

EX.4, p.6

$$(a) \quad y = a^x$$

$$\because a \text{ is a constant} \Rightarrow a = e^{\ln a}$$

$$\therefore y = (e^{\ln a})^x$$

$$= e^{(\ln a)(x)} \quad [\text{exponential property: } (b^n)^m = b^{n \cdot m}]$$

$$\frac{dy}{dx} = \frac{d}{dx} [e^{(\ln a)(x)}] = \frac{d}{dx} e^u \quad \text{where } u = (\ln a)(x)$$

$$= e^u \frac{du}{dx} \quad (5.3 (2), p.4)$$

$$= e^{(\ln a)(x)} \cdot \ln a \quad (u = (\ln a) \cdot x = \text{constant} \cdot x \Rightarrow u' = \text{constant} = \ln a)$$

$$= (e^{\ln a})^x \cdot \ln a$$

$$= a^x \ln a$$

$$(\because e^{\ln a} = a)$$

$$(d) \quad y = \alpha \cdot 10^{-x} + \beta 10^{-x^2}$$

$$y = u + v$$

$$y' = u' + v'$$

$$= \alpha \frac{d10^{-x}}{dx} + \beta \frac{d10^{-x^2}}{dx}$$

$$\because 10 \text{ is a constant} \Rightarrow \text{substitute} \quad 10 = e^{\ln 10}$$

$$\therefore y' = \alpha \frac{d}{dx} [e^{(\ln 10)(-x)}] + \beta \frac{d}{dx} [e^{(\ln 10)(-x^2)}]$$

$$= \alpha \frac{d}{dx} [e^a] + \beta \frac{d}{dx} [e^b] \quad \text{where } a = (\ln 10)(-x) \\ b = (\ln 10)(-x^2)$$

$$= \alpha e^a \frac{da}{dx} + \beta e^b \frac{db}{dx}$$

$$= \alpha (e^{\ln 10})^{-x} (-\ln 10) + \beta (e^{\ln 10})^{-x^2} (-2 \ln 10 x)$$

$$= -\ln 10 [\alpha 10^{-x} + 2\beta x 10^{-x^2}] \quad \text{remember } e^{\ln 10} = 10$$