

EE320 (1/2017)

INTRODUCTORY MATHEMATICAL ECONOMICS

EQUILIBRIUM and COMPARATIVE STATIC ANALYSIS

(Part 2)

Topics

- Equilibrium in Macroeconomic Models
 - Partial Market Equilibrium: Keynesian National-Income Model
 - General Equilibrium: IS-LM Model
- Comparative statics
- Policy effectiveness

Simplest Keynesian National-Income Model

- Consider a *closed* economy (i.e. no trade).

- The equilibrium is: $Y = C + I_0 + G_0 = AE$

where $C = a + bY \quad (a > 0, 0 < b < 1)$

- At equilibrium, $Y = a + bY + I_0 + G_0$



- Corresponding consumption: $C^* = a + bY^*$



Closed Economy with Proportional Income Tax

- Equilibrium condition: $Y = C + I_0 + G_0 = AE$

where $C = a + bY_d \quad (a > 0, 0 < b < 1)$

$$Y_d = Y - T$$

$$T = tY \quad (0 < t < 1)$$

➤ At equilibrium, $Y = a + bY_d + I_0 + G_0$

$$Y = a + b(1-t)Y + I_0 + G_0$$

$$\Rightarrow Y^* = \frac{a + I_0 + G_0}{1 - b(1-t)}$$

$$\Rightarrow C^* = \frac{a + b(1-t)(I_0 + G_0)}{1 - b(1-t)}$$

Open Economy with Proportional Income Tax

- Equilibrium condition: $Y = C + I_0 + G_0 + X_0 - M = AE$

where

$$C = a + bY_d \quad (a > 0, 0 < b < 1)$$

$$T = tY \quad (0 < t < 1)$$

$$M = mY$$

- At equilibrium, $Y = a + b(1-t)Y + I_0 + G_0 + X_0 - mY$



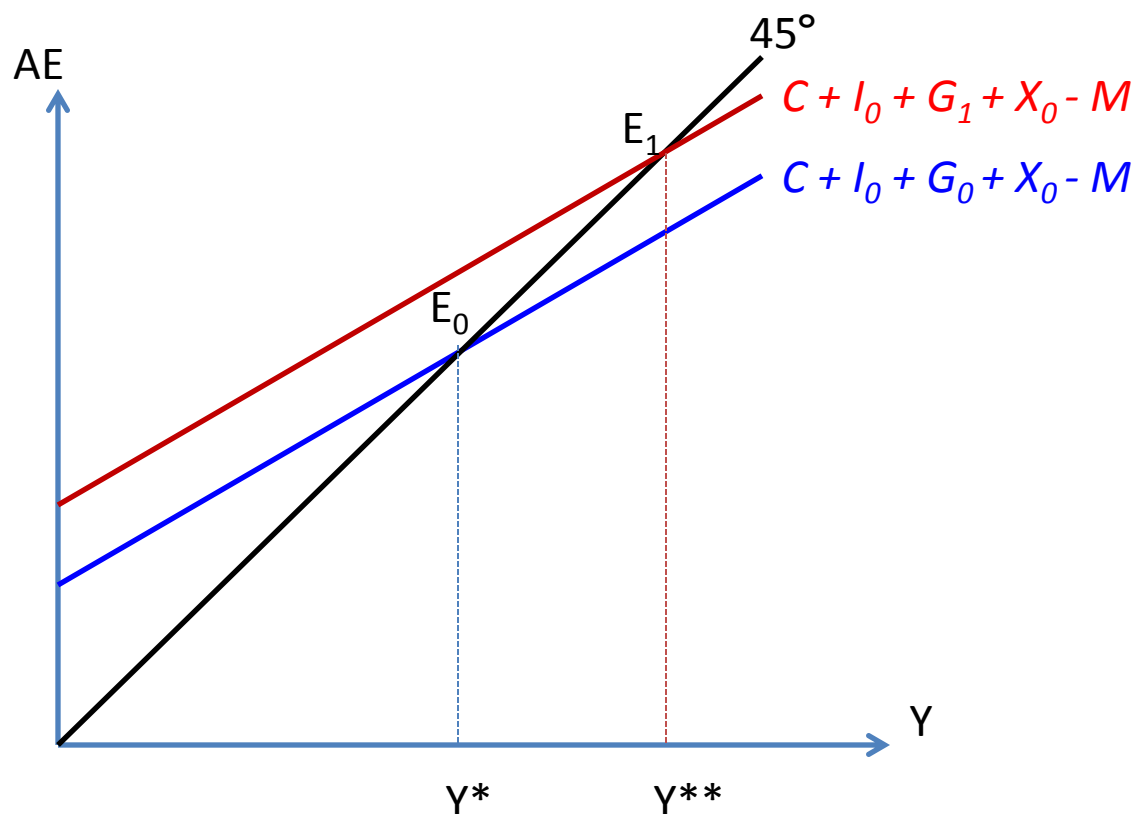
$$Y^* = \frac{a + I_0 + G_0 + X_0}{1 - b(1-t) + m}$$



$$C^* = \frac{a(1+m) + b(1-t)(I_0 + G_0 + X_0)}{1 - b(1-t) + m}$$

- If $M = mY_d$, $Y^* = ?$ (own practice!)

Graph: Keynesian National-Income Model



Suppose G increases. What is the new value of Y^* ?

➔ Will show the answer on slide 11.

IS-LM Model

- The previous Keynesian model only deals with the equilibrium in the goods (or commodity) market. It seeks to determine the equilibrium level of national income.
- The **IS-LM model** deals with not only the **commodity market** but also the **money market**. It determines **the equilibrium levels of national income and interest rate** in the economy.
- The **IS curve** represents the equilibrium in the commodity market.
 - **Planned “investment” = Planned “savings”**
- The **LM curve** represents the equilibrium in the money market.
 - **Liquidity preference (money demand) = Money supply**

IS-LM Model: Closed Economy & No Tax

- Commodity Market:

$$Y = C + I + G_0$$

$$C = a + bY \quad (a > 0, 0 < b < 1)$$

$$I = I_0 - ir \quad (I_0, i > 0, \text{ and } r \text{ is interest rate})$$

➤ $Y = a + bY + I_0 - ir + G_0 \quad \rightarrow \quad : IS$

- Money Market:

$$M^S = M_0$$

$$M^D = kY - hr \quad (k, h > 0)$$

➤ At equilibrium, $M_0 = kY - hr \quad \rightarrow \quad : LM$

➤ From the two equilibrium conditions, we can solve for Y^* and r^* :

IS-LM Model: Closed Economy with Tax

- Commodity Market:

$$Y = C + I + G_0$$

$$C = a + bY_d \quad (a > 0, 0 < b < 1)$$

$$I = I_0 - ir \quad (I_0, i > 0)$$

$$Y_d = Y - T \quad \text{where } T = tY \quad (0 < t < 1)$$

$$\Rightarrow Y = a + b(1-t)Y + I_0 - ir + G_0$$

$$\Rightarrow Y = \frac{(a + I_0 + G_0) - ir}{1 - b(1-t)} : IS$$

- Money Market:

$$M^S = M_0$$

$$M^D = kY - hr \quad (k, h > 0)$$

$$\Rightarrow M_0 = kY - hr$$

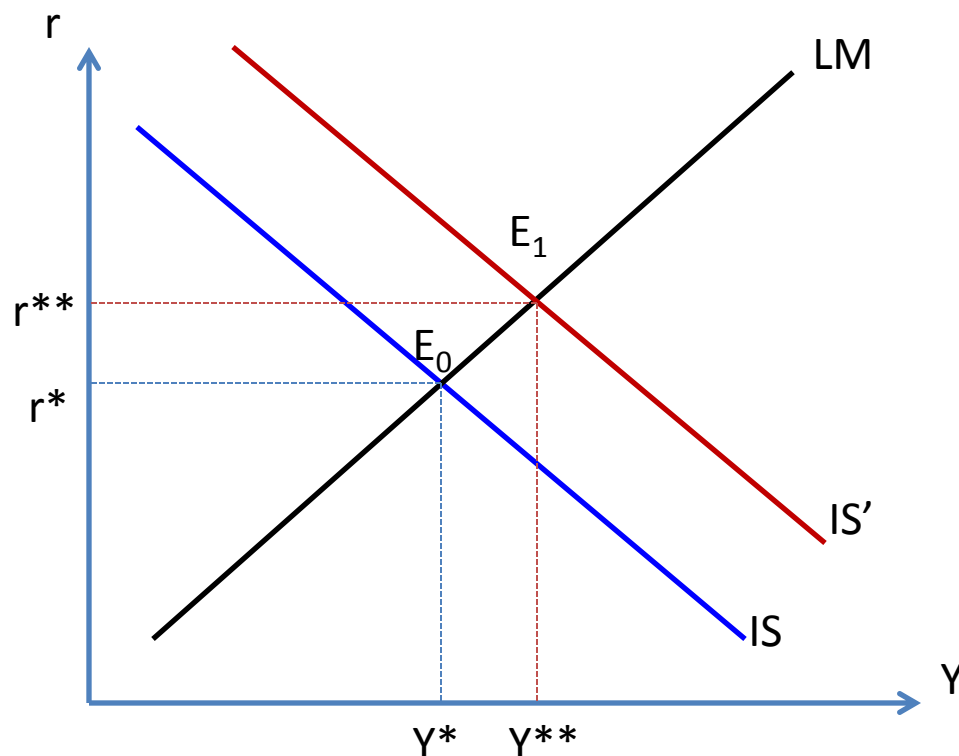
$$\Rightarrow Y = \frac{M_0}{k} + \frac{h}{k}r : LM$$

- Equilibrium values for Y^* and r^* :

$$Y^* = \frac{(a + I_0 + G_0)h + iM_0}{ik + h[1 - b(1-t)]}$$

$$\text{and } r^* = \frac{(a + I_0 + G_0)k - [1 - b(1-t)M_0]}{ik + h[1 - b(1-t)]}$$

Graph: Equilibrium in IS-LM Model



- When the government increases its expenditure, what's the impact on the equilibrium Y and r ? (➔ Will show the answer on slide 12.)

Comparative Statics Analysis: Simple Macroeconomic Model

- Suppose government increases its expenditure, what's the impact on the equilibrium national income (i.e. $\Delta Y^*/\Delta G=?$)
- Recall: $Y^* = \frac{a + I_0 + G_0 + X_0}{1 - b(1 - t) + m}$, and suppose $\Delta G = G_1 - G_0$.



Comparative Statics Analysis: IS-LM Model

- In a closed economy with tax, suppose G increases ($\Delta G = G_1 - G_0$), $\Delta Y^*/\Delta G = ?$ and $\Delta r^*/\Delta G = ?$
- Recall: $Y^* = \frac{(a + I_0 + G_0)h + iM_0}{ik + h[1 - b(1 - t)]}$ and $r^* = \frac{(a + I_0 + G_0)k - [1 - b(1 - t)]M_0}{ik + h[1 - b(1 - t)]}$

Policy Implications

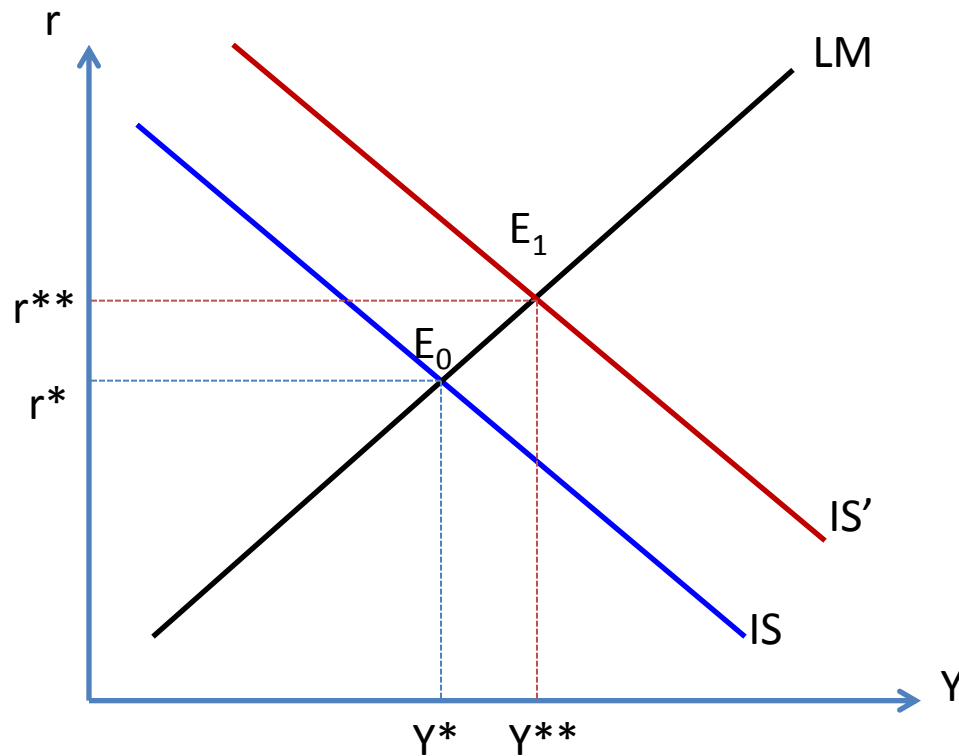
- **Crowding out effect**

- An increase in government expenditure (G) can have a side-effect in lowering private investment (I), through higher r . As a result, the aggregate expenditure (Y) will not increase as in the case in which r is fixed.

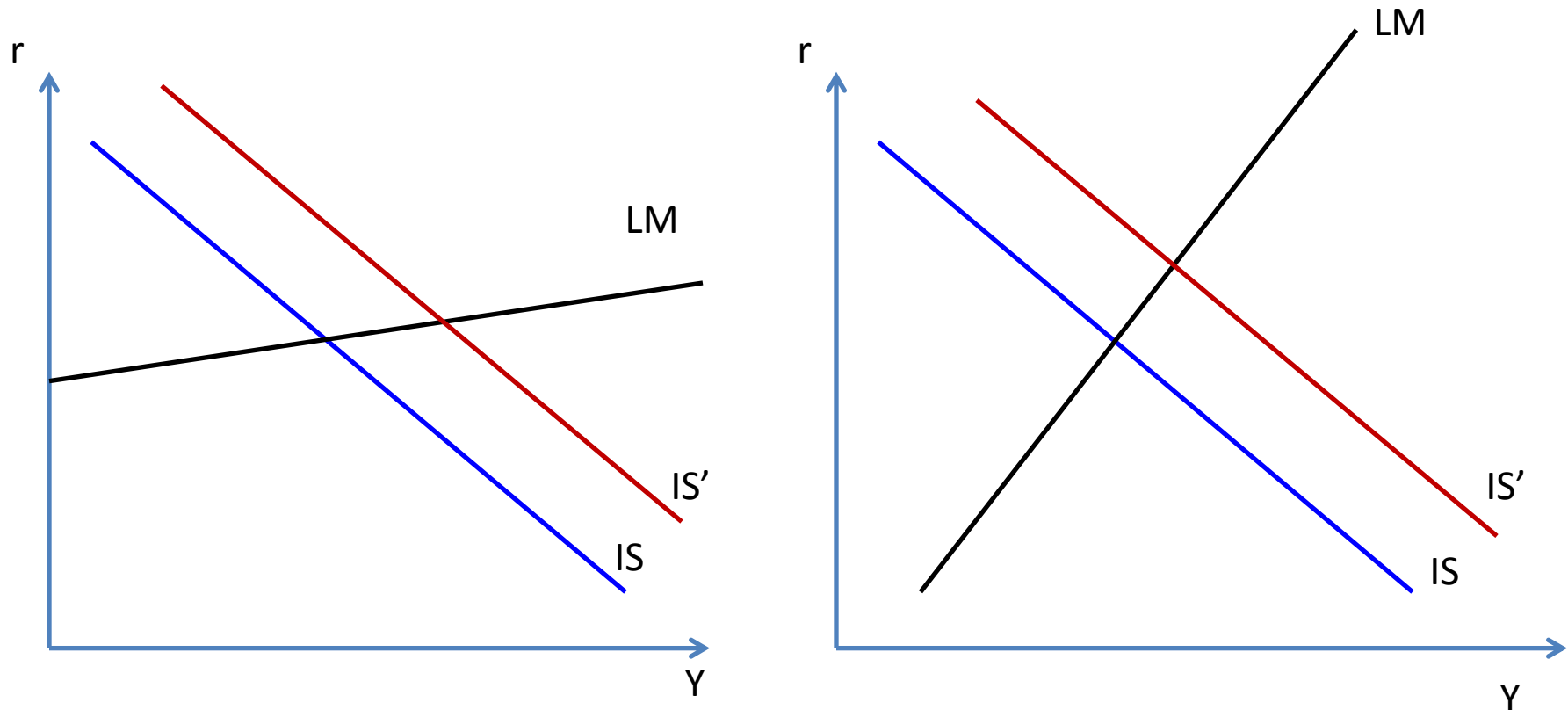
- **Policy effectiveness**

- Monetary policy is more effective when IS curve is flatter.
- Fiscal policy is more effective when LM curve is flatter.

Graph: Crowding-Out Effect



Graph: Policy Effectiveness (1)



Graph: Policy Effectiveness (2)

