$

$$\frac{\sum_{i=1}^k p_{it} q_{i0}}{\sum_{i=1}^k p_{i0} q_{i0}} \times 100 \quad \frac{\sum_{i=1}^k p_{it} q_{it}}{\sum_{i=1}^k p_{i0} q_{it}} \times 100$$

$$\text{Purchase power} = \frac{1}{\text{CPI}} \times 100$$