

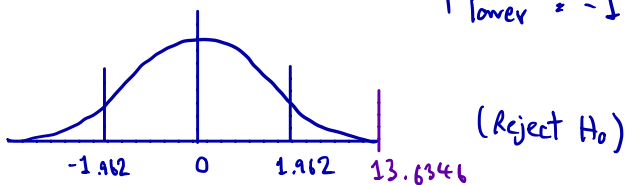
1.a)  $\log(\text{wage}_i) = 0.4436 + 0.0709 \text{educ}_i + 0.3898 \text{exper}_i - 0.006 \text{exper}_i^2 + 0.1925 \text{union}_i - 0.4422 \text{female}_i + u_i$

Based on the coefficient of  $\text{educ}_i$ , if a person has one more year of schooling, the wage would increase by  $100 \times 0.0709\%$ , or  $7.09\%$ . (based on log-in interpretation)

Test if  $0.0709 = 0$  at  $\alpha = 0.05$

$H_0: 0.0709 = 0$        $t_{cal} = \frac{0.0709 - 0}{0.0052} = 13.6346$   
 $H_1: 0.0709 \neq 0$

$df = 1260 - 6 = 1254$        $T_{upper} = 1.962$   
 $T_{lower} = -1.962$



Ans Education has a significant impact on log of wage at 95% significant level

1.b) use f test

$H_0 \rightarrow \beta_2 = \beta_3 = \beta_4 = \beta_5 = \beta_6 = \beta_7 = \beta_8 = 0$   
 $H_1 \rightarrow \text{otherwise}$

$F_{cal} = \frac{ESS/(k-1)}{RSS/(n-k)} = \frac{168.6972/7}{276.2828/1252} = 109.2311$

$F_{upper}(7, 1252) = 2.0096$



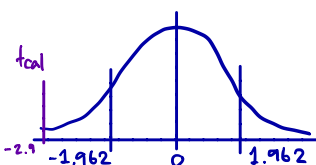
Ans The regression is significant at  $\alpha = 0.05$

1.c) use t test     $\alpha = 0.05$      $df = 1,252$      $t_{crit} = \pm 1.962$

$H_0 \rightarrow \beta_7 = 0$

$H_1 \rightarrow \beta_7 \neq 0$

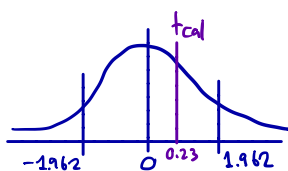
$t_{cal}(\beta_7) = \frac{-0.1388 - 0}{0.0478} = -2.9$



$H_0 \rightarrow \beta_8 = 0$

$H_1 \rightarrow \beta_8 \neq 0$

$t_{cal}(\beta_8) = \frac{0.007 - 0}{0.0303} = 0.23$



Ans Physical attractiveness has an impact on log of hourly wage but only for below average attractiveness. Above average, physical attractiveness has no impact on log of wage/hr.

1.d) No, because above average, physical attractiveness has no impact on log of wage/hr. The woman with average attractiveness and another with above average, both of them will receive the same log of wage/hr. at  $\alpha = 0.05$

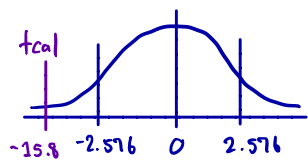
2.a) Yes, for example;  $-2835$  area;  $\rightarrow$  the area (municipality) = 0, otherwise = 1 meaning that households outside municipal areas will have less expenditure, which make sense because the cost of living outside municipal areas is cheaper. And  $+881$  child; make sense because more children almost always correlate to more expenditure.

2.b) use t test  $df = 14,908 - 3 = 14,905$   $\alpha = 0.01$   
 $t_{crit} = \pm 2.576$

$$H_0 \rightarrow 2835 = 0$$

$$H_1 \rightarrow 2835 \neq 0$$

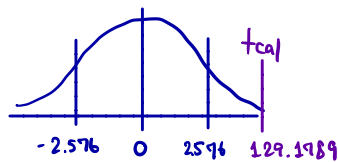
$$t_{cal} = -15.8$$



$$H_0 \rightarrow 881 = 0$$

$$H_1 \rightarrow 881 \neq 0$$

$$t_{cal} = 6.82$$



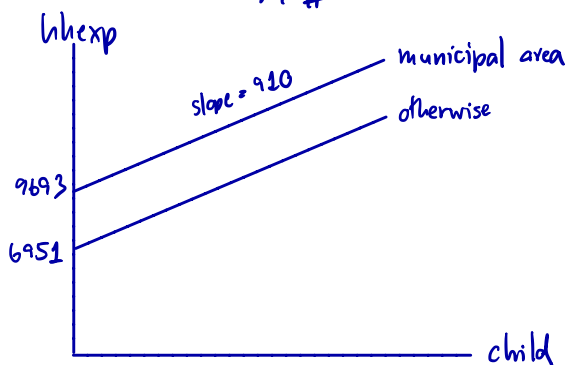
Ans  $\beta_2$  or 2835 is significantly different from zero at  $\alpha = 0.01$

$\beta_3$  or 881 is significantly different from zero at  $\alpha = 0.01$

2.c)  $hhexp = 9736 - 2835 \text{ area} + 881 \text{ child}$

$$hhexp = 9736 - 2835(1) + 881(3)$$

$$= 9374 \#$$



3.a)  $VIF = \frac{1}{1-r^2}$  VIF high  $\rightarrow r^2 \uparrow$  close to 1  $\rightarrow$  more multicollinearity

Ans age & agesq due to high  $r^2$ , which means higher coefficient of correlation between the two variables and higher multicollinearity

3.b) No, because there is no clear correlation between  $week_i$  and  $\hat{u}_i^2$

3.c)  $H_0 \rightarrow$  Homoscedasticity

$H_1 \rightarrow$  Heteroscedasticity

$$F_{cal} = \frac{R^2_{\hat{u}_i^2} / k}{(1 - R^2_{\hat{u}_i^2}) / (n - k - 1)} = \frac{0.0184 / 5}{(1 - 0.0184) / (2032 - 5 - 1)} = 7.6$$

$$F_{crit}(5, 2026) = 2.2141$$

$F_{cal} > F_{crit} \rightarrow$  Reject homoscedasticity

Ans Heterodaticity is present