

Upstream

$$MC = 2$$

Find MR

$$P = 10 - 2Q$$

$$TR = (10 - 2Q)Q = 10Q - 2Q^2$$

$$MR = 10 - 4Q$$

$$MR = MC$$

$$10 - 4Q = 2$$

$$Q = 2$$

$$Q = 2$$

$$P = 10 - 2Q$$

$$P = 6$$

Downstream

$$MR = 10 - 4Q$$

$$MC = P_U = 6$$

$$MR = MC$$

$$10 - 4Q = 6$$

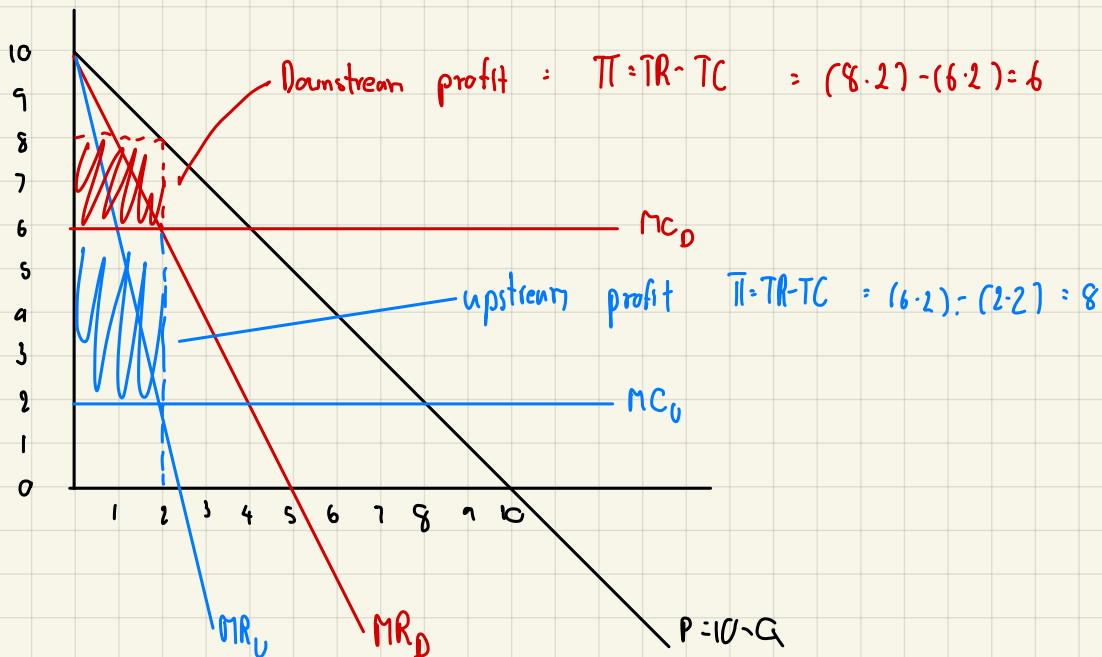
$$Q = 1$$

$$\text{sub } Q = 1 \text{ in } P = 10 - 2Q$$

$$P = 10 - 2$$

$$P = 8$$

Case 2 firm



If there are 2 firms $P_U^* = 6$, $Q_U^* = 2$, $P_D^* = 8$, $Q_D^* = 2$

$$\Pi_U^* = 8, \Pi_D^* = 6$$

Many firm

$$MR = MC$$

$$\text{sub } Q = 4 \text{ in } P = 10 - Q$$

$$10 - 2Q = 2$$

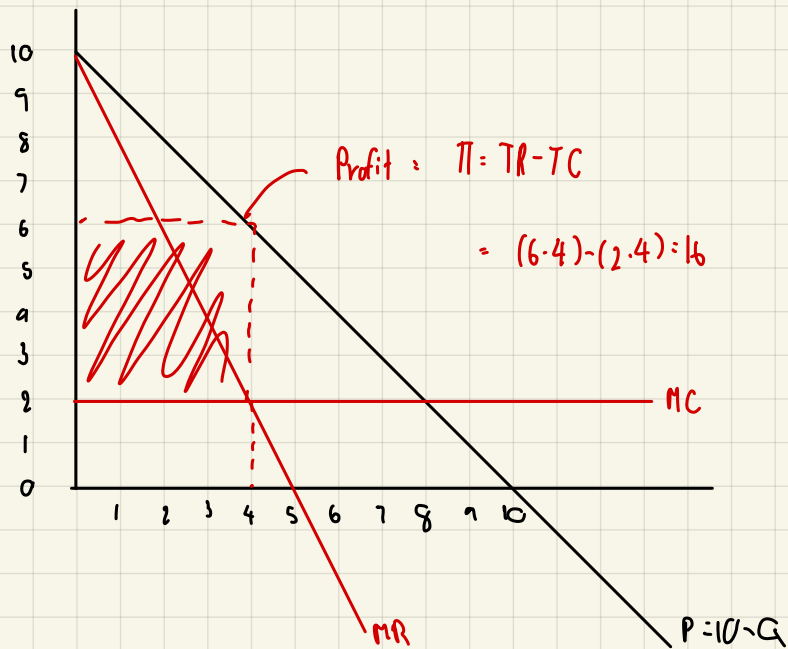
$$P = 10 - 4$$

$$8 = 2Q$$

$$P = 6$$

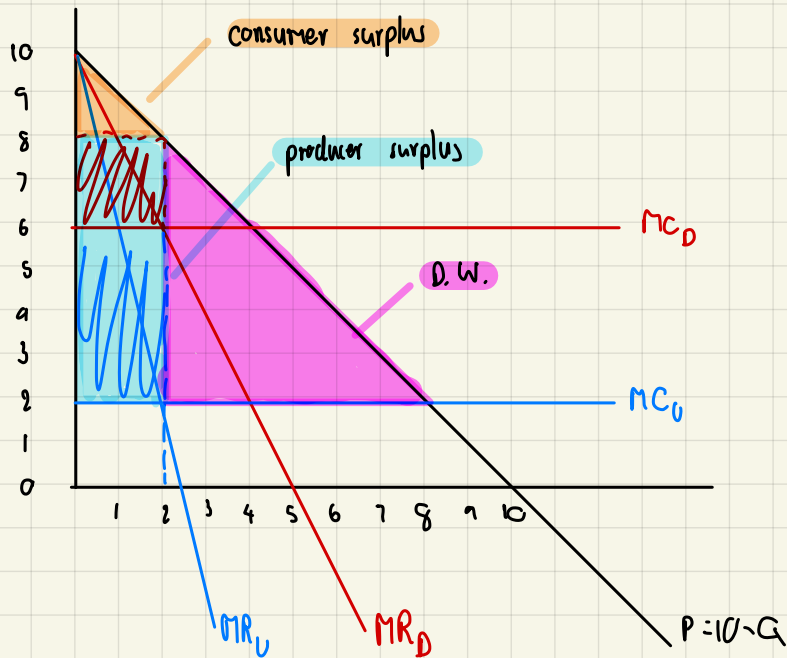
$$Q = 4$$

Merge firm $P^* = 6, Q^* = 4, \pi^* = 16$

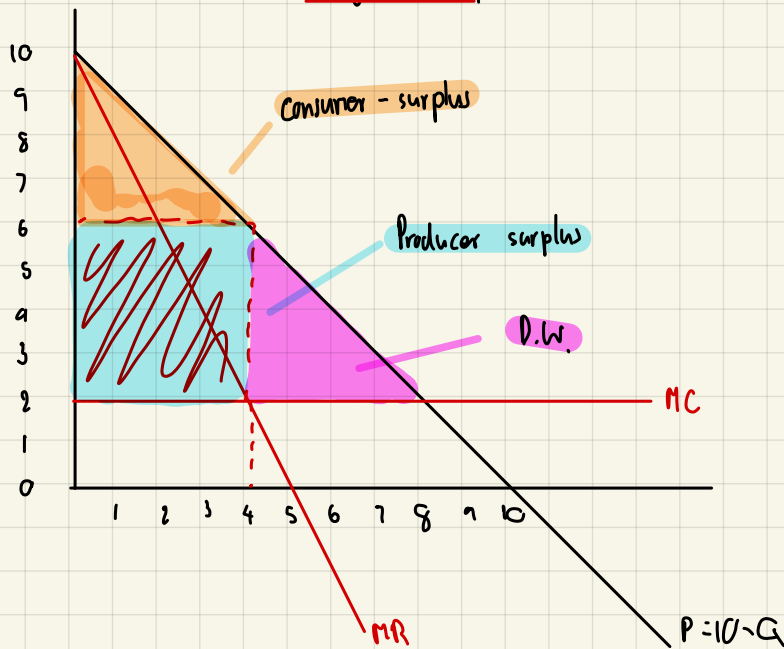


Welfare

2 firm



Merge firm



∴ Because the firm was merged both consumer and producer will have a gain in economic welfare as the size of dead weight loss decreases.