

## Assignment 8

1. Estimate VARs models using spot return (rspot) and future return (rfuture) as endogenous variables and determine the most appropriated lags models using SBIC.

To estimate the VARs model, we need to perform unit root test in order to ensure that all variables are stationary. However, this test already performed in the past assignment and it shows that all variables are stationary. Then, we determine the optimal lag by using SBIC as a criteria. We find out that the model with 6 lags is the most appropriated model since it has the lowest SBIC value which is -20.053.

```
. g rspot = (spot/l.spot)-1
(1 missing value generated)
```

```
. g rfuture = (future/l.future)-1
(1 missing value generated)
```

```
. varsoc rspot rfuture, maxlag(10)
```

Selection-order criteria

Sample: 12 - 7684

Number of obs = 7673

| lag | LL      | LR     | df | p     | FPE      | AIC       | HQIC      | SBIC     |
|-----|---------|--------|----|-------|----------|-----------|-----------|----------|
| 0   | 76671.7 |        |    |       | 7.2e-12  | -19.9843  | -19.9837  | -19.9825 |
| 1   | 76840.9 | 338.5  | 4  | 0.000 | 6.9e-12  | -20.0274  | -20.0255  | -20.0219 |
| 2   | 76931.4 | 180.85 | 4  | 0.000 | 6.7e-12  | -20.0499  | -20.0468  | -20.0408 |
| 3   | 76963.2 | 63.709 | 4  | 0.000 | 6.7e-12  | -20.0571  | -20.0528  | -20.0445 |
| 4   | 76979.4 | 32.291 | 4  | 0.000 | 6.7e-12  | -20.0603  | -20.0547  | -20.044  |
| 5   | 77017.6 | 76.544 | 4  | 0.000 | 6.6e-12  | -20.0692  | -20.0624  | -20.0493 |
| 6   | 77049.6 | 63.872 | 4  | 0.000 | 6.5e-12  | -20.0765  | -20.0684  | -20.053* |
| 7   | 77059.6 | 20.054 | 4  | 0.000 | 6.5e-12  | -20.0781  | -20.0688  | -20.0509 |
| 8   | 77070.3 | 21.332 | 4  | 0.000 | 6.5e-12  | -20.0798  | -20.0693* | -20.0491 |
| 9   | 77076.4 | 12.37* | 4  | 0.015 | 6.5e-12* | -20.0804* | -20.0686  | -20.046  |
| 10  | 77080.2 | 7.4487 | 4  | 0.114 | 6.5e-12  | -20.0803  | -20.0673  | -20.0423 |

Endogenous: rspot rfuture

Exogenous: \_cons

```
. var rspot rfuture, lag(1/6)
```

Vector autoregression

```
Sample: 8 - 7684      Number of obs   =    7,677
Log likelihood = 77062.5      AIC           = -20.06943
FPE           = 6.59e-12      HQIC          = -20.06136
Det(Sigma_ml) = 6.55e-12      SBIC           = -20.0459
```

| Equation | Parms | RMSE    | R-sq   | chi2     | P>chi2 |
|----------|-------|---------|--------|----------|--------|
| rspot    | 13    | .001777 | 0.0159 | 124.0308 | 0.0000 |
| rfuture  | 13    | .002042 | 0.0211 | 165.0864 | 0.0000 |

|                | Coef.     | Std. Err. | z      | P> z  | [95% Conf. Interval] |           |
|----------------|-----------|-----------|--------|-------|----------------------|-----------|
| <b>rspot</b>   |           |           |        |       |                      |           |
| rspot          |           |           |        |       |                      |           |
| L1.            | -.0429887 | .0160995  | -2.67  | 0.008 | -.0745432            | -.0114342 |
| L2.            | -.1255145 | .0163803  | -7.66  | 0.000 | -.1576194            | -.0934097 |
| L3.            | -.0654555 | .0165559  | -3.95  | 0.000 | -.0979044            | -.0330066 |
| L4.            | -.0555308 | .0165648  | -3.35  | 0.001 | -.0879973            | -.0230644 |
| L5.            | -.0646528 | .0163598  | -3.95  | 0.000 | -.0967173            | -.0325882 |
| L6.            | -.0420281 | .0160563  | -2.62  | 0.009 | -.0734979            | -.0105584 |
| rfuture        |           |           |        |       |                      |           |
| L1.            | .1025108  | .0140081  | 7.32   | 0.000 | .0750554             | .1299661  |
| L2.            | .0827253  | .0143869  | 5.75   | 0.000 | .0545274             | .1109231  |
| L3.            | .0530446  | .0145602  | 3.64   | 0.000 | .0245072             | .081582   |
| L4.            | .057478   | .0145501  | 3.95   | 0.000 | .0289603             | .0859958  |
| L5.            | .0435619  | .0143967  | 3.03   | 0.002 | .0153449             | .0717788  |
| L6.            | .0372007  | .0140183  | 2.65   | 0.008 | .0097254             | .064676   |
| _cons          | .0000232  | .0000203  | 1.14   | 0.252 | -.0000165            | .0000629  |
| <b>rfuture</b> |           |           |        |       |                      |           |
| rspot          |           |           |        |       |                      |           |
| L1.            | .2117743  | .0185008  | 11.45  | 0.000 | .1755133             | .2480352  |
| L2.            | .0743206  | .0188235  | 3.95   | 0.000 | .0374272             | .1112139  |
| L3.            | .0828566  | .0190252  | 4.36   | 0.000 | .0455679             | .1201454  |
| L4.            | .0448446  | .0190355  | 2.36   | 0.018 | .0075357             | .0821535  |
| L5.            | .0674903  | .0187999  | 3.59   | 0.000 | .0306433             | .1043374  |
| L6.            | .0590473  | .0184511  | 3.20   | 0.001 | .0228838             | .0952109  |
| rfuture        |           |           |        |       |                      |           |
| L1.            | -.1623592 | .0160974  | -10.09 | 0.000 | -.1939096            | -.1308088 |
| L2.            | -.1054217 | .0165328  | -6.38  | 0.000 | -.1378253            | -.073018  |
| L3.            | -.0724314 | .0167319  | -4.33  | 0.000 | -.1052253            | -.0396376 |
| L4.            | -.042915  | .0167203  | -2.57  | 0.010 | -.0756863            | -.0101437 |
| L5.            | -.0604119 | .016544   | -3.65  | 0.000 | -.0928375            | -.0279863 |
| L6.            | -.0392965 | .0161092  | -2.44  | 0.015 | -.0708699            | -.0077232 |
| _cons          | .0000259  | .0000233  | 1.11   | 0.266 | -.0000198            | .0000715  |

## 2. Perform stability test and Granger exogeneity test.

To evaluate the model, we need to test for stability and exogeneity. For the stability test, the result shows that all the eigen values lie inside the unit circle and VAR satisfies stability condition, meaning that the model has stability property. For the Granger exogeneity test, the purpose is to prove for independency. The prob > Chi2 for all variables is 0.00 (<0.05), implying that we can reject the null hypothesis that the variables are exogeneity at 95% confidence level. Therefore, both variables are endogeneity or interdependent relation.

. varstable, graph

Eigenvalue stability condition

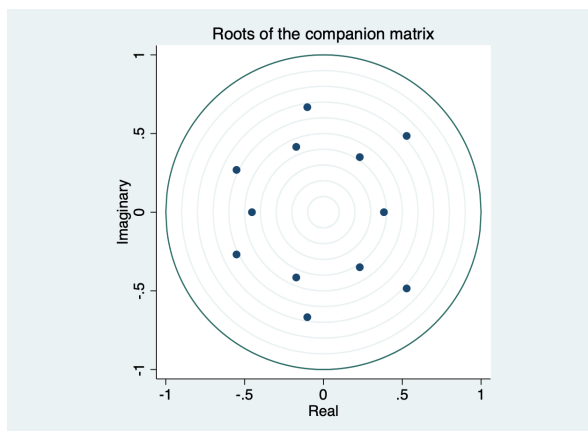
| Eigenvalue            | Modulus |
|-----------------------|---------|
| .5279554 + .4847924i  | .716771 |
| .5279554 - .4847924i  | .716771 |
| -.1022778 + .6675194i | .67531  |
| -.1022778 - .6675194i | .67531  |
| -.5513603 + .2689237i | .613448 |
| -.5513603 - .2689237i | .613448 |
| -.4536067             | .453607 |
| -.1726167 + .4151256i | .449584 |
| -.1726167 - .4151256i | .449584 |
| .2305361 + .3500458i  | .419141 |
| .2305361 - .3500458i  | .419141 |
| .3837855              | .383786 |

All the eigenvalues lie inside the unit circle.  
VAR satisfies stability condition.

. vargranger

Granger causality Wald tests

| Equation | Excluded | chi2   | df | Prob > chi2 |
|----------|----------|--------|----|-------------|
| rspot    | rfuture  | 82.299 | 6  | 0.000       |
| rspot    | ALL      | 82.299 | 6  | 0.000       |
| rfuture  | rspot    | 148.42 | 6  | 0.000       |
| rfuture  | ALL      | 148.42 | 6  | 0.000       |



### 3. Perform Impulse response analysis and determine which variable has more impact.

To interpret the estimated results, we need to derive the impact to be Impulse response function (IRF). However, in reality, the innovations or error term in VAR are not contemporaneously independent of once another. Then, it would be better to look at Cumulative orthogonal impulse response function (COIRF). The result shows that all values are significant since the lower and upper do not cover 0. The impulse response of rspot has a slightly higher impact on rspot. While the impulse response of rfuture has a higher impact on rfuture.

```
. irf create order1, order(rspot rfuture) step(6) set(irf01)
(file irf01.irf created)
(file irf01.irf now active)
(file irf01.irf updated)
```

```
. irf table irf, impulse(rspot rfuture) response(rspot rfuture)
```

Results from order1

| step | (1)<br>irf | (1)<br>Lower | (1)<br>Upper | (2)<br>irf | (2)<br>Lower | (2)<br>Upper | (3)<br>irf | (3)<br>Lower | (3)<br>Upper | (4)<br>irf | (4)<br>Lower | (4)<br>Upper |
|------|------------|--------------|--------------|------------|--------------|--------------|------------|--------------|--------------|------------|--------------|--------------|
| 0    | 1          | 1            | 1            | 0          | 0            | 0            | 0          | 0            | 0            | 1          | 1            | 1            |
| 1    | -.042989   | -.074543     | -.011434     | .211774    | .175513      | .248035      | .102511    | .075055      | .129966      | -.162359   | -.19391      | -.130809     |
| 2    | -.101957   | -.133505     | -.070409     | .030833    | -.00561      | .067276      | .061675    | .034224      | .089126      | -.057352   | -.089063     | -.025641     |
| 3    | -.034997   | -.066566     | -.003428     | .030738    | -.005677     | .067153      | .018216    | -.009265     | .045697      | -.025324   | -.057023     | .006376      |
| 4    | -.02148    | -.052956     | .009995      | .002714    | -.033596     | .039023      | .026291    | -.001106     | .053688      | -.004062   | -.035665     | .027541      |
| 5    | -.033647   | -.06485      | -.002443     | .034962    | -.001046     | .070971      | .01553     | -.011653     | .042713      | -.029332   | -.060699     | .002035      |
| 6    | -.010717   | -.041519     | .020085      | .017646    | -.017933     | .053226      | .006933    | -.01982      | .033686      | -.003566   | -.034475     | .027344      |

95% lower and upper bounds reported

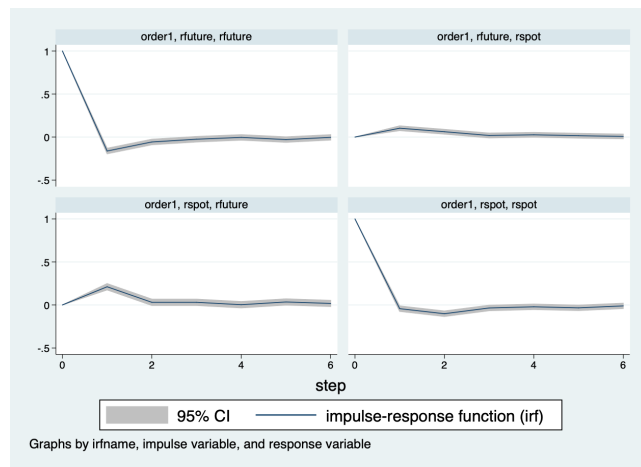
(1) irfname = order1, impulse = rspot, and response = rspot

(2) irfname = order1, impulse = rspot, and response = rfuture

(3) irfname = order1, impulse = rfuture, and response = rspot

(4) irfname = order1, impulse = rfuture, and response = rfuture

```
. irf graph irf, impulse(rspot rfuture) response(rspot rfuture)
```



```
. irf table oirf, impulse(rspot rfuture) response(rspot rfuture)
```

Results from order1

| step | (1)<br>oirf | (1)<br>Lower | (1)<br>Upper | (2)<br>oirf | (2)<br>Lower | (2)<br>Upper | (3)<br>oirf | (3)<br>Lower | (3)<br>Upper | (4)<br>oirf | (4)<br>Lower | (4)<br>Upper |
|------|-------------|--------------|--------------|-------------|--------------|--------------|-------------|--------------|--------------|-------------|--------------|--------------|
| 0    | .001775     | .001747      | .001803      | .001444     | .001404      | .001483      | 0           | 0            | 0            | .001441     | .001419      | .001464      |
| 1    | .000072     | .000032      | .000112      | .000142     | .000096      | .000188      | .000148     | .000108      | .000187      | -.000234    | -.00028      | -.000188     |
| 2    | -.000092    | -.000132     | -.000052     | -.000028    | -.000074     | .000018      | .000089     | .000049      | .000128      | -.000083    | -.000128     | -.000037     |
| 3    | -.000036    | -.000076     | 4.1e-06      | .000018     | -.000028     | .000064      | .000026     | -.000013     | .000066      | -.000037    | -.000082     | 9.2e-06      |
| 4    | -1.8e-07    | -.00004      | .00004       | -1.0e-06    | -.000047     | .000045      | .000038     | -1.6e-06     | .000077      | -5.9e-06    | -.000051     | .00004       |
| 5    | -.000037    | -.000077     | 2.5e-06      | .00002      | -.000026     | .000066      | .000022     | -.000017     | .000062      | -.000042    | -.000087     | 2.9e-06      |
| 6    | -9.0e-06    | -.000049     | .000031      | .000026     | -.00002      | .000072      | 1.0e-05     | -.000029     | .000049      | -5.1e-06    | -.00005      | .000039      |

95% lower and upper bounds reported

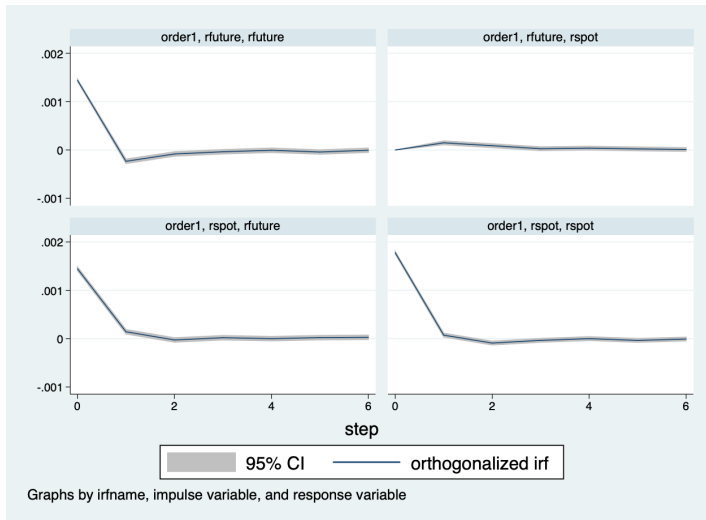
(1) irfname = order1, impulse = rspot, and response = rspot

(2) irfname = order1, impulse = rspot, and response = rfuture

(3) irfname = order1, impulse = rfuture, and response = rspot

(4) irfname = order1, impulse = rfuture, and response = rfuture

```
. irf graph oirf, impulse(rspot rfuture) response(rspot rfuture)
```



```
. irf table coirf, impulse(rspot rfuture) response(rspot rfuture)
```

Results from order1

| step | (1)<br>coirf | (1)<br>Lower | (1)<br>Upper | (2)<br>coirf | (2)<br>Lower | (2)<br>Upper | (3)<br>coirf | (3)<br>Lower | (3)<br>Upper | (4)<br>coirf | (4)<br>Lower | (4)<br>Upper |
|------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|
| 0    | .001775      | .001747      | .001803      | .001444      | .001404      | .001483      | 0            | 0            | 0            | .001441      | .001419      | .001464      |
| 1    | .001847      | .001798      | .001896      | .001585      | .001527      | .001644      | .000148      | .000108      | .000187      | .001207      | .001158      | .001257      |
| 2    | .001755      | .001691      | .001819      | .001557      | .001484      | .00163       | .000237      | .00018       | .000294      | .001125      | .001059      | .00119       |
| 3    | .001719      | .001644      | .001794      | .001575      | .001491      | .001659      | .000263      | .000194      | .000332      | .001088      | .00101       | .001166      |
| 4    | .001719      | .001635      | .001803      | .001574      | .00148       | .001668      | .000301      | .000223      | .000379      | .001082      | .000995      | .00117       |
| 5    | .001682      | .001589      | .001774      | .001594      | .001491      | .001697      | .000323      | .000238      | .000409      | .00104       | .000945      | .001136      |
| 6    | .001673      | .001573      | .001772      | .00162       | .001509      | .001731      | .000333      | .000242      | .000424      | .001035      | .000934      | .001136      |

95% lower and upper bounds reported

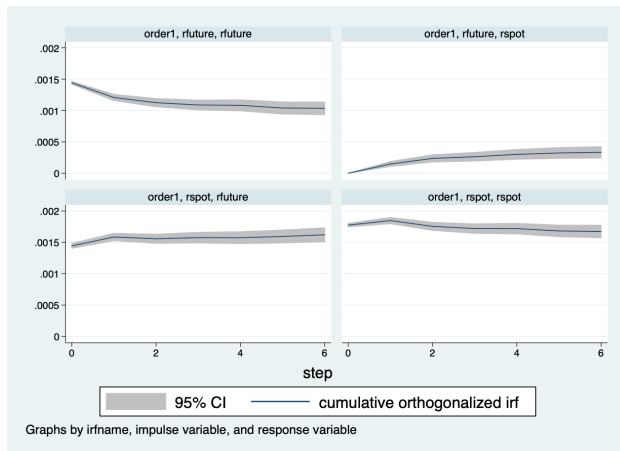
(1) irfname = order1, impulse = rspot, and response = rspot

(2) irfname = order1, impulse = rspot, and response = rfuture

(3) irfname = order1, impulse = rfuture, and response = rspot

(4) irfname = order1, impulse = rfuture, and response = rfuture

```
. irf graph coirf, impulse(rspot rfuture) response(rspot rfuture)
```



4. Perform forecast error variance decomposition and determine variable that has more impact on each endogenous variable.

From the results, we can see that the lower and upper do not cover 0, meaning that the test is significant. In addition, when looking at fevd, we can see the percentage of the variance of predicted Y caused by orthogonal innovation from each variable. So, impulse response of rspot has more impact on rspot since the percentage of decomposition is higher compared with rfuture ( $99\% > 1\%$ ). While impulse response of rfuture has almost the same impact on rspot and rfuture ( $50\%$ ).

```
. irf table fevd, impulse(rspot rfuture) response(rspot)
```

Results from order1

| step | (1)<br>fevd | (1)<br>Lower | (1)<br>Upper | (2)<br>fevd | (2)<br>Lower | (2)<br>Upper |
|------|-------------|--------------|--------------|-------------|--------------|--------------|
| 0    | 0           | 0            | 0            | 0           | 0            | 0            |
| 1    | 1           | 1            | 1            | 0           | 0            | 0            |
| 2    | .993131     | .989465      | .996798      | .006869     | .003202      | .010535      |
| 3    | .998693     | .98638       | .995006      | .009307     | .004994      | .01362       |
| 4    | .998483     | .986145      | .994821      | .009517     | .005179      | .013855      |
| 5    | .998038     | .98565       | .994426      | .009962     | .005574      | .01435       |
| 6    | .989888     | .985487      | .994289      | .010112     | .005711      | .014513      |

95% lower and upper bounds reported

(1) irfname = order1, impulse = rspot, and response = rspot

(2) irfname = order1, impulse = rfuture, and response = rspot

```
. irf table fevd, impulse(rspot rfuture) response(rfuture)
```

Results from order1

| step | (1)<br>fevd | (1)<br>Lower | (1)<br>Upper | (2)<br>fevd | (2)<br>Lower | (2)<br>Upper |
|------|-------------|--------------|--------------|-------------|--------------|--------------|
| 0    | 0           | 0            | 0            | 0           | 0            | 0            |
| 1    | .500791     | .484986      | .516596      | .499209     | .483404      | .515014      |
| 2    | .496679     | .480799      | .512558      | .503321     | .487442      | .519201      |
| 3    | .495972     | .480066      | .511879      | .504028     | .488121      | .519934      |
| 4    | .495855     | .479951      | .51176       | .504145     | .48824       | .520049      |
| 5    | .495851     | .479947      | .511756      | .504149     | .488244      | .520053      |
| 6    | .495689     | .479783      | .511594      | .504311     | .488406      | .520217      |

95% lower and upper bounds reported

(1) irfname = order1, impulse = rspot, and response = rfuture

(2) irfname = order1, impulse = rfuture, and response = rfuture