

1.1) Yes because the cigarette consumption (c_i) decreases by -1.34 when the real price per pack (P_i) increases for \$1. Also, c_i increases by 0.17 when real disposable income per capita increases for \$1.

1.2) Price elasticity = -1.34

$$H_0: \beta_2 = 1$$

$$H_a: \beta_2 \neq 1$$

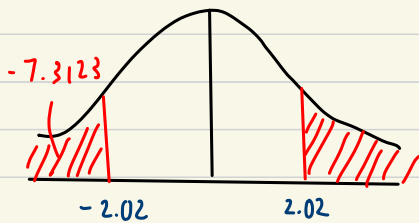
$$t_{\text{cal}} = \frac{-1.34 - 1}{0.32} = -7.3123 \sim t_{46-3}$$

$$t_{\text{lower}} = -2.02$$

$$t_{\text{upper}} = 2.02$$

$$\text{Note: } \alpha = 0.05$$

$$\text{d.f.} = 43$$



\therefore We can reject H_0 , with 95% of confidence interval, it is statistically significant. *

$$1.3) H_0: \beta_3 = 0$$

$$H_a: \beta_3 \neq 0$$

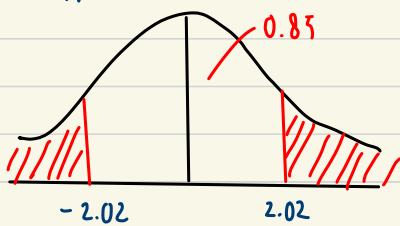
$$t_{\text{cal}} = \frac{0.17 - 0}{0.2} = 0.85 \sim t_{46-3}$$

$$t_{\text{lower}} = -2.02$$

$$t_{\text{upper}} = 2.02$$

$$\text{Note: } \alpha = 0.05$$

$$\text{d.f.} = 43$$



\therefore We can't reject H_0 , with 95% of confidence interval, it is not statistically significant. *

2.

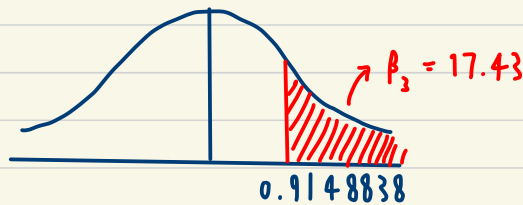
2.1) $H_0: \beta_3 < 1$

$H_a: \beta_3 \geq 1$

$$t_{cal}(\beta_3) = \frac{\hat{\beta}_3 - \beta_3}{\hat{\sigma}_{\hat{\beta}_3}} = 17.43 \sim t_{9, 272}$$

$\alpha = 0.005$

$t_{upper} = 0.9148838$



- β_3 is significant
- reject H_0
- β_3 is ≥ 1 .

2.2) $nettfa_i = \beta_1 + \beta_2 lnc_i + \beta_3 age_i + u_i$ (restricted)

$nettfa_i = \beta_1 + \beta_2 lnc_i + \beta_3 age_i + \beta_4 age_i^2 + u_i$ (unrestricted)

$H_0: \beta_4 = 0$: shouldn't add

$H_a: \beta_4 \neq 0$: should add

Note: $\alpha = 0.05$, $m = k - r = 4 - 3 = 1$

$F_{cal} = \frac{RSS_R - RSS_{UR}}{m}$

$\frac{RSS_{UR}}{h - k}$

$= \frac{(315280770.7 - 31376372.3) / 1}{31376372.3 / 9275 - 4}$

$= 45.03024$

critical value



$F_{0.05, (1, 9271)} = 3.84$

\therefore we reject H_0 since we cannot make sure that, 95% of the time, $\beta_4 = 0$. Thus, we have enough evidence to say that we should add age^2 to the model.

3. $\hat{\beta}_1 = 11.05$

$$\hat{\beta}_2 = -0.95$$

$$\hat{\beta}_3 = -0.13$$

$$\hat{\beta}_4 = 0.25$$

$$\hat{\beta}_5 = 0.05$$

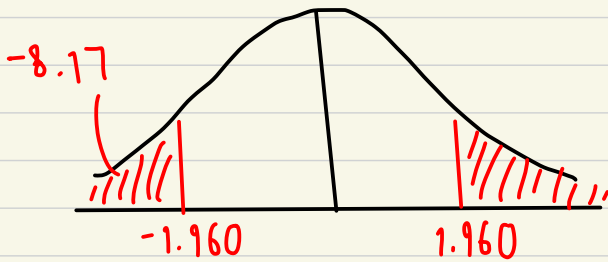
3.2) $\ln(\text{NOX}_i)$

$$H_0: \beta_2 = 0$$

$$H_a: \beta_2 \neq 0$$

$$t_{\text{cal}}(\beta_2) = \frac{0.4535 - 0}{0.1167} = -8.17$$

Note: $\alpha = 0.05$



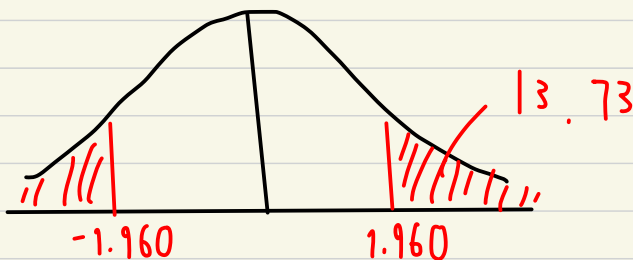
$\therefore \beta_2$ is significant *

Room i

$$H_0: \beta_5 = 0$$

$$H_a: \beta_5 \neq 0$$

$$t_{\text{cal}}(\beta_5) = \frac{0.2545 - 0}{0.01853} = 13.73$$



$\therefore \beta_5$ is significant *

$$3.3) ESS = TSS - RSS = 84.58 - 35.78 = 49.4$$

$$R^2 = \frac{ESS}{TSS} = \frac{84.58}{49.40} = 1.71$$

adjust R^2 :

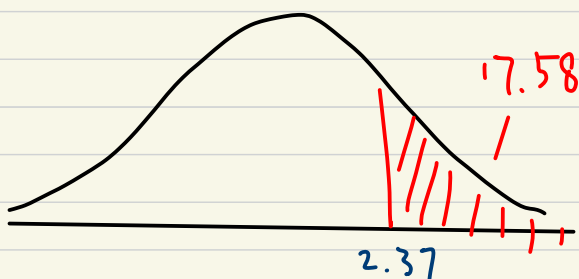
$$\frac{1 - RSS/n \cdot k}{TSS/n - 1} = \frac{-0.07}{0.17} = -0.4$$

$$H_0: \beta_2 = \beta_3 = \beta_4 = \beta_5 = 0$$

Note: $\alpha = 0.05$

H_a : not all coefficients are equal to 0.

$$F_{cal} = \frac{ESS/k-1}{RSS/n-k} = \frac{49.40/4}{35.18/5} = 175.84$$



\therefore we can reject H_0 , with 95% of the time, at least one coefficient is not equal to 0.

4 4.1) model 1: $\ln \hat{Y}_t = 18.27 + 0.536 \ln L_t + 0.024 \ln K_t$

$$\sum_x^y = \frac{\% \Delta y}{\% \Delta x}$$

$$\hat{\beta}_1 = 18.27$$

$$\hat{\beta}_2 = 0.54$$

$$\hat{\beta}_3 = 0.10$$

4.2) model 1: $\ln Y_t = \beta_1 + \beta_2 \ln L_t + \beta_3 \ln K_t + v_t$ (unrestricted)

model 2: $\ln Y_t = \beta_1 + \beta_2 \ln \left(\frac{K}{L} \right) + v_t$ (restricted)

$$H_0: \beta_2 + \beta_3 = 1$$

Note: $\alpha = 0.05$

$$H_a: \beta_2 + \beta_3 \neq 1$$

$$F = \frac{(R_{uk}^2 - R_R^2) / m}{(1 - R_{uk}^2) / (n - k_{uk})} = \frac{(0.9389 - 0.8087) / 1}{(1 - 0.9389) / 127} = 57.535$$

critical value:

$$f_{0.05, 1, 126} = 4.23$$

\therefore we can reject H_0

4.3) We can't compare the R^2 value between the two regression model.