

# DEMAND AND SUPPLY OF HEALTH INSURANCE

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EE 474 Health Economics

Semester 2/2021

# Topics

- What Is Insurance?
- Risk and Insurance
- ✓ • Demand for Insurance
- ✓ • Supply of Insurance
- ✓ • Moral Hazard
- Health Insurance and the Efficient Allocation of Resources
- The New Theory of Demand for Health Insurance

# Do You Have Any of these Insurances?

- Health insurance
- Car insurance
- House insurance
- Natural disaster insurance

# Example of An Insurance

- There are 100 students in the student union.
- Suppose that 1 out of 100 students *randomly* gets sick and incurs **health care costs of \$5,000**.
- Students worried about potential losses due to illness, so the student union decides to **collect \$50 from each student** and put the \$5,000 ( $\$50 \times 100$ ) in the bank.
- If a member becomes ill, the fund is used to pay for the treatment.
- Thus, the \$50 is paid to avoid the **risk** or **uncertainty of having to pay \$5,000 when ill**.

# Insurance Terminology (1)

- *Premium, Coverage*
  - Ex: Premium = \$50 (what the insured pays)
  - Ex: Coverage = \$5000 (what insurer pays out)
- *Coinsurance and Copayment*
  - **Coinsurance** is the *percentage* of loss paid by the insured when the loss occurs.
    - Ex: Suppose the coinsurance rate = 20% and the cost of health care is \$1000. So, the insured would have to pay \$200.
  - **Copayment** is the *fixed amount* paid by the insured when the loss occurs.
    - Often times, the copayment is fixed, regardless of the amount of loss.
- **Deductible** : Maximum amount the insured needs to pay out-of-pocket before the insurance policy starts.
  - Ex: The deductible is \$400.
    - If total loss = \$350, the insured pays the total amount.
    - If total loss = \$500, the insured pays \$400 and the insurer pays \$100.

# Insurance Terminology (2)

- *Exclusions* : Services or conditions not covered by the insurance policy
  - Ex: Cosmetic or experimental treatments.
- *Limitations*: Maximum coverage provided by insurance policies.
  - Ex: A policy may provide a maximum of \$3 million lifetime coverage.
- *Pre-Existing Conditions*: Medical problems not covered if the problems existed prior to issuance of insurance policy.
  - Ex: pregnancy, cancer, HIV/AIDS, chronic diseases
- *Loading Fees*: General costs associated with the insurance company doing business, such as sales, advertising, or profit.

# Insurance vs. Social Insurance

- In this lecture, we will talk about *private* health insurance.
- (Private) Insurance
  - Provided through markets
  - Buyers buy insurance to protect themselves against rare events with certain probabilities
- Social Insurance- Government is the insurer:
  - Premiums are heavily and often completely subsidized.
  - Participation is constrained according to some eligibility rules.

# Risk and Insurance: Expected Value

- **Expected value** is determined by summing the **values** of the various **outcomes** of an event times the **probabilities** that each outcome will occur.
- Example: the expected value (or expected return) of a coin toss game where you win \$1 if heads appears and \$0 if tails appears is:

$$\begin{aligned} \text{EV} &= \text{Prob}_{\text{heads}} * \$1 + \text{Prob}_{\text{tails}} * \$0 \\ &= 0.5 * \$1 + 0.5 * \$0 \quad (\text{assuming a fair coin}) \\ &= \$0.5 \end{aligned}$$

# Expected Value (In General)

- With  $n$  outcomes, expected value  $E$  is written as:

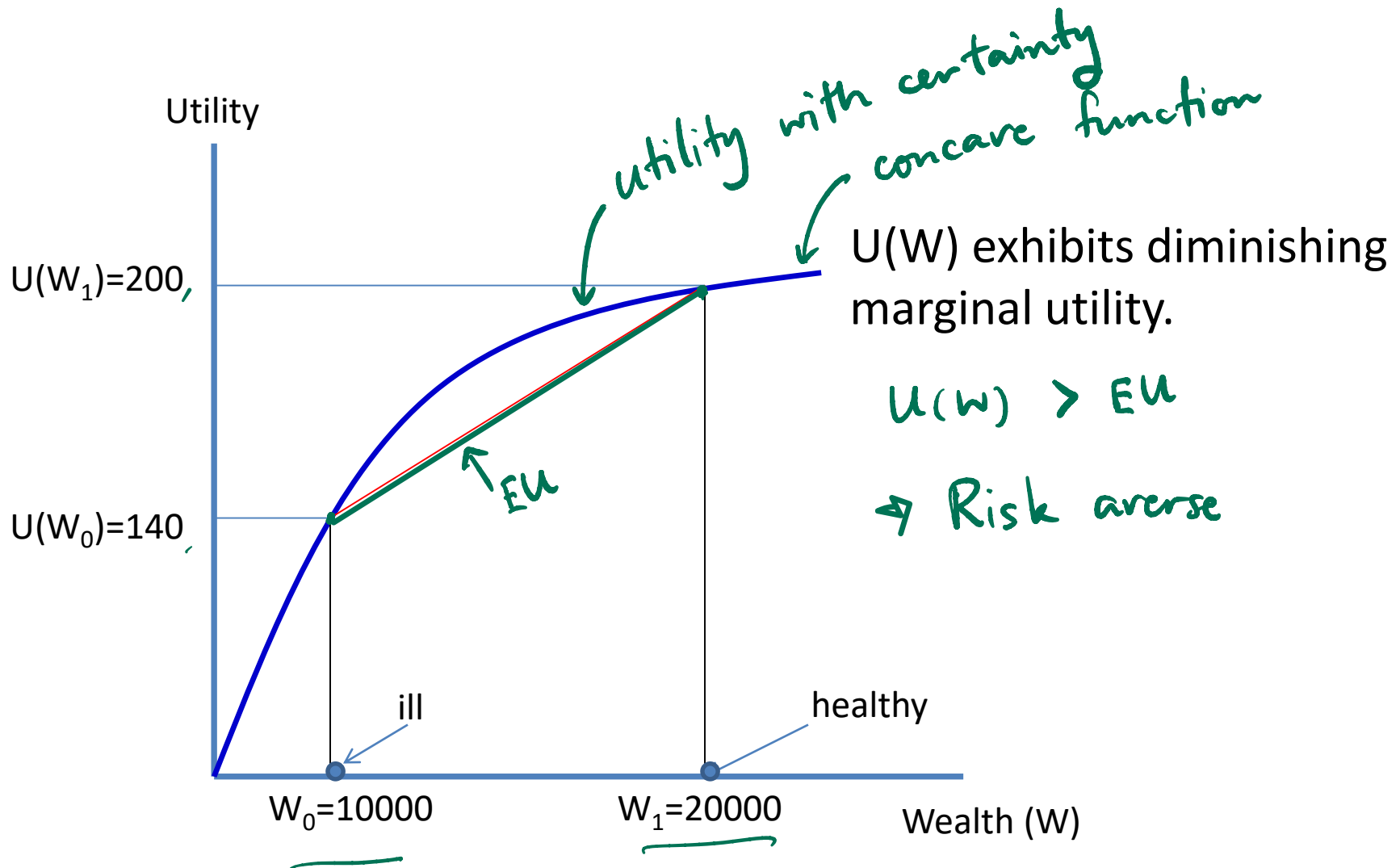
$$E = p_1 R_1 + p_2 R_2 + \dots + p_n R_n$$

- $p_i$  is the probability of outcome  $i$ , ( $i= 1, 2, \dots, n$ )
  - $R_i$  is the return if outcome  $i$  occurs.
  - The sum of the probabilities  $p_i$  equals 1.
- **St.Petersburg's paradox:** How much would you pay to play coin toss game where you win \$1 if H, \$2 if TH, \$4 if TTH, \$8 if TTTH, etc.?  
→  $EV = (1/2)*\$1 + (1/4)*\$2 + (1/8)*\$4 + (1/16)*\$8 + \dots$   
 $= 0.5 + 0.5 + 0.5 + 0.5 + \dots = \infty$

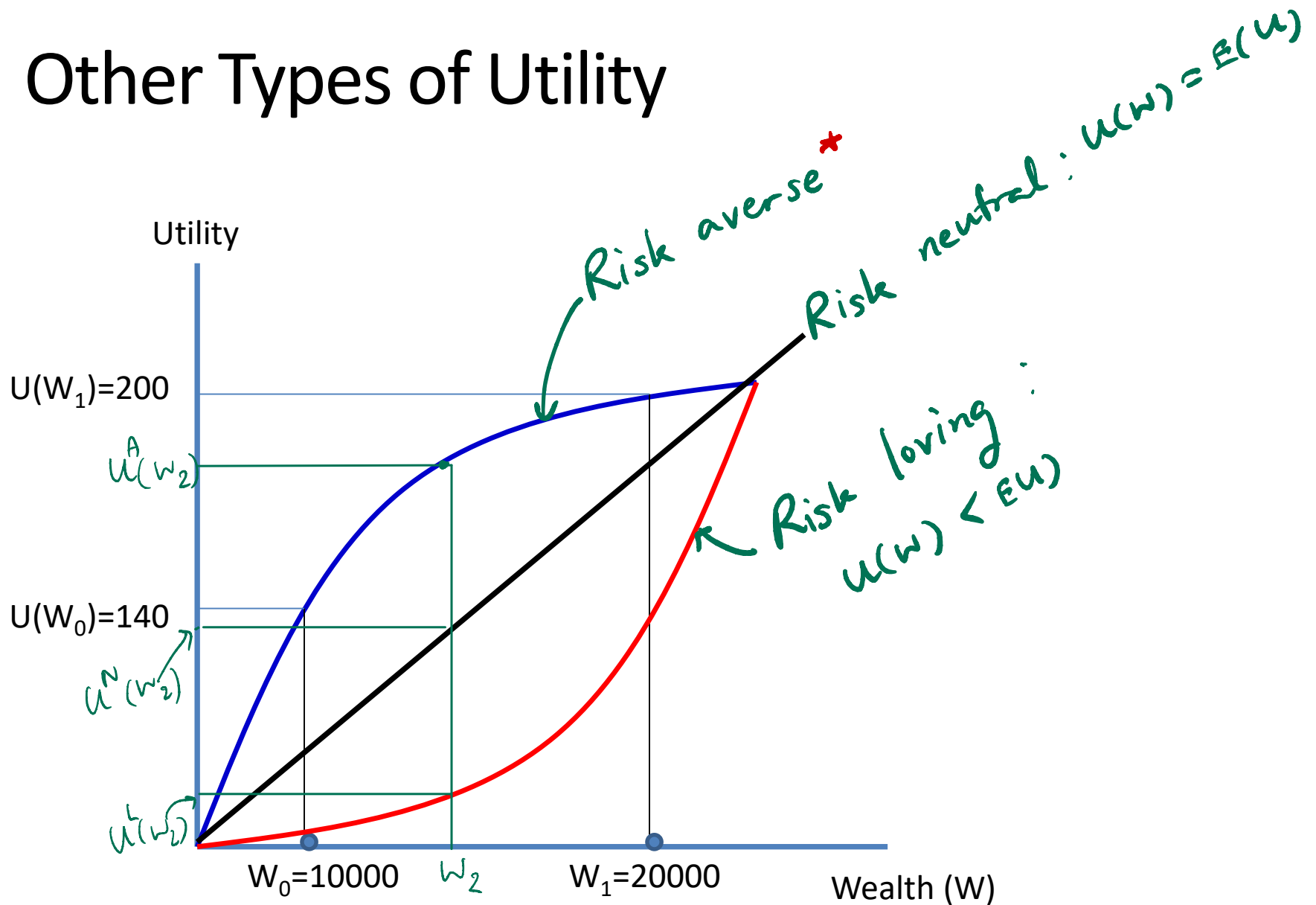
# Marginal Utility of Wealth and Risk Aversion

- Bernoulli's solution was that *money has a different value or utility* depending on *how much you have*.
  - From the previous example, if the coin flip yields \$100 or nothing, and you now asked to pay \$50 to play. Would you still want to play?
    - Perhaps not, why?
    - The utility of an extra \$ is worth more if you have less money than the utility of an extra \$ is worth when you have more money.
- *Diminishing marginal utility*

# Utility of Wealth



# Other Types of Utility



# Expected Wealth and Expected Utility if

**Uninsured**  $W_H = \$20,000$  ,  $W_I = \$20,000 - \$10,000 = \$10,000$  ;  $U(W_H) = 200$  ;  $U(W_I) = 140$

- Suppose the probability of being ill is **0.1** (probability of being healthy = 0.9), and the illness incurs a \$10,000 expense.
- **Expected value of wealth:**

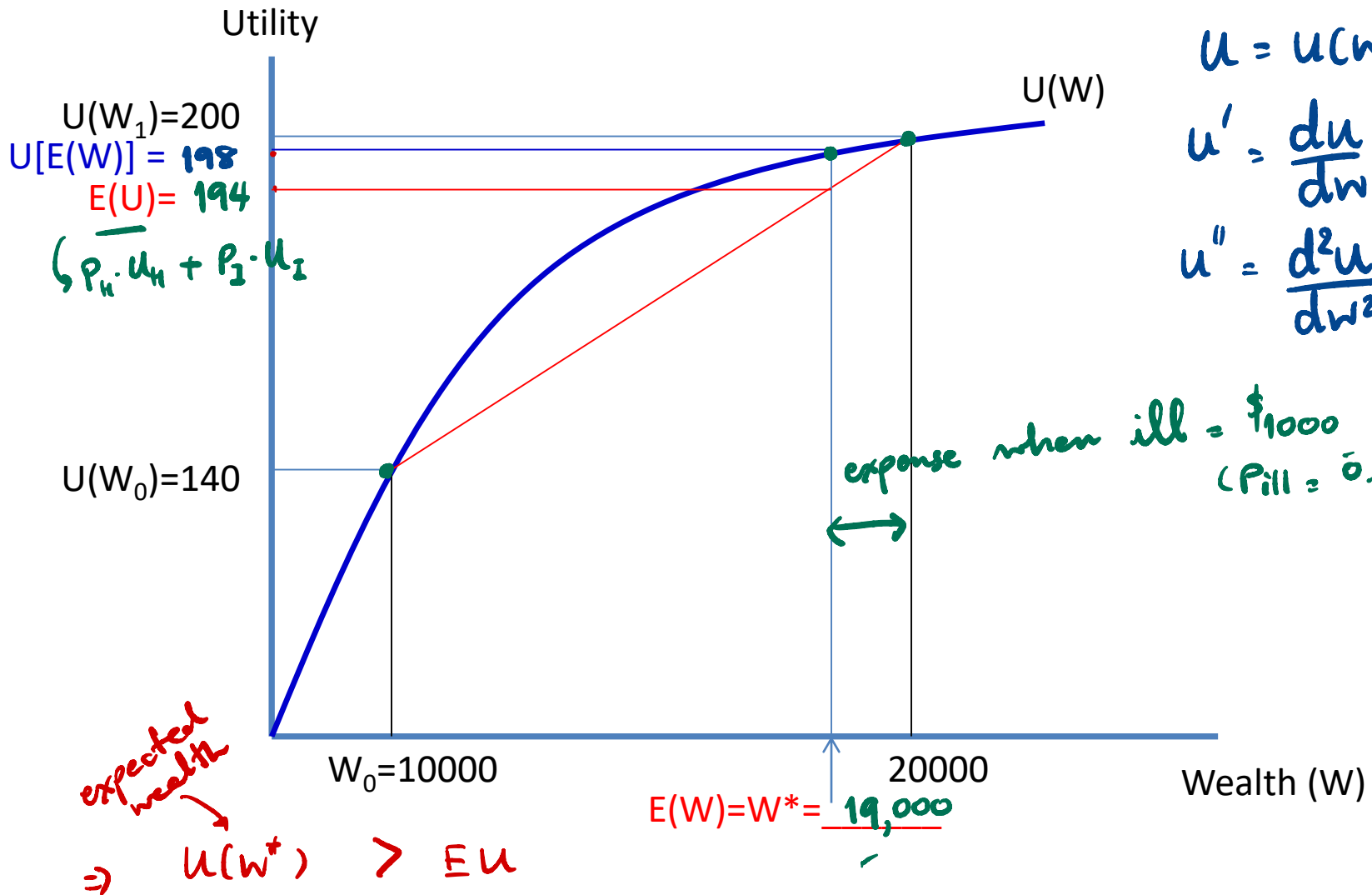
$$\begin{aligned} E(W^{\text{uninsured}}) &= (\text{Prob}_{\text{healthy}} * W_{\text{healthy}}) + (\text{Prob}_{\text{ill}} * W_{\text{ill}}) \\ &= (0.9 * 20,000) + (0.1 * 10,000) \\ \bar{W} = E(W) &= 18,000 + 1,000 = \$19,000 \end{aligned}$$

- **Expected utility of wealth:**

$$\begin{aligned} E(U^{\text{uninsured}}) &= (\text{Prob}_{\text{healthy}} * U_{\text{healthy}}) + (\text{Prob}_{\text{ill}} * U_{\text{ill}}) \\ &= (0.9 * 200) + (0.1 * 140) \\ &= 180 + 14 \\ E(U) &= 194 \text{ utils} \end{aligned}$$

# Expected Utility if Uninsured

Given info,  $U = 198$  when wealth is \$19,000. ✓





# Expected Utility if Insured

pays AFP whether ill or healthy

## • Wealth when insured:

✓ • If healthy:  $W_{\text{healthy}} = W_1 - \overset{\text{AFP}}{(W_1 - W^*)} = W^*$

➤  $W_{\text{healthy}} = \underline{20,000} - 1,000 = \underline{\$19,000}$

• If ill:  $W_{\text{ill}} = \underline{W_1} - \overset{\text{loss due to illness}}{(W_1 - W_0)} - \overset{\text{AFP}}{(W_1 - W^*)} + \overset{\text{coverage}}{(W_1 - W_0)} = W^*$

➤  $W_{\text{ill}} = \underline{20,000} - \cancel{10,000} - 1,000 + \cancel{10,000} = \underline{\$19,000}$

## • Expected value of wealth if insured:

$$E(W^{\text{insured}}) = (\text{Prob}_{\text{healthy}} \overset{19,000}{*} W^*) + (\text{Prob}_{\text{ill}} \overset{19,000}{*} W^*) = W^* = \underline{19,000}$$

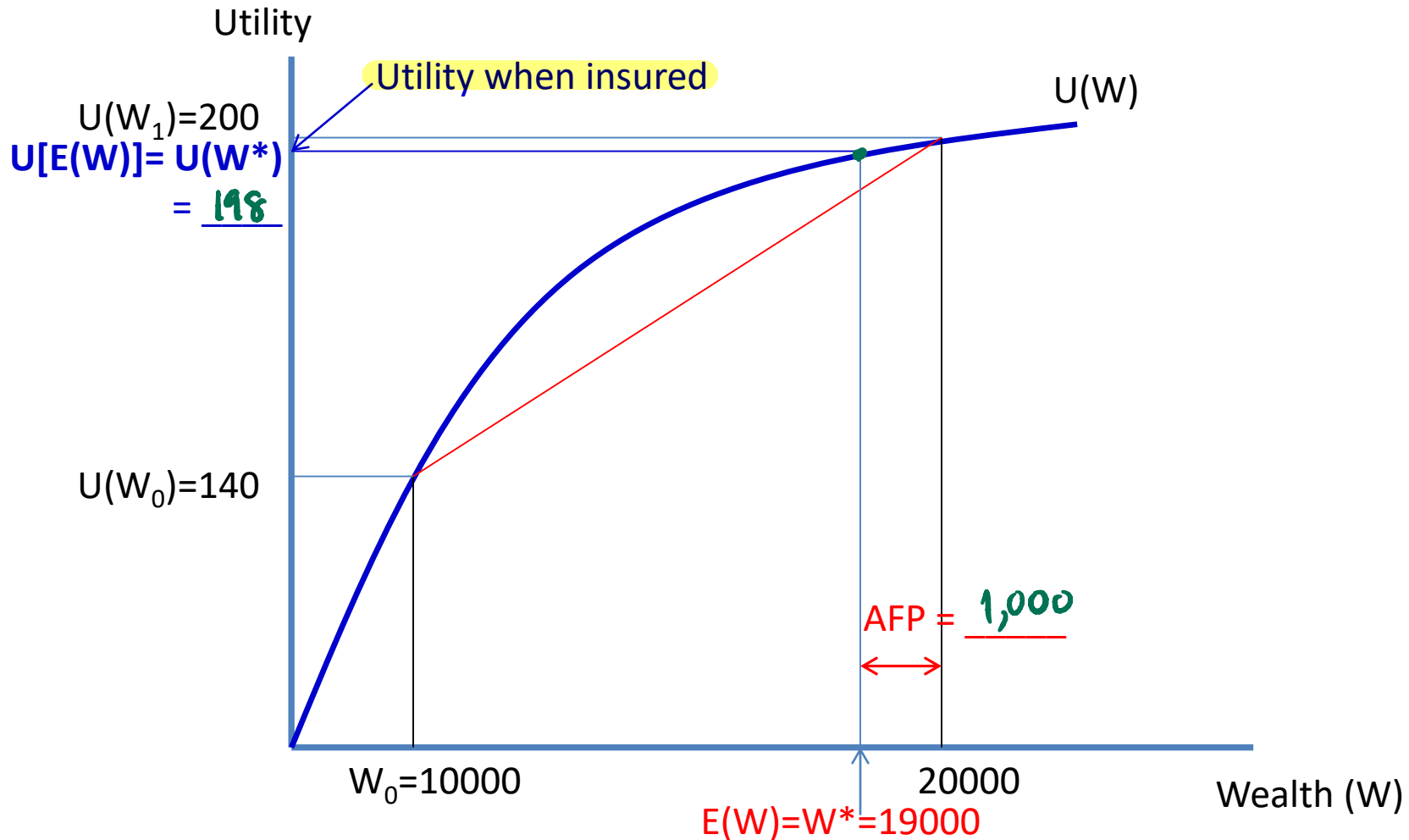
## • Expected utility if insured:

$$E(U^{\text{insured}}) = (\text{Prob}_{\text{healthy}} \overset{u(19,000)}{*} U(W^*)) + (\text{Prob}_{\text{ill}} \overset{u(19,000)}{*} U(W^*)) = \underline{198 = u(W^*)}$$

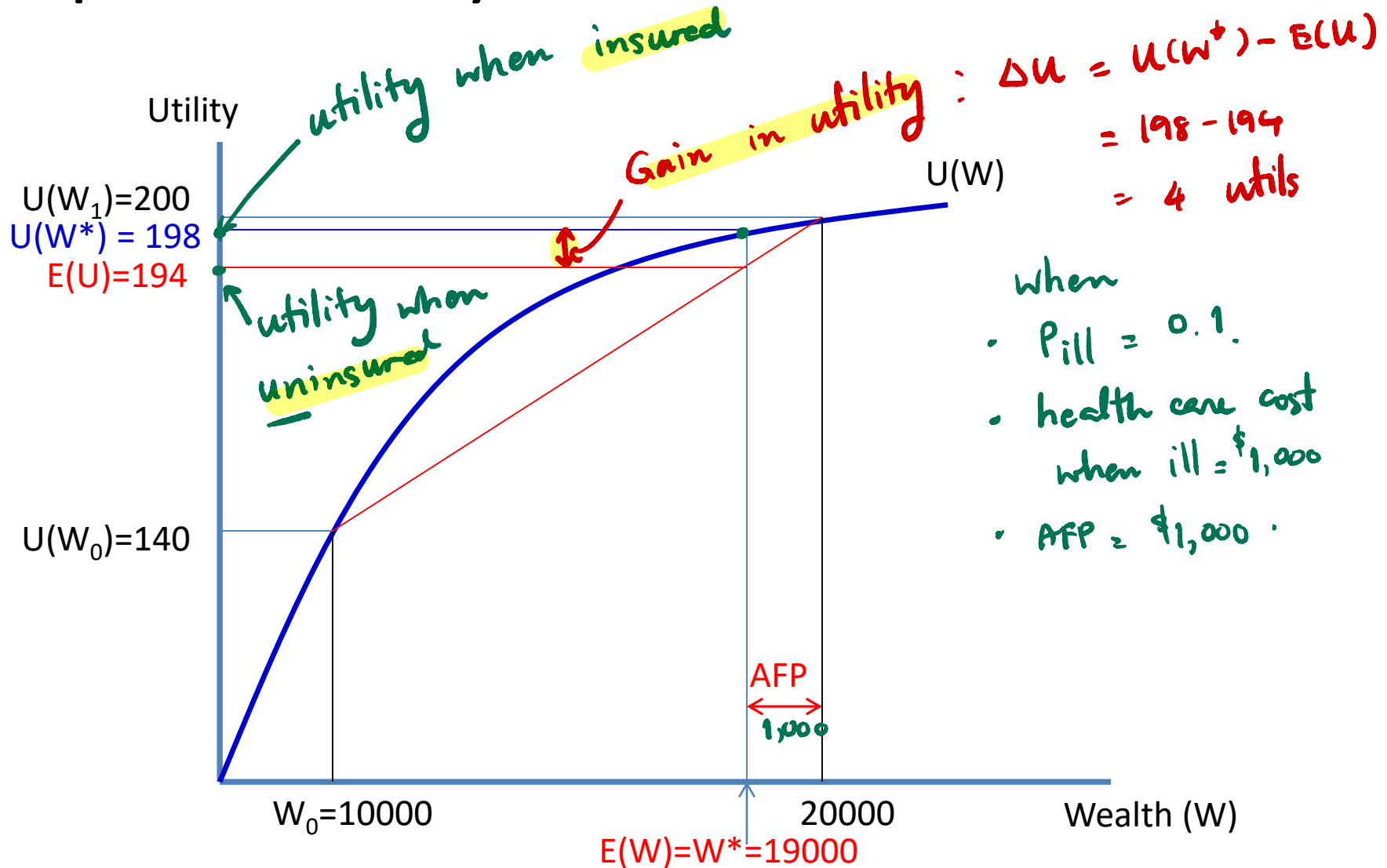
➤ Expected utility if insured is certain!

➔  $EU^{\text{insured}} = u[E(W)] = u(W^*)$

Expected Utility if **Insured** :  $E(U^{\text{insured}}) = U(W^*)$   
 Uninsured :  $E(U^{\text{uninsured}}) < U(W^*)$



# Expected Utility if Insured and Uninsured



# Expected Utility if Insured and Uninsured

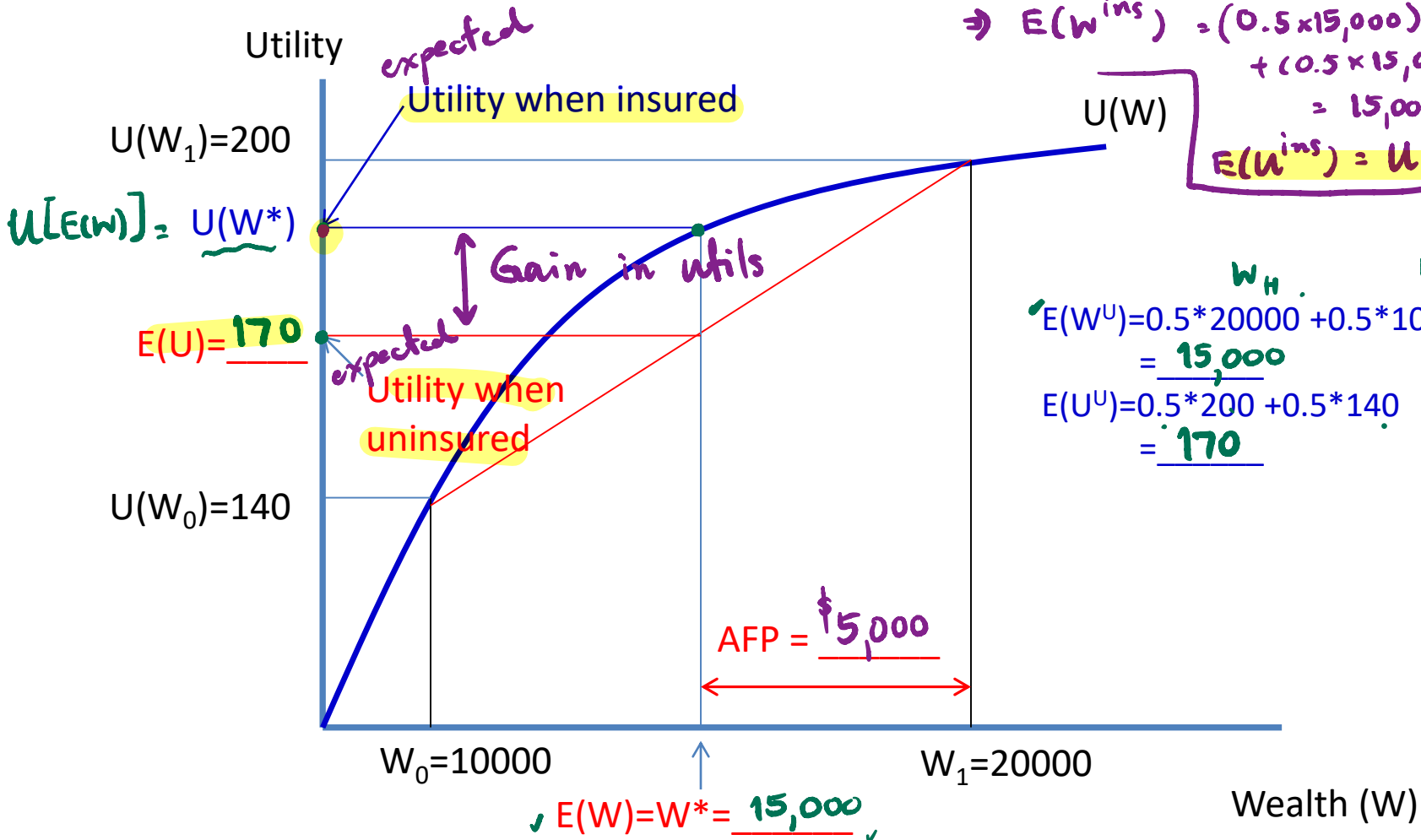
(when  $P_{ill}=0.5$ )

Given  $W_H = 20,000$ ,  $W_I = 10,000$

When insured,  $AFP = 0.5 \times 10,000 = \$5,000$

$$\Rightarrow E(W^{ins}) = (0.5 \times 15,000) + (0.5 \times 15,000) = 15,000$$

$$E(U^{ins}) = U(W^*)$$



$$E(W^U) = 0.5 \cdot W_H + 0.5 \cdot W_I = 0.5 \cdot 20000 + 0.5 \cdot 10000 = 15,000$$

$$E(U^U) = 0.5 \cdot 200 + 0.5 \cdot 140 = 170$$

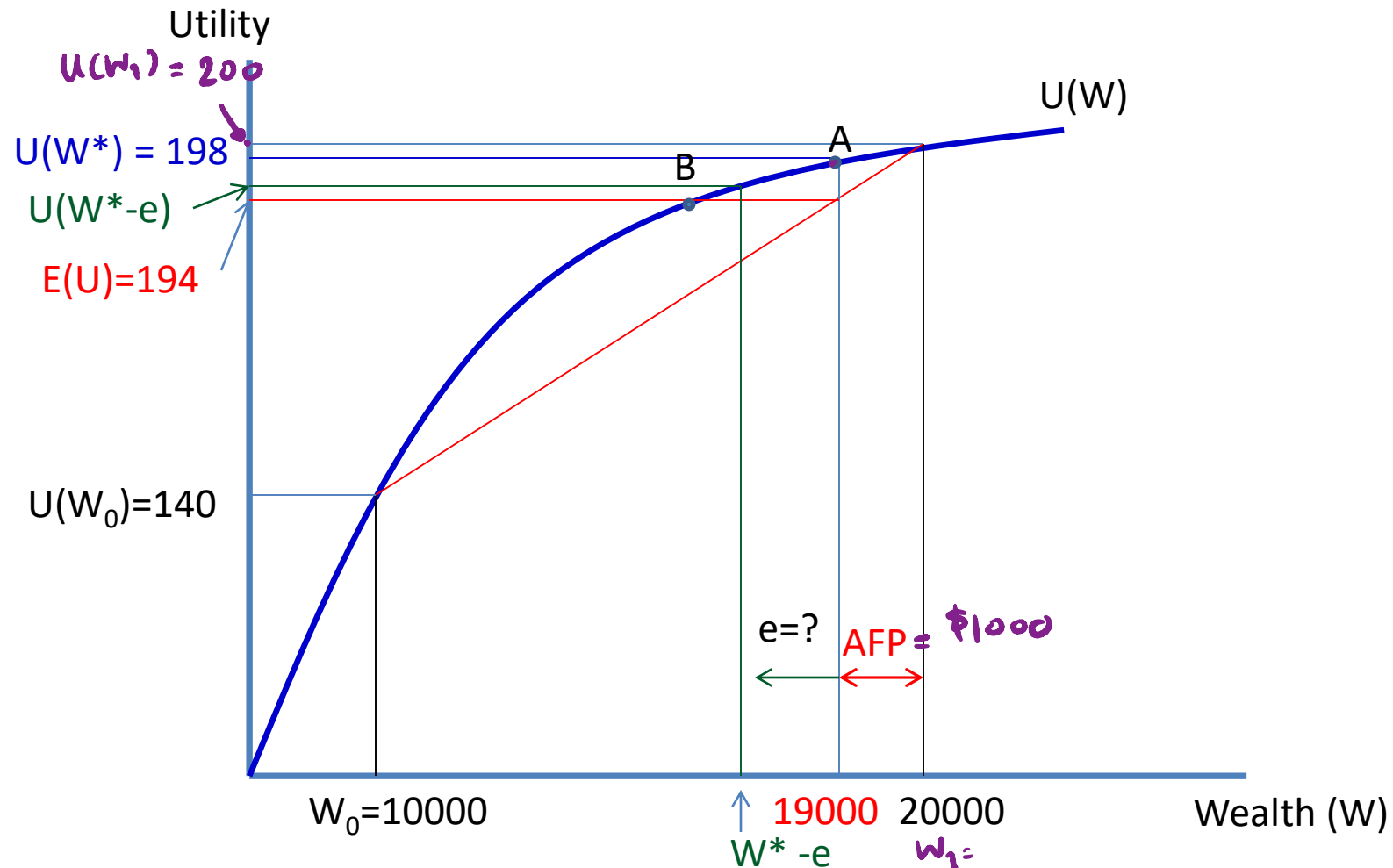
# Gain from Insurance in Utility

- If insured,  $EU^{\text{ins}} = U(W^*)$ , and if uninsured,  $EU^{\text{unins}} = E(U^{\text{unins}}) < U(W^*)$ 
  - Gain from insurance is  $U(W^*) - E(U^{\text{unins}})$  in utility terms
  - In our example, gain from insurance =  $\underline{198 - 194 = 4}$  utils.
- Conventional theory of the demand for health insurance :
  - Insurance is a choice between certainty and uncertainty (Friedman and Savage, JPE, 1948)
  - Consumers buy insurance because they prefer certain loss (the premium) to uncertain loss (medical care expenses if ill) of the same expected magnitude.
    - Consumers are risk averse.
- “Preference for certainty” ~ “risk avoidance”

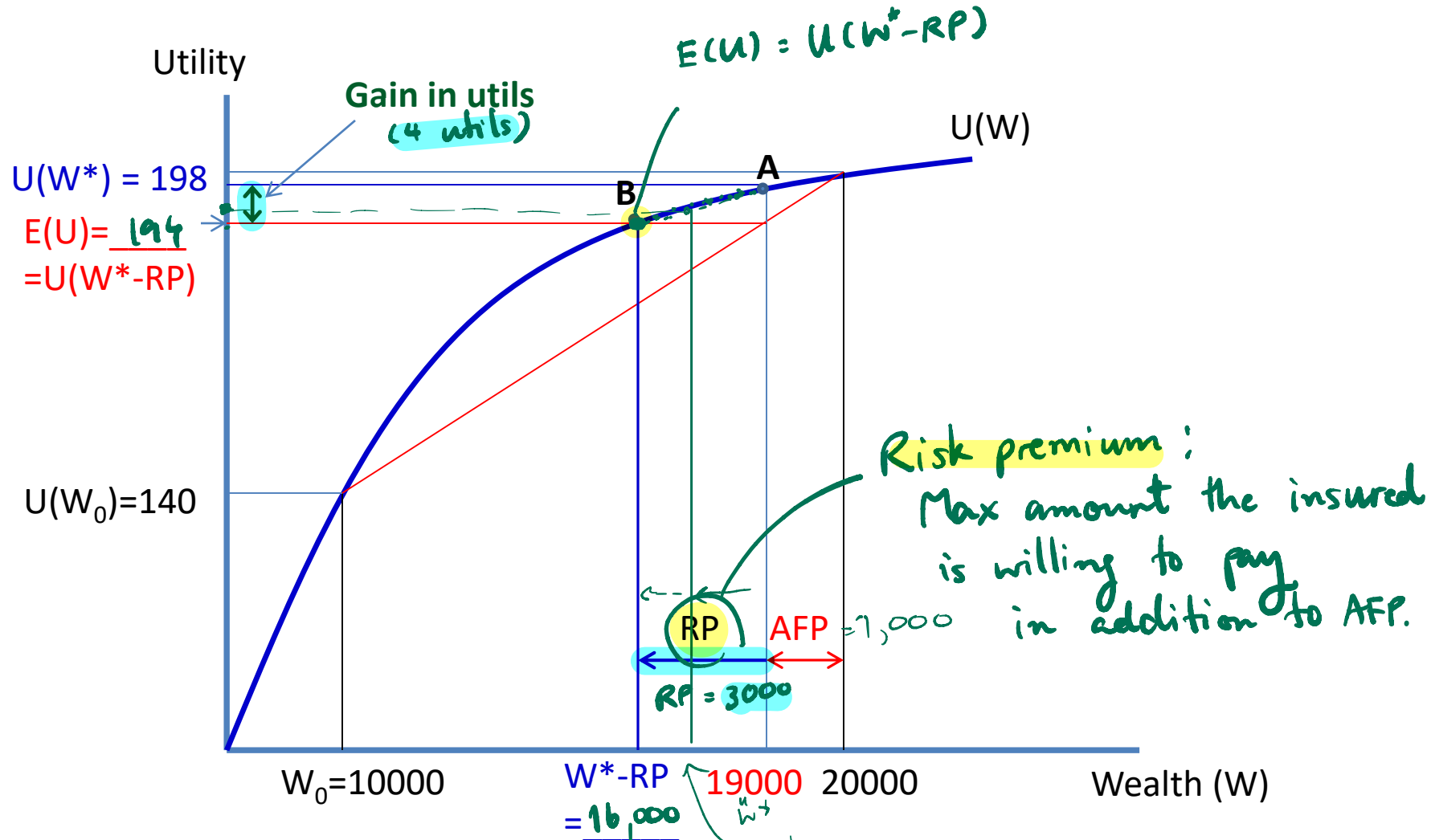
# Gain from Insurance in Dollars

- The gain from EU to  $U(W^*)$  is in utility terms.
- What about the gain in *dollar* terms?
  - We know that AFP is the amount the consumer would expect to pay with or without insurance.
  - What is the maximum amount that the consumer would be willing to pay for insurance (i.e. how much more than the AFP)?
  - The additional amount the consumer would be willing to pay is the value of insurance.

# Gain from Insurance in Dollars $(P_{ill} = 0.1)$



# Gain from Insurance in Dollars



**Risk premium:**  
 Max amount the insured is willing to pay in addition to AFP.

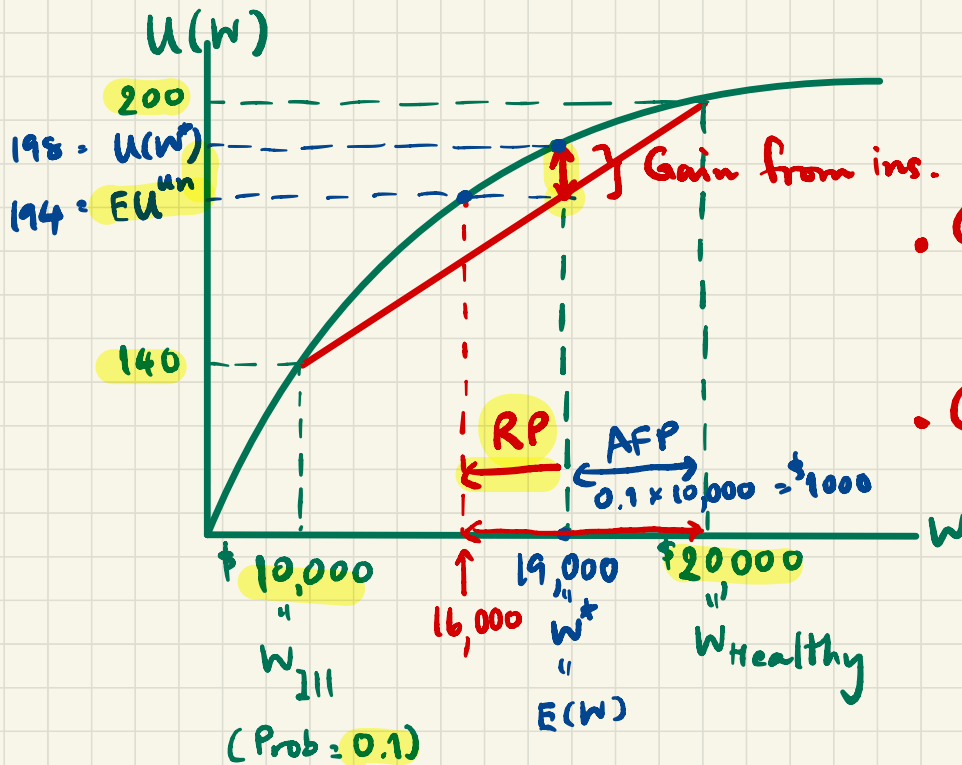
Suppose  $U = 194$  when  $w = 16,000$

# Value of Insurance

- The **risk premium (RP)** is the maximum amount over and above the AFP that the consumer would be willing to pay for insurance.  $(b/c U(W^*) \geq EU)$
- If the consumer pays **AFP + RP** for insurance, he would be *indifferent* to being insured or uninsured.  $(Point B)$
- The **welfare gain** from **risk avoidance** is measured in dollars by the **risk premium** and represents the value of the **welfare gain** from being insured.
  - Example: The consumer would be willing to pay up to \$4,000. Thus, the welfare gain is equal to \$4000-\$1000 = \$3000.
  - Note: 4,000= 20,000-16,000, where 16,000 is wealth associated with  $U(W)=194$ .

# Part II : Health Insurance

## Review : Gain from Insurance



## ✓ Optimal Level of Health Insurance

- Demand for health insurance ✓
- Supply of health insurance ✓

# Demand for Insurance

gain from coverage.

paying premium.

- Apply the concepts of marginal benefits (MB) and marginal costs (MC) to determine health insurance choice.

$$w_H = \$20,000, \quad w_I = \$10,000$$

- Suppose that the insurance coverage = \$500, and the consumer must pay a 20% premium ( $20\% * 500 = \$100$ ).

✓ • New wealth when ill:  $W_I' = \underbrace{20,000}_{\text{HC cost}} - \underbrace{10,000}_{\text{premium}} - \underbrace{100}_{\text{coverage}} + \underbrace{500}_{\text{coverage}} = 10,400$   $\Delta W_{\text{ill}} = +400$   
 $\downarrow$   
 $MB_{500}$

✓ • New wealth when healthy:  $W_H' = \underbrace{20,000}_{\text{premium}} - \underbrace{100}_{\text{premium}} = 19,900$

➤  $MB_{500} = E[MU_{400}]$

➤  $MC_{500} = E[MU_{100}]$

$MB_{500} > MC_{500}$

$\Delta W_H = -100$   
 $\downarrow$   
 $MC_{500}$

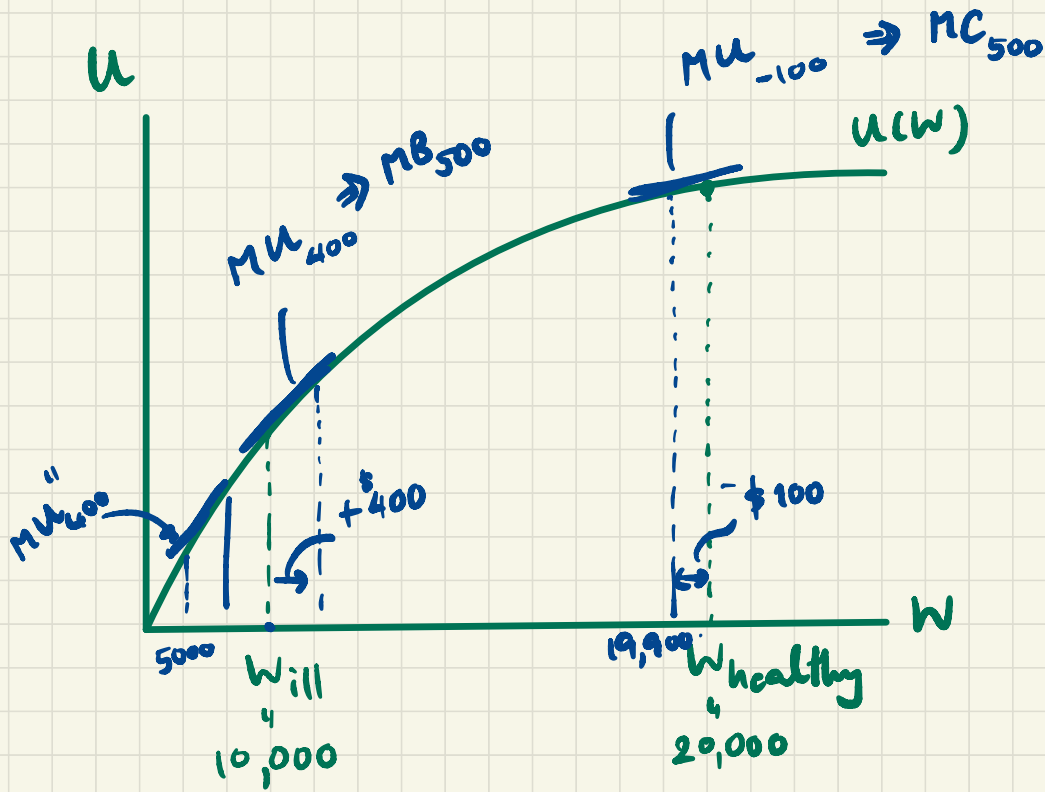
- If purchase an additional \$500 insurance, then:

➤  $MB_{1000} < MB_{500}$

➤  $MC_{1000} > MC_{500}$

b/c of diminishing marginal utility of wealth

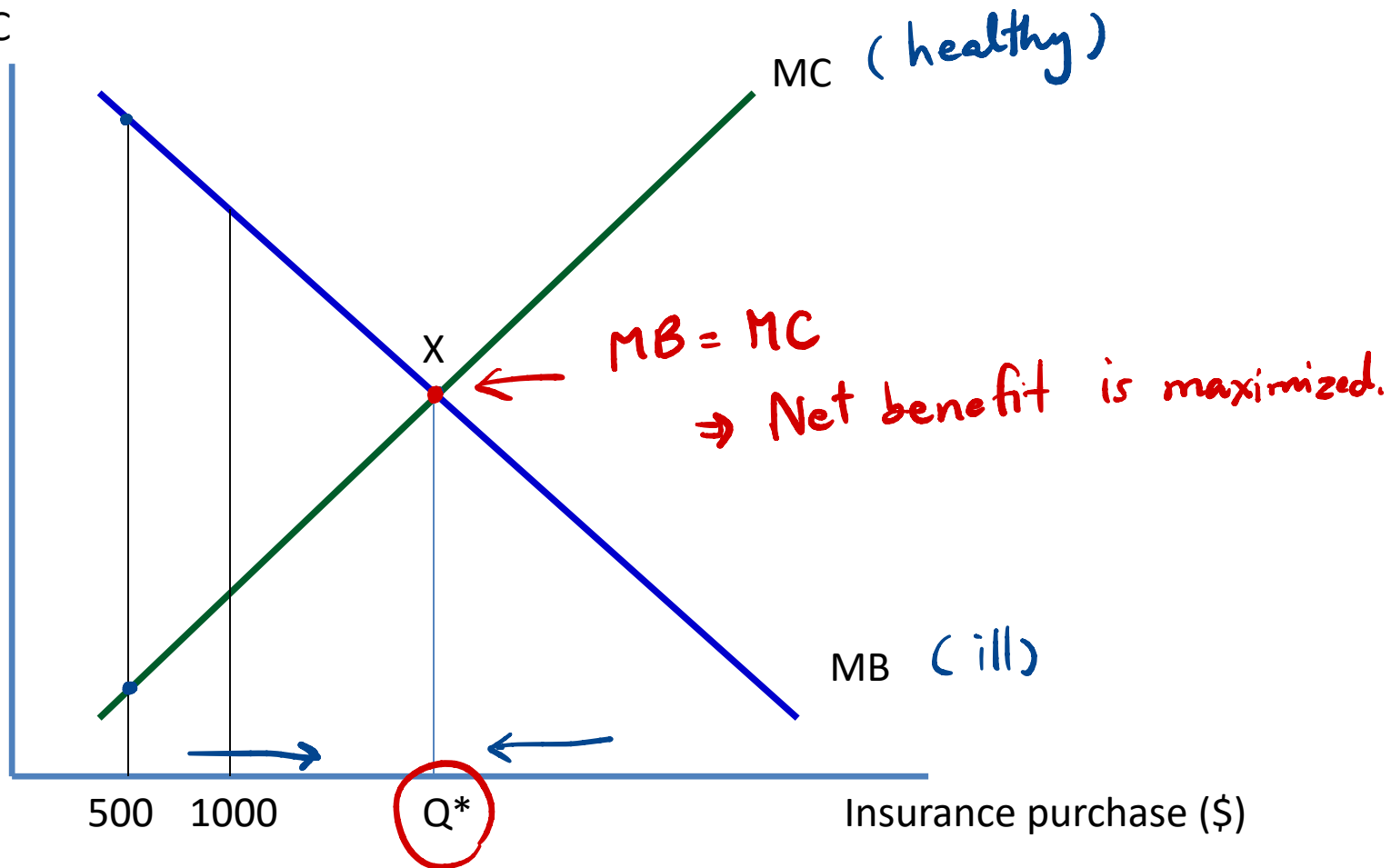
Buy more HI as long as  $MB > MC$ !



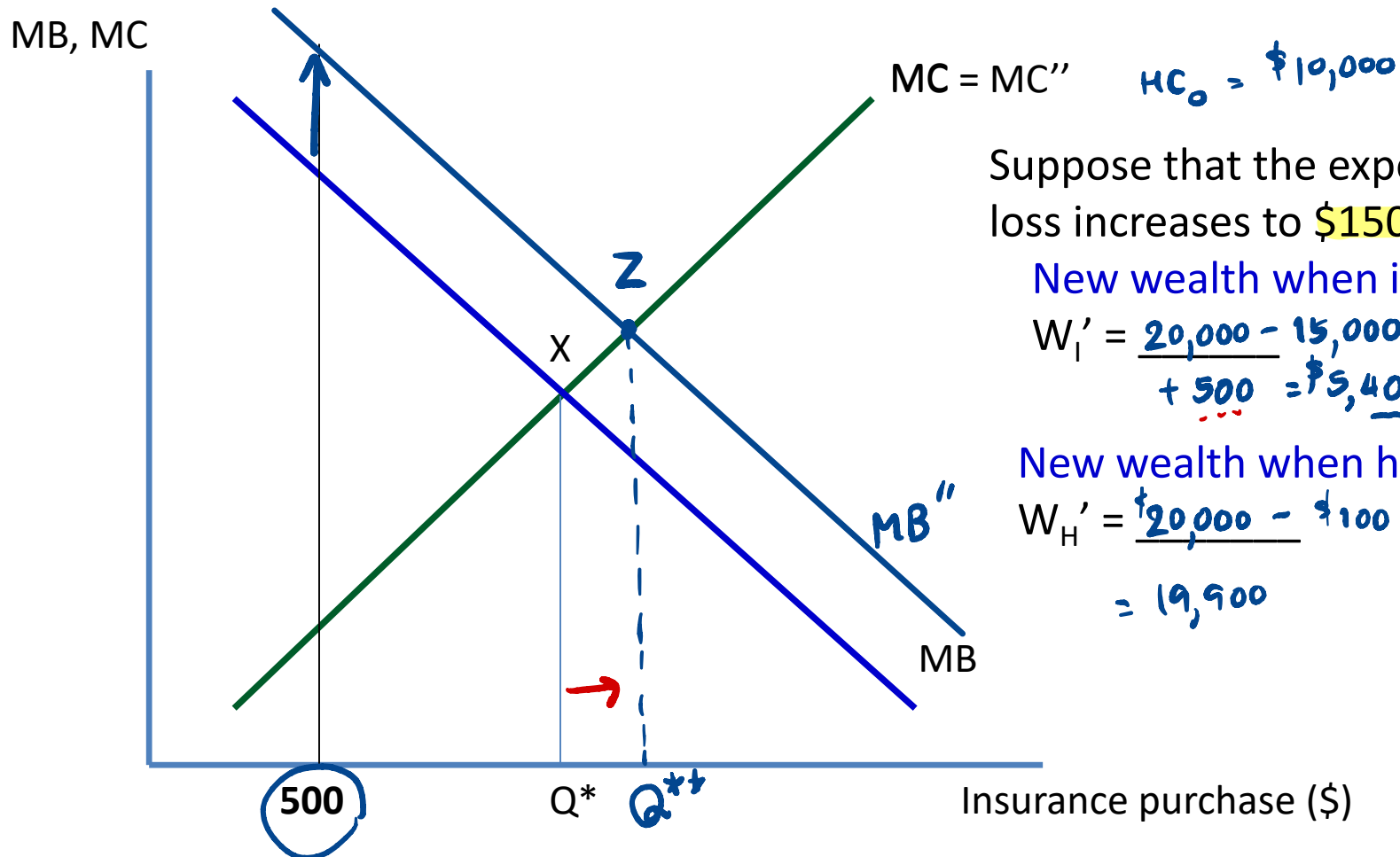
$\Rightarrow MB_{500} > MC_{500} \Rightarrow$  should buy HI.

# Optimal Amount of Insurance

MB, MC



# Optimal Amount of Insurance: Expected Loss Increases



# Supply of Insurance

- Insurer's profit:  $\text{Profit} = \text{Total Revenue} - \text{Total Cost}$
- Previous example:
  - Revenues = \$100 per policy (20% <sup>20% x \$500</sup>)
  - Costs:
    - Insurance coverage = \$500 (with Prob = 0.1)
    - Processing cost (a.k.a. loading fee) = \$8
  - For insured who *do not get sick* (Prob = 0.9), the insurer's cost is \$8.
  - For insured who *do get sick* (Prob = 0.1), the insurer's cost is \$500 + \$8 = \$508.
- Insurer's profit = \$100 -  $\underbrace{[(0.9 \cdot 8) + (0.1 \cdot 508)]}_{\text{expected cost}} = \underline{\$42} > 0$  <sup>+ve  $\pi$ .</sup>

# Role of Competition in Insurance Market

- Since there are positive profits (\$42), other firms have incentive to enter the market and offer a lower premium (e.g. 15% = \$75).  $0.15 \times \$500 = \$75$ 
  - Profit =  $\underline{\$75} - [(0.9 \times 8) + (0.1 \times 508)] = \$17 > 0$
- Eventually, the entry into the market would continue until excess profit is driven away, i.e. profit=0 (perfect competition condition).
  - What is the premium rate under perfect competition?
  - Try premium rate = 11.6% !

# Competitive Premium

- Let  $a$  = premium rate,  $q$  = amount of payout (coverage),  $t$  = processing cost, and  $p$  = probability of payout.

➤  $Profit = aq - pq - t$

- Under perfect competition:  $Profit = aq - pq - t = 0$

$$a = \frac{t}{q} + p$$

$$aq = t + pq$$

$$a = \frac{t}{q} + p$$

- When  $t=0$ , the premium is the actuarially fair rate

→  $a = p$ .

eg.  $p = 10\%$  (Prob of ill) ⇒ AFP rate = 10%.

- Example:  $p = 0.1$ ,  $t = 8$ ,  $q = 500$

→  $a^* = \left(\frac{8}{500}\right) + 0.1 = 0.116$  (11.6%)

# Optimal Level of Coverage

$t = 0$

- Suppose no loading costs and the insurance market is perfectly competitive.
- To **maximize utility**, the consumer will choose the coverage level that equates her **expected wealth when healthy** to her **expected wealth when ill**.
- Same example ( $P_{ill} = 0.1$ , loss = 10,000):

- $W_{healthy} = \$20,000 - (a * q)$

- $W_{ill} = \$20,000 - \$10,000 - (a * q) + q$

→  $q^* = \underline{\$10,000}$

$$W_H = W_{ill}$$

$$20,000 - aq = 10,000 - aq + q$$

$$q^* = 10,000$$

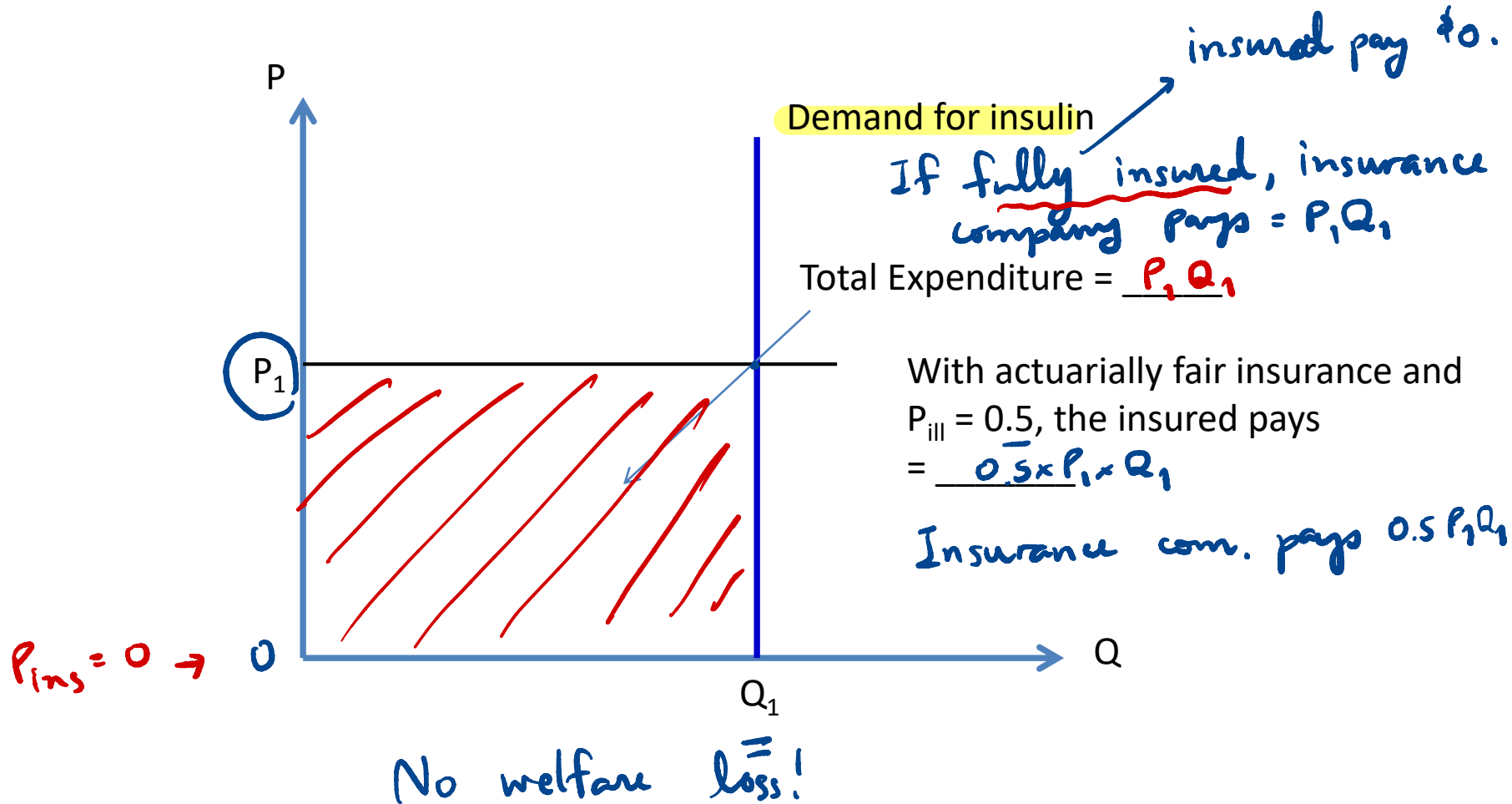
premium ← coverage

- Optimal coverage is equal to the health care cost (in the absence of loading fees).
- Not necessarily the case!

# What is Moral Hazard?

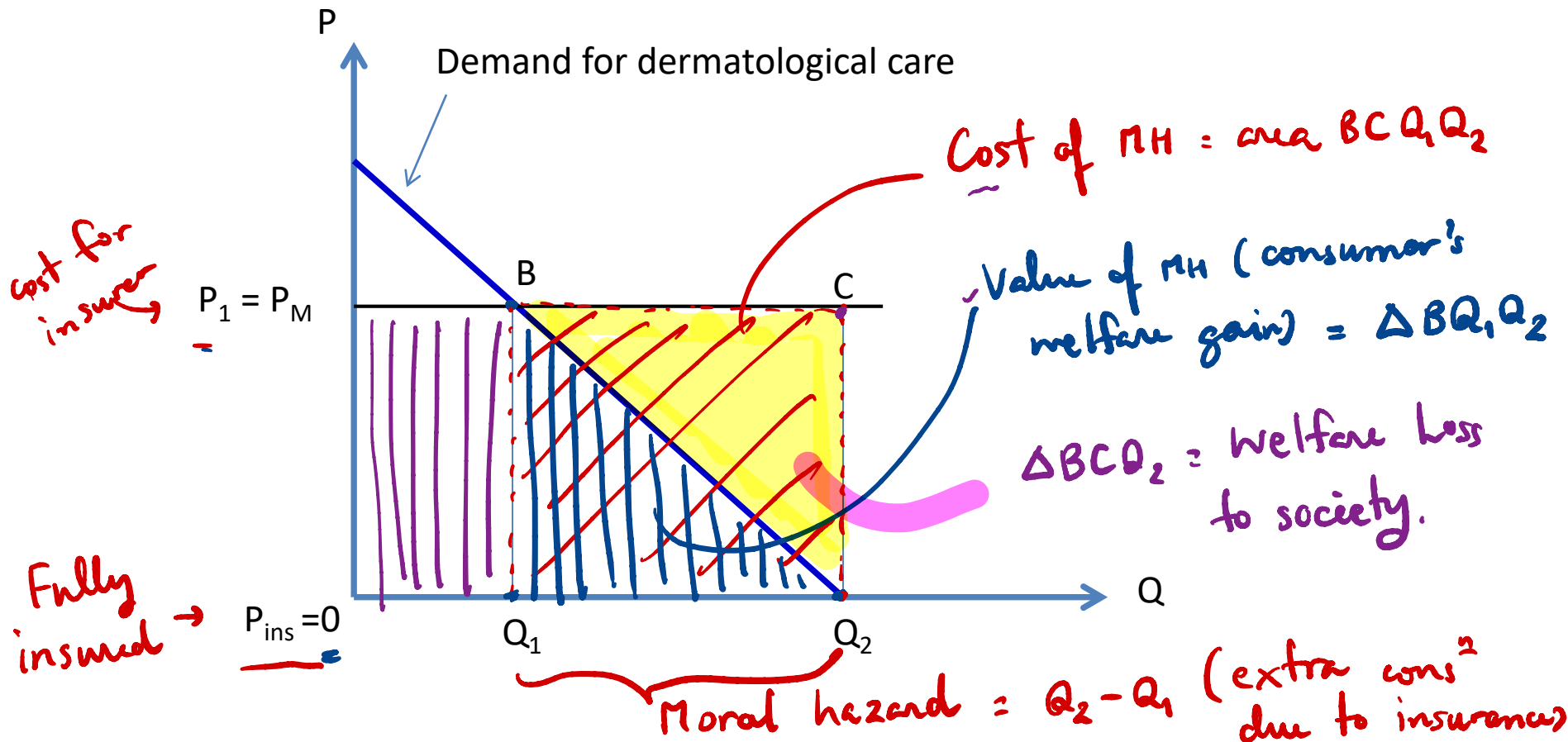
- **Moral hazard** is the change in behavior that is associated with becoming insured
- \* • **Ex post moral hazard** refers to the change in behavior *after* you become ill  
*excessive health care use*
  - An increase in health care consumption by the insured consumers
- **Ex ante moral hazard** refers to the change in behavior *before* you become ill → *less careful*.
  - An increase in the probability of illness of the insured consumers because they have fewer incentives to take care of themselves.

# Demand for Care and Moral Hazard (Perfectly Inelastic Demand)



# Demand for Care and Moral Hazard (Relatively Elastic Demand) $\Delta$ Full Insurance.

$$\rightarrow P_{\text{cons}} = 0$$



# Predictions on the Types of Health Insurance

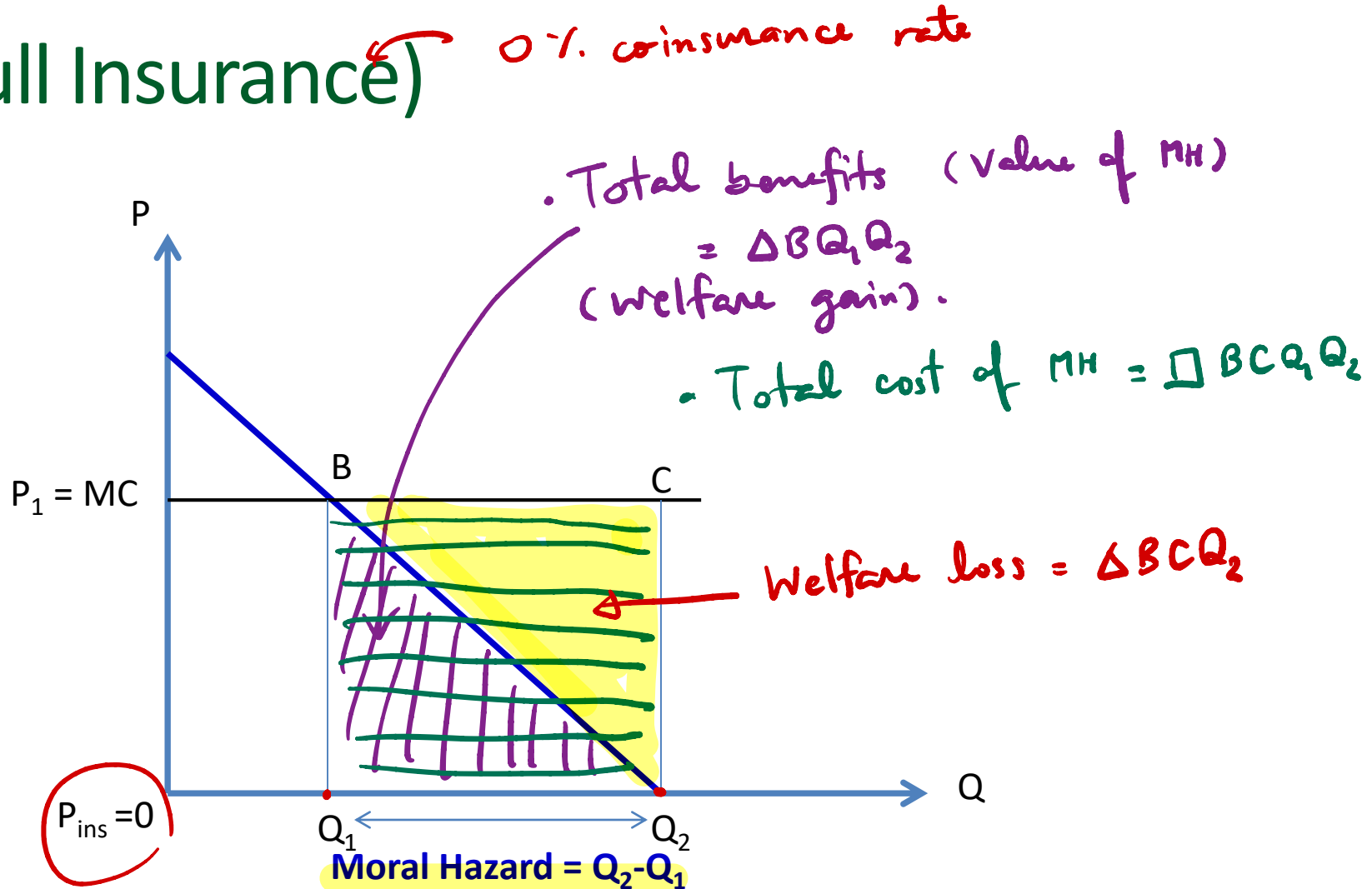
- ✓ • More inelastic demand health care services
  - ➔ ➤ More complete coverage
- ✓ • More elastic demand health care services
  - ➔ ➤ Less complete coverage or no insurance
- To reduce moral hazard, insurance companies use the following policies:
  - Deductibles
  - Coinsurance

# Efficient Allocation of Resources

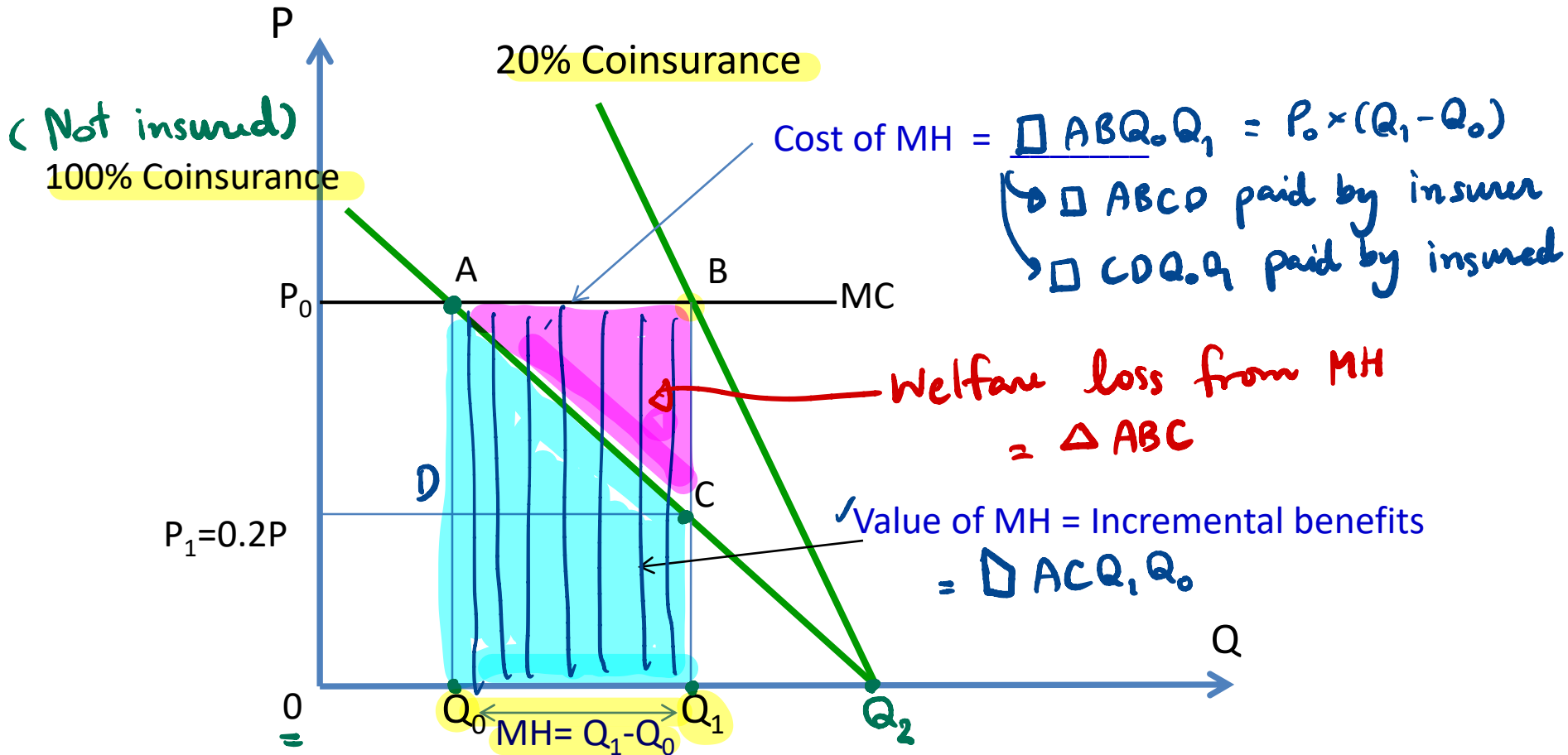
- The **efficient allocation** of society's scarce resources occurs when **marginal cost (MC) equals marginal benefits (MB)**.
  - **MC** = The incremental cost of bringing the resources to market
  - **MB** = The valuation to those who buy the resources
- If  $MB \neq MC$ , society's welfare could be improved by re-allocating resources.
  - If  $MB > MC$ , allocate more resource to the individual or sector and less resources to others.
  - If  $MB < MC$ , allocate less resource to the individual or sector more resources to others.
- **Moral hazard** induced by health insurance can lead to inefficient allocation of resources.
  - $MC > MB \rightarrow$  Welfare loss to society

insurer  
↓  
insured

# Moral Hazard and Welfare Loss (Full Insurance)



# Moral Hazard and Welfare Loss (20% Co-insurance)



# Two-tiers Insurance

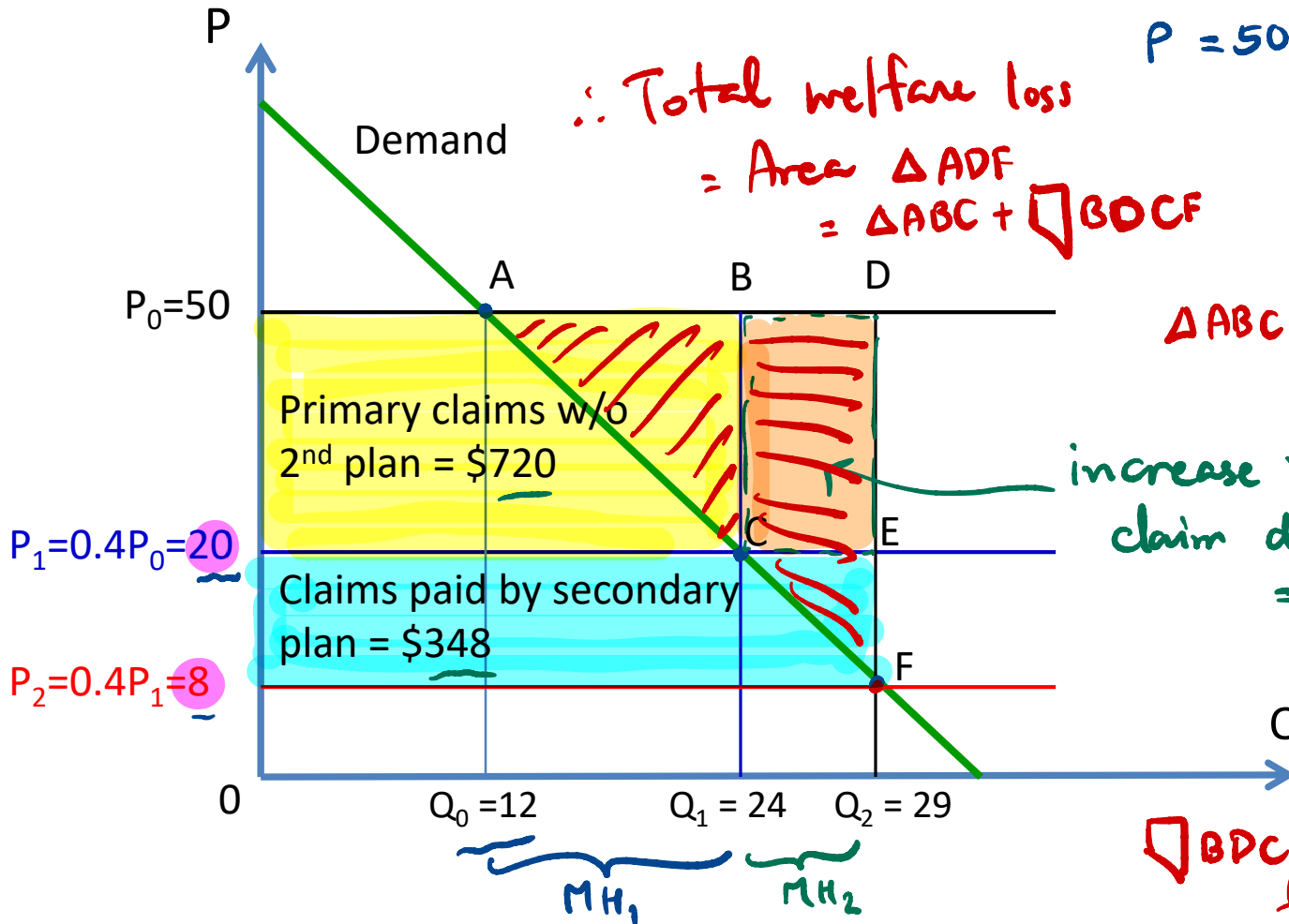
(Primary Plan – 60% of total cost & Secondary plan – 60% of the rest)

↳ coins rate = 40%.

↳ coins rate = 40%.

$P = 50 \rightarrow 1^{st}: P_1^C = 0.4 \times 50 = \$20$   
 $\rightarrow 2^{nd}: P_2^C = 0.4 \times 20 = \$8$

∴ Total welfare loss  
 = Area  $\Delta ADF$   
 =  $\Delta ABC + \square BOCF$

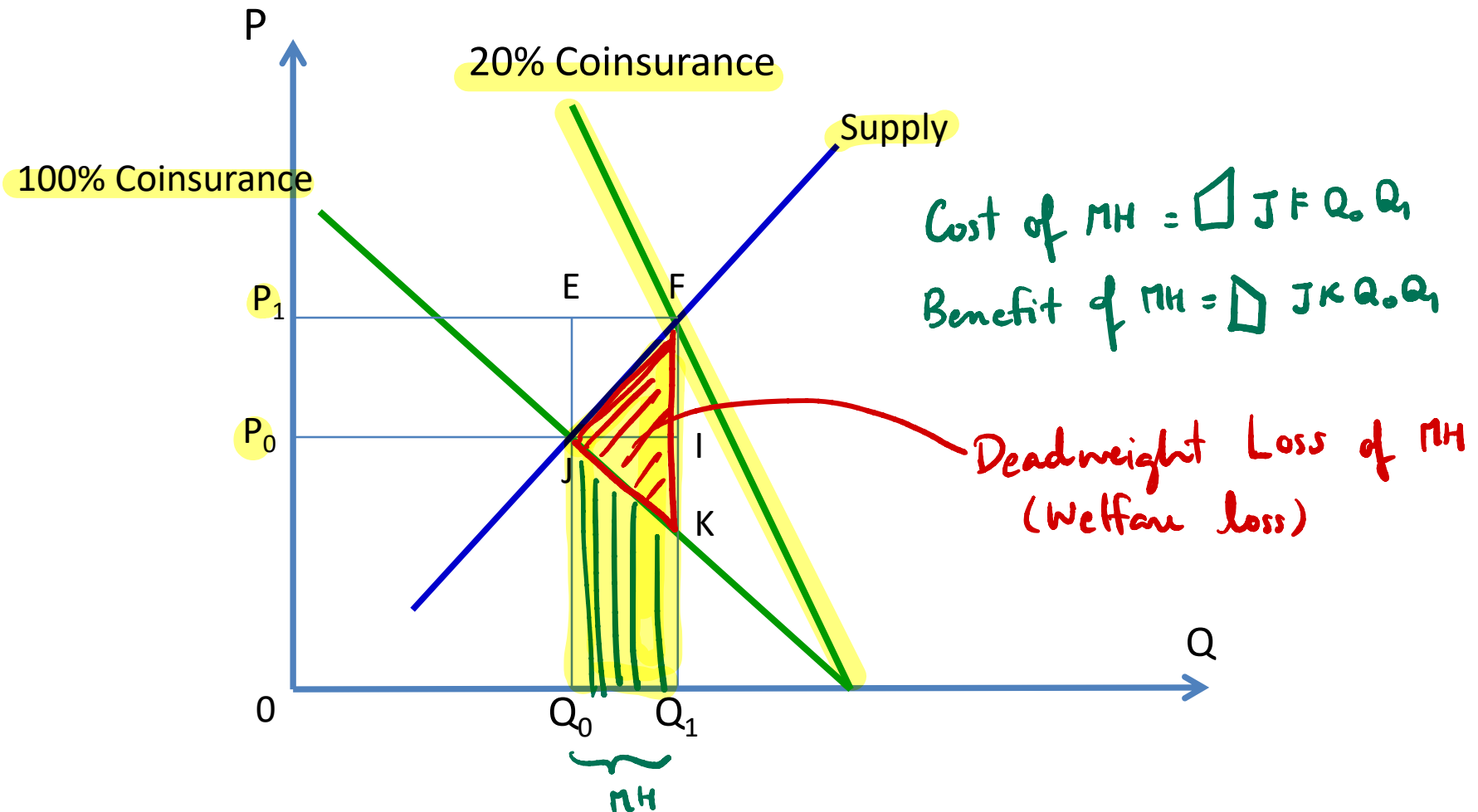


$\Delta ABC$  = welfare loss from  $MH_1$

increase in primary claim due to 2<sup>nd</sup> plan.  
 =  $(50 - 20) \times 5$   
 = \$150

$\square BOCF$  = welfare loss from  $MH_2$

# Welfare Loss (MC is not constant)



# The (New) Theory of Demand for Health Insurance

- So far, we have learned about the *conventional insurance theory*, which suggests that health insurance always creates a *welfare loss*.
- John Nyman's (1999) *new theory of demand for health insurance*:
  - Health insurance is demanded in order to obtain *an transfer of income when ill* (income transfers from those who remain healthy to those who become ill).
  - Health insurance generally *increases welfare*, mainly because of moral hazard which represents *access to health care that would otherwise be unaffordable*.

# Nyman's Model

- Some notations:

- $m_i$  is total medical care cost when illness occurs \$10,000

- $r$  is the premium

- $\pi$  is the probability of illness. 10%.

- $c$  = coinsurance rate (Note: we've assumed  $c=0$  previously.)

$$\text{AFP} = 10\% \times \$10,000 = \$1,000 \quad (\text{w/o coinsurance})$$

- Insurer sets a premium,  $r$ , at the actuarially fair level:

$$r = \pi(1-c)m_i$$

- The coverage payoff that the insurer pays to the beneficiary who becomes ill is equal to  $(1-c)m_i$ .

$$\text{If } c=0, \text{ coverage} = m_i$$

# Nyman's Model

- **Income transfers** are the portion of the payoff to the ill that is paid for by those who purchase insurance and remain healthy:
  - *Payoff* to ill:  $(1-c)m_i$
  - *Premium* paid by each insured:  $\pi(1-c)m_i$
  - *Income transfers* to ill:  $(1-\pi)(1-c)m_i$
- Example: Medical spending with insurance is \$10,000, coinsurance rate is 20%, and probability of illness is 0.02.
  - Each insured pays:  $c*m_i = \$2,000$  out of pocket 20% \* 10,000
  - ✓ • Insurer pays:  $(1-c)m_i = \underline{(1-0.02) \times \$10,000} = \$8,000$
  - • AFP:  $r = \pi(1-c)m_i = \underline{0.02 \times \$8,000} = \$160$
  - **Income transfers** are:  $\underline{(1-\pi)(1-c)m_i} = \$8,000 - \$160 = \$7,840$

# Diagram of $c$ , $\pi$ , and $m$ in Nyman's Model

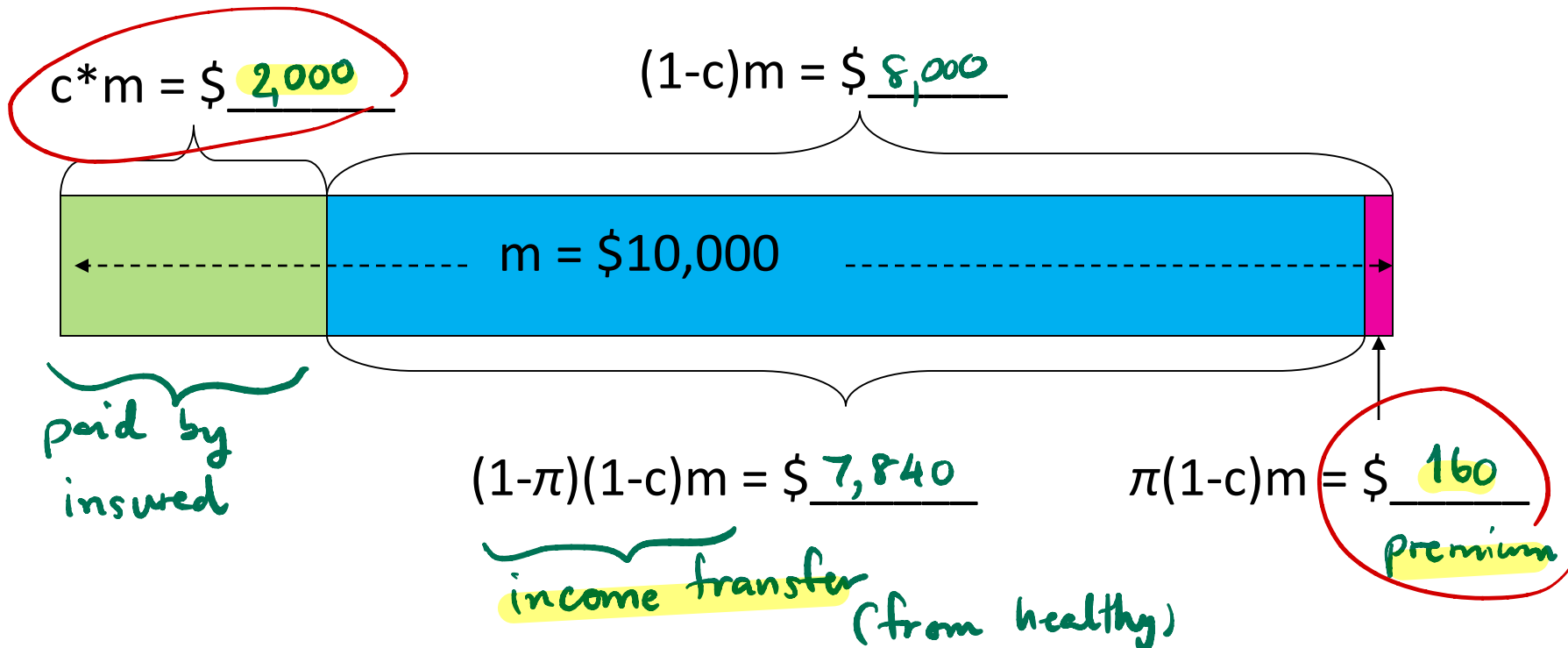
- Example

- $m = \$10,000$  : medical cost.

- $c=20\%$   $\Rightarrow 20\% \times \$10,000 = \$2,000$

- $\pi=2\%$  : Prob of ill

coinsurance } insured.  
premium }  
rest paid by insurer



# Elizabeth Example

- Elizabeth is diagnosed with breast cancer.
- *Without insurance*, she purchases
  - Mastectomy for \$20,000 ← Spending without insurance
- *With insurance* that pays for all her care, she receives the
  - Mastectomy for \$20,000,
  - A breast reconstruction for \$20,000
  - 2 extra days in the hospital for \$4,000

Spending with insurance = 44,000
- **Moral hazard spending:**
  - \$44,000 – \$20,000 = \$24,000 for breast reconstruction and hospital days

MH  
(extra  
HC)

# Elizabeth Example

- Question: Is the \$44,000 spending efficient?
- Assume that, if she had been paid off with a **lump sum payment** equal to the amount the insurer paid for her care (\$44,000), she would have purchased the **mastectomy** and the **breast reconstruction**, but **not the 2 extra days in the hospital**.
- Conclusion:
  - ↖ *necessary*
  - ↖ *not necessary.*
- ✓ • The **breast reconstruction** is *efficient* and *welfare* increasing because Elizabeth would have purchased that with the income transfer.
- The **2 extra days in the hospital** are *inefficient* and *welfare decreasing* because she only purchases them because the insurer had distorted the price.

# Illustration of Elizabeth's Welfare Gain

